

TITLE: Interaction-dependent effects of surface structure on microbial spatial self-organization

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RUNNING TITLE: Surface structure and self-organization

KEYWORDS: Microbial ecology, range expansion, self-organization, surface structure, pattern formation, denitrification

ABSTRACT

Surface-attached microbial communities consist of different cell-types that, at least to some degree, organize themselves non-randomly across space (referred to as spatial self-organization). While spatial self-organization can have important effects on the functioning, ecology, and evolution of communities, the underlying determinants of spatial self-organization remain unclear. Here, we hypothesize that the presence of physical objects across a surface can have important effects on spatial self-organization. Using pairs of isogenic strains of *Pseudomonas stutzeri*, we performed range expansion experiments in the absence or presence of physical objects and quantified the effects on spatial self-organization. We demonstrate that physical objects create local deformities along the expansion frontier, and these deformities increase in magnitude during range expansion. The deformities affect the densities of interspecific boundaries and diversity along the expansion frontier, and thus affect spatial self-organization, but the effects are interaction-dependent. For competitive interactions that promote sectorized patterns of spatial self-organization, physical objects increase the density of interspecific boundaries and diversity. In contrast, for cross-feeding interactions that promote dendritic patterns, they decrease the density of interspecific boundaries and diversity. These qualitatively different outcomes are likely caused by fundamental differences in the orientations of the interspecific boundaries. Thus, in order to predict the effects of physical objects on spatial self-organization, information is needed regarding the interactions present within a community and the general geometric shapes of spatial self-organization that emerge from those interactions.

INTRODUCTION

Surface-attached microbial communities are ubiquitous across our planet, contribute to all major biogeochemical processes, and have important roles in human health and disease [1-5]. These communities expand across space (*i.e.*, range expansion) as a consequence of growth and cell division (*e.g.*, cell shoving) [6-9] and active cell motility [3, 10]. During range expansion, different cell-types arrange themselves non-randomly across space and form spatial patterns [11-25], which is referred to as spatial self-organization [26-31]. Importantly, these patterns can be important determinants of community-level properties. For example, they can determine community-level productivity [13, 21, 32-35], the metabolic processes performed by communities [34, 36-39], the resistance and/or resilience of communities to environmental perturbations [40-42], and the evolutionary processes acting on communities [14, 22, 43-46]. Identifying the determinants of spatial self-organization is therefore important for our basic understanding of the structure, functioning and evolution of microbial communities [47].

One plausible determinant of spatial self-organization is the physical structure of the surface over which the microbial community expands [45, 48-52]. The majority of microbial range expansion studies have been conducted across smooth surfaces that lack physical objects [11-20, 22-26]. Yet, outside of controlled laboratory settings, physical objects are likely pervasive across surfaces. This then raises an important question: How do physical objects affect spatial self-organization? In other words, can we generalize results obtained with smooth surfaces to more complex surfaces that contain physical objects?

To address this question, consider a simplified community consisting of two cell-types with equivalent fitness. If a liquid suspension of the community is inoculated as a droplet onto a smooth surface containing no physical objects, the shape of the expansion frontier is approximately uniform and circular (*i.e.*, a circularity isoperimetric quotient $[\frac{perimeter^2}{4 \times \pi \times area}] \cong 1$ [53]) and can be described as the radius of curvature (R_C) of the inoculation area (Fig. 1A). In contrast, if a liquid suspension of the community is inoculated as a droplet onto a surface containing physical objects, where the physical objects are smaller than the inoculation area but larger than individual cells, then these physical objects can create deformities along the expansion frontier [45, 50, 51] (Fig. 1B). These deformities could result from two processes. First, if the physical objects lie behind the expansion frontier, the objects could deform the expansion frontier as a consequence of liquid-surface interactions and create local regions with smaller R_C (R_{SC}) and inverted curvature (R_{IC}) [51] (Fig. 1C). Second, if the physical objects lie ahead of the expansion frontier, the expansion frontier could eventually collide with the physical objects and deform the expansion frontier [50]. In both cases, the deformed expansion frontier would have a larger perimeter-to-area ratio and a shape that deviates from circular (*i.e.*, a circularity isoperimetric quotient > 1) (Fig. 1B).

Do these deformities along the expansion frontier affect spatial self-organization? Theoretical considerations and experimental investigations indicate that this is likely the case [45, 50, 51]. Consider again a simplified community consisting of two cell-types with equivalent fitness. As the community expands across space, the cell-types demix as a consequence of random sampling at the expansion frontier and the stochastic coalescence of interspecific boundaries [12, 14] (Fig. 1D). Theoretical considerations predict that the probability of stochastic boundary coalescence is negatively related to R_C [51]. Importantly,

if physical objects lie behind the expansion frontier, then they could create local regions of R_{SC} (Fig. 1C). The consequence is a larger angle between neighboring interspecific boundaries and a reduced probability of stochastic boundary coalescence, and we therefore expect more interspecific mixing and diversity along the expansion frontier [51] (Fig. 1E). In addition, the physical objects could also create local regions of R_{IC} (Fig. 1C). The consequence is that neighboring interspecific boundaries would be oriented towards coalescence, and we therefore expect the deterioration of interspecific mixing and diversity along the expansion frontier [51] (Fig. 1F). Finally, if physical objects lie ahead of the expansion frontier, the expansion frontier may eventually collide with those physical objects. The consequence is that some interspecific boundaries may become lost, and we therefore expect the deterioration of interspecific mixing and diversity along the expansion frontier [50] (Fig. 1G). Thus, the presence of physical objects can impose a variety of positive and negative effects on interspecific mixing and diversity.

Our objectives here were three-fold. First, we sought to experimentally test whether the presence of physical objects do indeed create deformities along the expansion frontier. Second, we wanted to determine what types of deformities (*i.e.*, local regions of R_{SC} [Fig. 1E], local regions of R_{IC} [Fig. 1F], or collisions [Fig. 1G]) have the predominant effects on interspecific mixing, diversity, and spatial self-organization along the expansion frontier. Third, we wanted to test whether our results are generalizable to different types of microbial interactions that promote the formation of fundamentally different patterns of spatial self-organization. To achieve these objectives, we performed range expansion experiments with synthetic microbial communities consisting of pairs of isogenic mutant strains of the denitrifying bacterium *Pseudomonas stutzeri* A1501 (Fig. 2A). One pair consists

of two strains that are genetically identical except that they express different fluorescent protein-encoding genes (referred to as complete reducers) [22, 54, 55] (Fig. 2A). When grown together in the absence of oxygen and with an exogenous supply of nitrate (NO_3^-) as the growth-limiting substrate, they have equivalent fitness and can completely reduce nitrate to dinitrogen gas (Fig. 2A). They therefore engage in a competitive interaction for nitrogen oxides [22, 54, 55]. The other pair consists of two strains that differ in their ability to reduce nitrogen oxides [22, 54, 56] (Fig. 2A). One strain contains a loss-of-function mutation in the *nirS* gene and can reduce nitrate but not nitrite (NO_2^-) (referred to as the producer) while the other strain contains a loss-of-function mutation in the *narG* gene and can reduce nitrite but not nitrate (referred to as the consumer) [22, 54, 56] (Fig. 2A). When grown together in the absence of oxygen and with an exogenous supply of nitrate as the growth-limiting substrate, the producer supports its growth via the reduction of nitrate to nitrite while the consumer supports its growth via the reduction of nitrite. They therefore engage in a nitrite cross-feeding interaction [22, 25, 54, 56]. Importantly, the two communities form fundamentally different patterns of spatial self-organization during range expansion (Figs. 2B and C). Namely, pairs of complete reducers (competitive interaction) form segregated or sectorized patterns where the interspecific boundaries are oriented approximately parallel to the axis of range expansion [22, 25] (Fig. 2B). In contrast, pairs of producer and consumer (nitrite cross-feeding interaction) form dendritic patterns where the dendrites originate from single points in the inoculation area and increase in width during range expansion, thus resulting in interspecific boundaries that are not oriented parallel to the axis of range expansion [22, 25] (Fig. 2C).

To address our main questions, we performed range expansion experiments in the presence or absence of physical objects for both pairs of complete reducers (competitive interaction) and for pairs of producer and consumer (nitrite cross-feeding interaction). We selected Nafion particles with a size distribution of 35-60 μm as physical objects, which is smaller than the size of the inoculation area [22, 25] but larger than the size of individual cells. Nafion particles are composed of a transparent and inert fluorocarbon polymer that is amenable to microscopic interrogation and have been successfully applied in other studies to create synthetic porous media [57-59]. While we could have used other particles as physical objects, such as spherical beads with precisely defined geometries, we selected Nafion particles due to their ability to mimic natural soils [57, 58]. After allowing the communities to expand, we then quantitatively compared how the presence of physical objects affect interspecific mixing, diversity, and spatial self-organization along the expansion frontier.

MATERIALS AND METHODS

Experimental model system. We described all of the strains used in this study in detail elsewhere [22, 54, 55]. For this study, our experimental model system is composed of four isogenic mutant strains of the bacterium *Pseudomonas stutzeri* A1501 (Fig. 2 and Supplementary Table S1). Briefly, the two complete reducers do not carry any disruptions in the denitrification pathway and can completely reduce nitrate (NO_3^-) to nitrite (NO_2^-), nitric oxide (NO), nitrous oxide (N_2O) and finally to dinitrogen gas (N_2) (Fig. 2 and Supplementary Table S1). In contrast, the producer carries a single loss-of-function deletion in the *nirS* gene and can reduce nitrate but not nitrite (Fig. 2 and Supplementary Table S1) while the

consumer carries a single loss-of-function deletion in the *narG* gene and can reduce nitrite but not nitrate (Fig. 2 and Supplementary Table S1). Importantly, the two complete reducers, producer and consumer are all isogenic mutants of each other that differ at only single genetic loci [22, 54, 55], thus minimizing any potential confounding factors that could arise when using more distantly related strains. We reported complete descriptions for the deletion of the *narG* and *nirS* genes elsewhere [54].

In addition to the genetic changes described above, each strain contains two additional genetic changes. First, all of the strains contain a single loss-of-function deletion in the *comA* gene [54] (Supplementary Table S1). This minimizes the probability that the strains will take up extracellular DNA [60], and thus minimizes the probability that they will recombine with each other when grown together. Second, each strain contains either the IPTG-inducible green fluorescent protein-encoding *egfp* gene or the cyan fluorescent protein-encoding *ecfp* gene (Fig. 2 and Supplementary Table S1), which enables us to distinguish and quantify the abundances of each strain when grown together [22, 25, 56]. We reported complete descriptions for the deletion of the *comA* gene and the introduction of the fluorescent protein-encoding genes elsewhere [22, 54, 55]. We previously reported that there are no observable differential costs for expressing different fluorescent protein-encoding genes for our isolates [55].

Range expansion experiments. We performed anaerobic range expansion experiments as described in detail elsewhere [22, 25], which is a modified version a protocol developed for aerobic range expansions [12]. Briefly, we first grew the two complete reducers, producer, and consumer independently in aerobic lysogeny broth (LB) medium overnight in a shaking

incubator at 37°C at 220 rpm. After reaching stationary phase, we adjusted the densities of each culture to an optical density at 600 nm of one (OD_{600}), centrifuged the cultures at 3600 x g for eight minutes at room temperature, discarded the supernatants, and suspended the cells in 1000 μ l of 0.9% (w/v) saline solution. We then transferred the cultures into a glove box (Coy Laboratory Products, Grass Lake, MI) containing a nitrogen (N_2):hydrogen (H_2) (97:3) anaerobic atmosphere, mixed the two complete reducers together or the producer and consumer together at a volumetric ratio of 1:1, and deposited 1 μ l of each mixture onto the center of a separate anaerobic LB agar plate amended with 1 mM of sodium nitrate ($NaNO_3$) and adjusted to pH 7.5 with 0.5 M NaOH. Because the complete reducers, producer and consumer are all isogenic mutants of each other and have identical optical properties, a volumetric ratio of 1:1 is equivalent to a cell number ratio of 1:1. We provided a complete description for the preparation of anaerobic LB agar plates elsewhere [22].

To assess the effects of physical objects on interspecific mixing, diversity, and spatial self-organization, we used Nafion particles with a size range of 35-60 μ m (Sigma-Aldrich, Buchs, Switzerland). Briefly, after we inoculated the anaerobic LB agar plates with pairs of complete reducers or pairs of producer and consumer, we incubated the plates for 48 h. This allowed for the suspension liquid from the inoculum to dissipate and for individual cells to attach to the LB agar surface. After 48 hours, we then deposited approximately 5 mg of dry Nafion particles (*i.e.*, the particles were not suspended in solution) to the inoculation area of each plate that was assigned to the physical object treatment group and continued to incubate the plates for a total of two weeks. We note here that the growth-limiting substrate is nitrate (NO_3^-) for all of our experiments, which we exogenously added to the LB agar that

resides below the Nafion particles. We therefore do not expect the Nafion particles, which reside on top of the LB agar, to constrain the diffusional supply of nitrate.

Microscopy and image analysis. We imaged the range expansions with a Leica TCS SP5 II confocal microscope (Leica Microsystems, Wetzlar, Germany) as described in detail elsewhere [22, 25]. Briefly, prior to imaging the range expansions, we exposed the LB agar plates to ambient air for 1 h to induce maturation of the fluorescent proteins [22, 25]. We then quantified the circularity of the range expansion area using the circularity isoperimetric quotient ($\frac{perimeter^2}{4 \times \pi \times area}$) [53]. We next quantified the number of interspecific boundaries between two complete reducers or between the producer and consumer by first plotting a line at 50 pixels from the leading edge of the range expansion area. We set this distance to avoid possible microscopy artefacts that could emerge due to uneven illumination at the expansion frontier. We then measured the number of color transitions along the internal end-joined line, where the number of color transitions are equivalent to the number of interspecific boundaries along the line. We note here that these measures are inherently one-dimensional in nature. The advantage of this approach is that we do not have to discriminate between the inoculation and expansion areas, which is technically difficult. The disadvantage, however, is that we cannot measure the number of boundary coalescence events, which would require discriminating between the inoculation and expansion areas and applying two-dimensional methodologies. Finally, we quantified the fractal dimension of the dendrites formed by the producer and consumer using the fractal box-counting method as described in detail elsewhere [22].

Statistical analysis. We used parametric methods for all of our statistical tests and considered a P-value < 0.05 to be statistically significant. We reported the type of statistical test, the sample size for each test, and the exact P-value for each test in the results section.

RESULTS

Physical objects create deformities along the expansion frontier. We first tested whether the addition of physical objects to a surface creates immediate deformities along an expansion frontier. To accomplish this, we assembled pairs of complete reducers together (1:1 initial cell number ratio) and deposited them onto separate replicated LB agar plates (n = 18). We then added Nafion particles as physical objects to half the plates, immediately interrogated the expansion frontier via microscopy, and quantified the immediate effects of physical objects on the shape of the expansion frontier.

We found that the addition of physical objects immediately created deformities along the expansion frontier. In the absence of physical objects, the expansion frontier slightly deviated from circular (Fig. 3A) with a mean circularity isoperimetric quotient among independent replicates of 1.14 (SD = 0.081, n = 9) (Fig. 3D). In the presence of physical objects, in contrast, the expansion frontier strongly deviated from circular (Fig. 3B) with a mean circularity isoperimetric quotient among independent replicates of 3.22 (SD = 0.96, n = 9) (Fig. 3E). Overall, the addition of physical objects significantly increased the circularity isoperimetric quotient by nearly three-fold when compared to the absence of physical objects (two-sample two-sided t-test; $P = 3 \times 10^{-5}$, n = 9), indicating a significant increase in the perimeter-to-area ratio. Moreover, the presence of physical objects clearly created

deformities along the expansion frontier that included both local regions of R_{SC} and R_{IC} (Fig. 3C). Thus, adding physical objects to the surface does indeed immediately create deformities along the expansion frontier.

We next tested whether deformities created immediately after the addition of physical objects persist as the communities expand across space. To accomplish this, we allowed pairs of complete reducers (1:1 initial cell number ratio) ($n = 3$ without and with physical objects) or pairs of producer and consumer (1:1 initial cell number ratio) ($n = 9$ without and with physical objects) to expand for two weeks, interrogated the expansion frontier via microscopy, and quantified the shape of the expansion frontier. In the absence of physical objects, the expansion frontier continued to slightly deviate from circular (Fig. 4A) with a mean circularity isoperimetric quotient among independent replicates of 1.45 (SD = 0.15, $n = 12$) (Fig. 4C). In the presence of physical objects, in contrast, the expansion frontier strongly deviated from circular (Fig. 4B) with a mean circularity isoperimetric quotient among independent replicates of 8.04 (SD = 3.3, $n = 12$) (Fig. 4D). This latter value is significantly greater than the value observed immediately after the addition of physical objects (two-sample two-sided t-test; $P = 0.001$, $n_1 = 12$, $n_2 = 9$) (Fig. 3D). Overall, after two weeks of range expansion in the presence of physical objects, the circularity isoperimetric quotient significantly increased by more than five-fold when compared to range expansion in the absence of physical objects (two-sample two-sided t-test; $P = 9 \times 10^{-7}$, $n = 12$). Thus, the deformities created immediately after the addition of physical objects not only persist after the onset of range expansion, but also increase in magnitude during range expansion.

Effect of deformities on the general geometric shapes of spatial self-organization. We next tested whether the addition of physical objects affects the general geometric shapes of spatial self-organization that form as the communities expand across space. To accomplish this, we analyzed the geometric shapes of spatial self-organization that emerged after two weeks of range expansion using the same images obtained from the previously described experiment. Because we deposited physical objects both behind and in front of the initial expansion frontier (Fig. 3B) and allowed the communities to expand across space, deformities would be created that consist of local regions of R_{SC} (Fig. 1E) and R_{IC} (Fig. 1F) and by collisions with physical objects (Fig. 1G).

We first tested whether the deformities created by physical objects affect the general geometric shapes of spatial self-organization formed by pairs of complete reducers (1:1 initial cell number ratio) ($n = 3$ without and with physical objects). In the absence of physical objects, the two complete reducers rapidly segregated into sectors as they expanded and formed interspecific boundaries oriented approximately parallel to the axis of range expansion (Figs. 5A and 5B). This is consistent with our previously reported observations [22, 25] and with observations from similar experiments conducted with pairs of cell-types that have equivalent fitness [12, 14]. Moreover, the interspecific boundaries underwent occasional stochastic boundary coalescence during range expansion (Fig. 5B, white arrows), indicating an increase in sector width and a reduction in interspecific mixing and diversity along the expansion frontier. In the presence of physical objects, the two complete reducers again rapidly segregated into sectors as they expanded and formed interspecific boundaries oriented approximately parallel to the axis of range expansion (Figs. 5C and 5D). As in the absence of physical objects, the interspecific boundaries also underwent occasional

stochastic boundary coalescence during range expansion (Fig. 5D, white arrows), again indicating an increase in sector width and a reduction in interspecific mixing and diversity along the expansion frontier. Importantly, the geometric shapes of the sectors and interspecific boundaries were qualitatively similar regardless of whether physical objects were not or were present (Figs. 5B and 5D). Thus, deformities along the expansion frontier do not qualitatively affect the general geometric shapes of spatial self-organization formed by pairs of complete reducers.

We next tested whether the deformities created by physical objects affect the general geometric shapes of spatial self-organization formed by pairs of producer and consumer (1:1 initial cell number ratio) ($n = 9$ without and with physical objects). In the absence of physical objects, the producer and consumer did not form sectors but instead formed dendrites of the consumer that protruded into the producer (Figs. 5E and 5F), which is consistent with our previously reported observations [22, 25]. These dendrites tend to originate from single points in the inoculation area, increase in width during range expansion, and have interspecific boundaries that are not oriented parallel to the axis of range expansion (Fig. 5F), which are again features consistent with our previously reported observations [22, 25]. The dendrites display a fractal-like property with a mean fractal dimension among independent replicates of 1.73 ($SD = 0.034$, $n = 9$) (Fig. 6A), which is statistically indistinguishable from the fractal dimension for the dendrites described in our previous investigation with the same experimental system [22]. In the presence of physical objects, the producer and consumer again rapidly formed dendrites as they expanded (Fig. 5G and 5H). Moreover, the mean fractal dimension of the dendrites formed in the presence of physical objects was 1.72 ($SD = 0.024$, $n = 9$) (Fig. 6B) and was statistically indistinguishable

from the mean fractal dimension measured in the absence of physical objects (two-sample two-sided t-test; $P = 0.33$, $n = 9$) (Fig. 6). Thus, as with the general geometric shapes of spatial self-organization formed by pairs of complete reducers, deformities along the expansion frontier also do not affect the general geometric shapes of spatial self-organization formed by pairs of producer and consumer.

Effect of deformities on the density of interspecific boundaries. We next tested whether deformities created by physical objects affect the density of interspecific boundaries at the expansion frontier. The density of interspecific boundaries provides a measure of interspecific mixing and diversity along the expansion frontier. We chose to measure the density of interspecific boundaries rather than the absolute number of interspecific boundaries because the length of the expansion frontier dramatically increases in response to Nafion particles (Figs. 3 and 4). Thus, if we were to use the absolute number of interspecific boundaries, we would expect our experiments with Nafion particles to have more interspecific boundaries simply because of the longer expansion frontier. To achieve our objective, we first measured the numbers of interspecific boundaries after two weeks of range expansion using the same images obtained from the previously described experiment, all of which were conducted with pairs of complete reducers (1:1 initial cell number ratio) ($n = 3$ without and with physical objects) or with pairs of producer and consumer (1:1 initial cell number ratio) ($n = 9$ without and with physical objects). We then quantified the mean density of interspecific boundaries among independent replicates.

We first tested whether deformities created by physical objects affect the density of interspecific boundaries formed by pairs of complete reducers along the expansion frontier.

We found that, in the absence of physical objects, the mean density of interspecific boundaries was 0.0073 boundaries per μm (SD = 0.0016, $n = 3$) (Fig. 7A). In the presence of physical objects, the mean density of interspecific boundaries was 0.0258 boundaries per μm (SD = 0.0086, $n = 3$) (Fig. 7B). Overall, we observed a significantly larger mean density of interspecific boundaries in the presence of physical objects than in the absence of physical objects (two-sample two-sided t-test; $P = 0.021$, $n = 3$) (Fig. 7). The theoretical considerations that we outlined in Fig. 1 predict that local regions R_{SC} should increase the density of interspecific boundaries along the expansion frontier (Fig. 1E) while local regions of R_{IC} and particle collisions should both decrease the density of interspecific boundaries along the expansion frontier (Figs. 1F and 1G). Thus, because we experimentally observed that physical objects increase the density of interspecific boundaries along the expansion frontier, our results indicate that local regions of R_{SC} likely have the dominant effect while local regions of R_{IC} and collisions with physical objects likely have small effects on interspecific mixing, diversity, and spatial self-organization for pairs of complete reducers.

One alternative explanation for why physical objects might affect the density of interspecific boundaries for pairs of complete reducers (competitive interaction) along the expansion frontier is that physical objects also affect the initial cell density along the expansion frontier. Briefly, we used the same number of cells for experiments conducted without and with physical objects. The addition of physical objects, however, increased the length of the expansion frontier (*i.e.*, physical objects increased the circularity isoperimetric quotient [Fig. 3]). The initial cell density along the expansion frontier would therefore have been smaller, as the same number of cells were distributed along a longer length of frontier. The smaller initial cell density along the expansion frontier should have either no effect on [12] or result

in a smaller number of interspecific boundaries [19]. However, we observed the opposite outcome, where physical objects increased rather than decreased the density of sectors along the expansion frontier. Thus, the effect of physical objects on the length of the expansion frontier, and thus on the initial cell density along the expansion frontier, cannot explain our results for pairs of complete reducers.

We finally tested whether deformities created by physical objects affect the density of interspecific boundaries formed by pairs of producer and consumer along the expansion frontier. We found that, in the absence of physical objects, the mean density of interspecific boundaries was 0.208 boundaries per μm (SD = 0.050, $n = 9$) (Fig. 8A). In the presence of physical objects, the mean density of interspecific boundaries was 0.103 boundaries per μm (SD = 0.024, $n = 9$) (Fig. 8B). Overall, we observed a significantly smaller mean density of interspecific boundaries in the presence of physical objects than in the absence of physical objects (two-sample two-sided t-test; $P = 3 \times 10^{-5}$, $n = 9$) (Fig. 8), which is qualitatively opposite to what we observed for pairs of complete reducers (Fig. 7). Again, the theoretical considerations that we outlined in Fig. 1 predict that local regions R_{SC} should increase the density of interspecific boundaries along the expansion frontier (Fig. 1E) while local regions of R_{IC} and particle collisions should both decrease the density of interspecific boundaries along the expansion frontier (Fig. 1F and 1G). Thus, because we experimentally observed that physical objects decrease the density of interspecific boundaries along the expansion frontier, our results indicate that local regions of R_{SC} have relatively small effects while local regions of R_{IC} and/or collisions with physical objects likely have the dominant effects on interspecific mixing, diversity, and spatial self-organization for pairs of producer and consumer.

396

397 **DISCUSSION**

398

399 We show here that physical objects can have important effects on the interspecific mixing,
400 diversity, and spatial self-organization of microbial communities. Perhaps surprisingly, the
401 effects of physical objects on the density of interspecific boundaries depends on the type of
402 interaction that occurs between the resident cell-types. Competitive interactions that
403 promote segregation and the formation of sectors with interspecific boundaries oriented
404 approximately parallel to the axis of range expansion are positively affected by physical
405 objects, where physical objects result in increased numbers of interspecific boundaries (Fig.
406 7). Conversely, cross-feeding interactions that promote the formation of dendrites with
407 interspecific boundaries not oriented parallel to the axis of range expansion are negatively
408 affected by physical objects, where physical objects result in decreased numbers of
409 interspecific boundaries (Fig. 8). Thus, in order to make even qualitative predictions
410 regarding the effects of physical objects on interspecific mixing, one needs information
411 regarding the interactions that are present within a community and the general geometric
412 shapes of spatial self-organization likely to emerge from those interactions.

413

414 Why do physical objects have interaction-dependent effects on interspecific mixing within
415 microbial communities? One plausible explanation is that different interactions result in
416 different orientations of the interspecific boundaries [22, 25]. Consider local regions of R_{SC}
417 formed by physical objects (Fig. 1E). We expect these local regions to have potentially
418 profound effects at preventing or delaying the coalescence of interspecific boundaries
419 formed by competitive interactions. Briefly, when the competing cell-types have equivalent

fitness, sectors form and the boundaries are oriented approximately parallel to the axis of range expansion [12, 14] (Figs. 2 and 5). Stochastic processes then act on the boundaries resulting in a random walk-like behavior [12, 14]. Given sufficient time, this random walk-like behavior can result in the stochastic coalescence of neighboring boundaries [12, 14] (Fig. 5). Local regions of R_{SC} increase the angle between these neighboring boundaries (Fig. 1E), which would decrease the probability of stochastic boundary coalescence [51]. In contrast, we expect local regions of R_{SC} to have relatively small effects at preventing the coalescence of the interspecific boundaries formed by cross-feeding interactions. Cross-feeding interactions promote the formation of dendrites that do not have boundaries oriented parallel to the axis of range expansion. Instead, the boundaries diverge from each other as the dendrites expand across space [22, 25] (Figs. 2 and 5). Because the boundaries are not oriented parallel to the axis of range expansion, a subset of the neighboring boundaries will inevitably be oriented towards coalescence regardless of the radius of curvature of the expansion frontier. Thus, interactions that form interspecific boundaries oriented parallel to the axis of range expansion will be more affected by local regions of R_{SC} than interactions that form interspecific boundaries not oriented parallel to the axis of range expansion, thus providing an explanation for why local regions of R_{SC} have larger effects for pairs of complete reducers (competitive interaction) than for pairs of producer and consumer (nitrite cross-feeding interaction).

Similar arguments can be made for local regions of R_{IC} formed by physical objects (Fig. 1F). We expect these local regions to have smaller effects at promoting the coalescence of interspecific boundaries formed by competitive interactions than those formed by nitrite cross-feeding interactions. As discussed above, the boundaries formed by competitive

interactions are oriented approximately parallel to the axis of range expansion [12, 14] (Figs. 2 and 5), and local regions of R_{IC} will inevitably orient them towards coalescence (Fig. 1F). However, it will take a relatively long period of time for coalescence to occur, as they nevertheless remain oriented parallel to the axis of range expansion. In contrast, the boundaries formed by nitrite cross-feeding interactions are not oriented parallel to the axis of range expansion [22, 25] (Figs. 2 and 5), and a subset of the neighboring boundaries will inevitably be oriented towards coalescence regardless of whether they occur within a local region of R_{IC} or not. If they are located within a local region of R_{IC} , these neighboring boundaries will be oriented even more sharply towards coalescence, thus resulting in a relatively short period of time for coalescence to occur. Thus, interactions that form interspecific boundaries oriented parallel to the axis of range expansion will be less affected by local regions of R_{IC} than interactions that form interspecific boundaries not oriented parallel to the axis of range expansion, thus providing another explanation for why local regions of R_{SC} have smaller effects for pairs of complete reducers (competitive interaction) than for pairs of producer and consumer (nitrite cross-feeding interaction).

What can our results tell us about the maintenance of diversity within microbial communities? We used the number of interspecific boundaries as a measure of diversity. Briefly, the number of interspecific boundaries is a proxy measure for how many individuals migrated out of the inoculation area and contributed to range expansion [12, 14]. If genetic heterogeneity occurs within populations, then more of that genetic heterogeneity will be maintained during range expansion as the number of interspecific boundaries increases. Thus, because physical objects affect the number of interspecific boundaries, physical objects also affect the diversity of microbial communities. Physical objects may therefore

not only be an important determinant of spatial self-organization, but also be an important determinant of the diversity of spatially structured microbial communities.

Under what environmental conditions do we expect the presence of physical objects to have effects? We can address this question by considering what types of interactions are likely to occur under different environmental conditions. In our case, we investigated a linear metabolic pathway (*e.g.* denitrification) where a competitive interaction occurs between completely denitrifying strains while a cross-feeding interaction occurs between partially denitrifying strains. Importantly, previous theoretical studies predict that low substrate supply selects for completely consuming strains (and thus competitive interactions) while high substrate supply selects for partially consuming strains (and thus cross-feeding interactions) [61, 62]. Combined with these theoretical studies, our results therefore lead to the following prediction. In environments with low substrate supply, we expect competitive interactions to predominate. The presence of physical objects would then increase interspecific mixing and diversity along the expansion frontier. In contrast, in environments with high substrate supply, we expect cross-feeding interactions to predominate. The presence of physical objects would then decrease interspecific mixing and diversity along the expansion frontier. Importantly, this prediction is experimentally testable and generalizable across a wide variety of metabolic processes, environments, and microbial communities.

DATA ACCESSIBILITY

All data and codes required to reproduce the figures and conclusions are available on the Eawag Research Data Institutional Collection (ERIC) repository.

AUTHORS' CONTRIBUTIONS

D.C. and D.R.J. conceived the research questions and designed the methodology and experiments; D.C., A.C. and V.M. performed the experiments; D.C. and D.R.J. analyzed and interpreted the data; D.C. and D.R.J. wrote the manuscript.

COMPETING INTERESTS

We declare that we have no competing interests.

FUNDING

This work was supported by grants from the Swiss National Science Foundation (grant numbers 31003A_149304 and 31003A_176101) awarded to D.R.J.

ACKNOWLEDGEMENTS

We thank Benedict Borer, Emanuel A. Fronhofer, Sara Mitri, Dani Or, and Jan Roelof van der Meer for helpful discussions.

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FIGURE LEGENDS

Figure 1. Effect of physical objects on spatial self-organization. A) In the absence of physical objects, the initial expansion frontier is approximately uniform and has a circularity isoperimetric quotient approximately equal to one. B) In the presence of physical objects (grey circles), the initial expansion frontier contains local deformities, deviates from circular, and has a circularity isoperimetric quotient greater than one. C) Magnification of deformities along the initial expansion frontier produced by the addition of physical objects (grey circles). The deformities consist of local regions of small R_c (R_{sc}) and inverted curvature (R_{ic}). D) At local regions of large R_c , the angle between neighboring interspecific boundaries is relatively small, which increases the probability of stochastic boundary coalescence and decreases interspecific mixing and diversity along the expansion frontier. E) At local regions of small R_c (R_{sc}), the angle between neighboring interspecific boundaries is relatively large, which decreases the probability of stochastic boundary coalescence and increases interspecific mixing and diversity along the expansion frontier. F) At local regions of inverted curvature (R_{ic}), neighboring interspecific boundaries are oriented towards coalescence, which decreases interspecific mixing and diversity along the expansion frontier. G) Collision of an expansion frontier into a physical object. If the physical object is larger than the length-scale of spatial self-organization, then the collision causes some interspecific boundaries to become lost and decreases interspecific mixing and diversity along the expansion frontier.

Figure 2. Experimental model system used in this study. A) Our experimental model system is composed of four isogenic mutant strains of *P. stutzeri*. The two complete reducer strains are genetically identical except that they express either the cyan fluorescent protein-

encoding *ecfp* gene or the green fluorescence protein-encoding *egfp* gene. The producer contains a loss-of-function mutation in the *nirS* gene and can reduce nitrate (NO_3^-) but not nitrite (NO_2^-). The consumer contains a loss-of-function mutation in the *narG* gene and can reduce nitrite but not nitrate. In addition, the producer expresses the cyan fluorescence protein-encoding *ecpf* gene while the consumer expresses the green fluorescence protein-encoding *egfp* gene. When the two complete reducer strains are grown together with nitrate as the growth-limiting substrate, they have equivalent fitness and engage in a competitive interaction for nitrogen oxides. When the producer and consumer are grown together with nitrate as the growth-limiting substrate, they engage in a nitrite cross-feeding interaction. Thick arrows indicate the nitrogen oxides that can be reduced by each strain. Definitions: Nar, nitrate reductase; Nir, nitrite reductase; Nor, nitric oxide reductase; Nos, nitrous oxide reductase. B) Pattern of spatial self-organization formed by pairs of complete reducers (1:1 initial cell number ratio) after two weeks of range expansion. One complete reducer carried the cyan fluorescent protein-encoding *ecfp* gene (shown in magenta) while the other carried the green fluorescent protein-encoding *egfp* gene (shown in green). C) Pattern of spatial self-organization formed by pairs of producer and consumer (1:1 initial cell number ratio) after two weeks of range expansion. The producer carried the cyan fluorescent protein-encoding *ecfp* gene (shown in magenta) while the consumer carried the green fluorescent protein encoding *egfp* gene (shown in green). The scale bars are equivalent to 1000 μm .

Figure 3. Circularity of the expansion frontier immediately after the addition of physical objects. Patterns of spatial self-organization formed by pairs of complete reducers (1:1 initial cell number ratio) (competitive interaction) A) in the absence of physical objects or B)

immediately after the addition of physical objects. One complete reducer carried the cyan fluorescent protein-encoding *ecfp* gene (shown in magenta) while the other carried the green fluorescent protein-encoding *egfp* gene (shown in green). The scale bars are equivalent to 1000 μ m. The circularity isoperimetric quotients for range expansions C) in the absence of physical objects or D) immediately after the addition of physical objects.

Figure 4. Circularity of the expansion frontier after two weeks of range expansion in the absence or presence of physical objects. Patterns of spatial self-organization formed by pairs of complete reducers (1:1 initial cell number ratio) (competitive interaction) after two weeks of range expansion A) in the absence of physical objects or B) in the presence of physical objects. One complete reducer carried the cyan fluorescent protein-encoding *ecfp* gene (shown in magenta) while the other carried the green fluorescent protein-encoding *egfp* gene (shown in green). The scale bars are equivalent to 1000 μ m. The circularity isoperimetric quotients for range expansions of pairs of complete reducers (n = 3) and pairs of producer and consumer (1:1 initial cell number ratio) (nitrite cross-feeding interaction) (n = 9) C) in the absence of physical objects or D) immediately after the addition of physical objects.

Figure 5. Effect of physical objects on the general geometric shapes of spatial self-organization. Patterns of spatial self-organization formed by pairs of complete reducers (1:1 initial cell number ratio) (competitive interactions) after two weeks of range expansion A-B) in the absence of physical objects or C-D) in the presence of physical objects. One complete reducer carried the cyan fluorescent protein-encoding *ecfp* gene (shown in magenta) while the other carried the green fluorescent protein-encoding *egfp* gene (shown in green). Panels

B and D are magnifications of panels A and C, respectively. Patterns of spatial self-organization formed by pairs of producer and consumer (1:1 initial cell number ratio) (nitrite cross-feeding interaction) after two weeks of range expansion *E-F*) in the absence of physical objects or *G-H*) in the presence of physical objects. The producer carried the cyan fluorescent protein-encoding *ecfp* gene (shown in magenta) while the consumer carried the green fluorescent protein-encoding *egfp* gene (shown in green). Panels F and H are magnifications of panels E and G, respectively. All scale bars are equivalent to 1000 μm . White arrows indicate events of stochastic boundary coalescence.

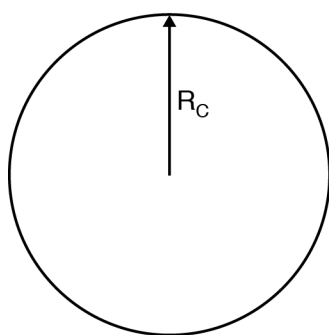
Figure 6. Fractal dimension of dendrites in the absence or presence of physical objects. The fractal dimension for pairs of producer and consumer (1:1 initial cell number ratio) (nitrite cross-feeding interaction) after two weeks of range expansion *A*) in the absence of physical objects or *B*) in the presence of physical objects. The fractal dimension was measured using the fractal box counting method.

Figure 7. Density of interspecific boundaries for pairs of complete reducers (1:1 initial cell number ratio) (competitive interaction) in the absence or presence of physical objects. The density of interspecific boundaries is the number of boundaries per μm of expansion frontier after two weeks of range expansion. Densities are for range expansions *A*) in the absence of physical objects or *B*) in the presence of physical objects.

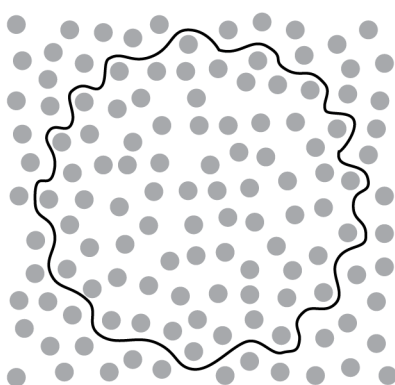
Figure 8. Density of interspecific boundaries for pairs of producer and consumer (1:1 initial cell number ratio) (nitrite cross-feeding interaction) in the absence or presence of physical objects. The density of interspecific boundaries is the number of boundaries per μm of

743 expansion frontier after two weeks of range expansion. Densities are for range expansions

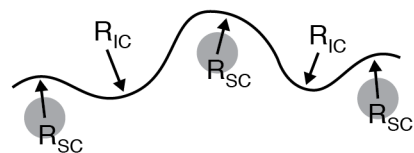
744 *A*) in the absence of physical objects or *B*) in the presence of physical objects.

A

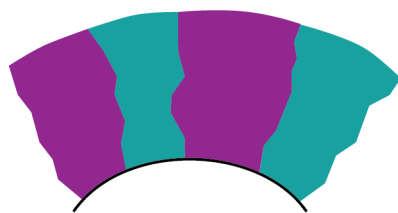
$$\text{Circularity} = P^2/4\pi A = 1$$

B

$$\text{Circularity} = P^2/4\pi A > 1$$

C**D**

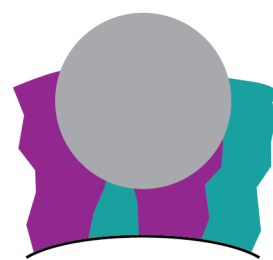
Large curvature, R_C

E

Small curvature, R_{SC}

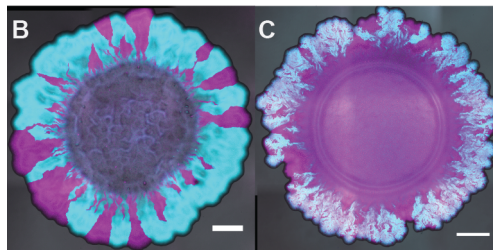
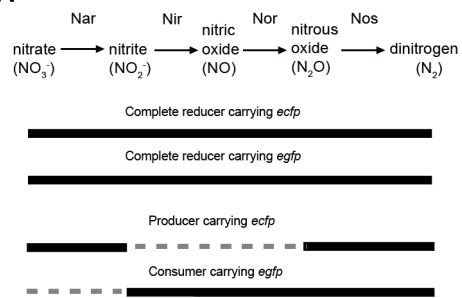
F

Inverted curvature, R_{IC}

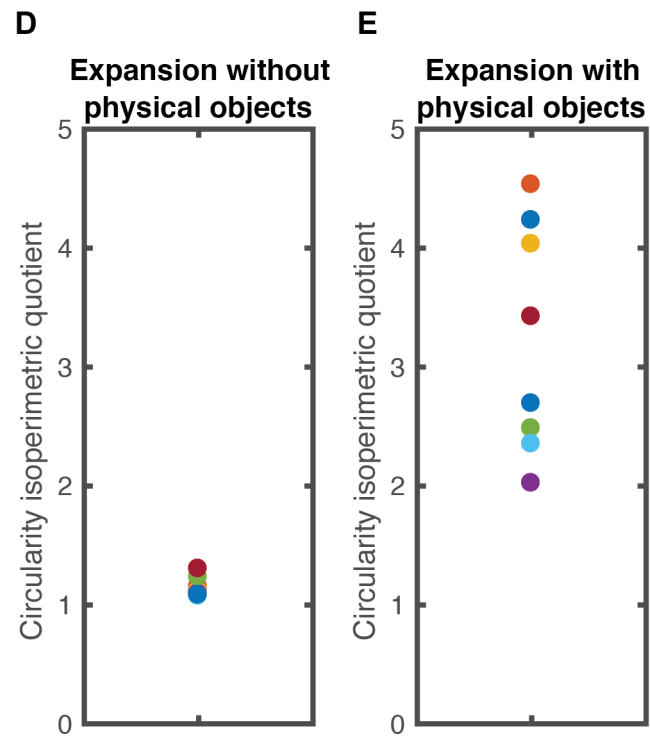
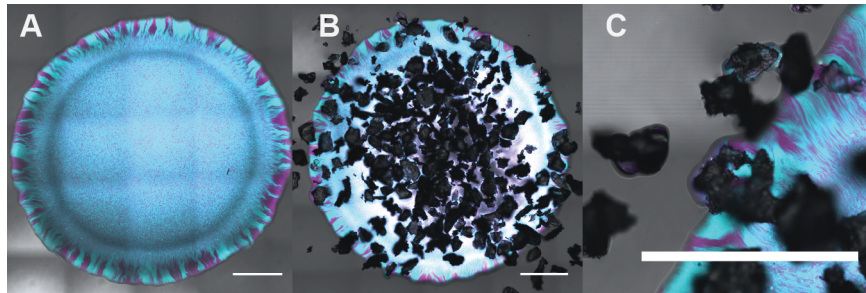
G

Collision

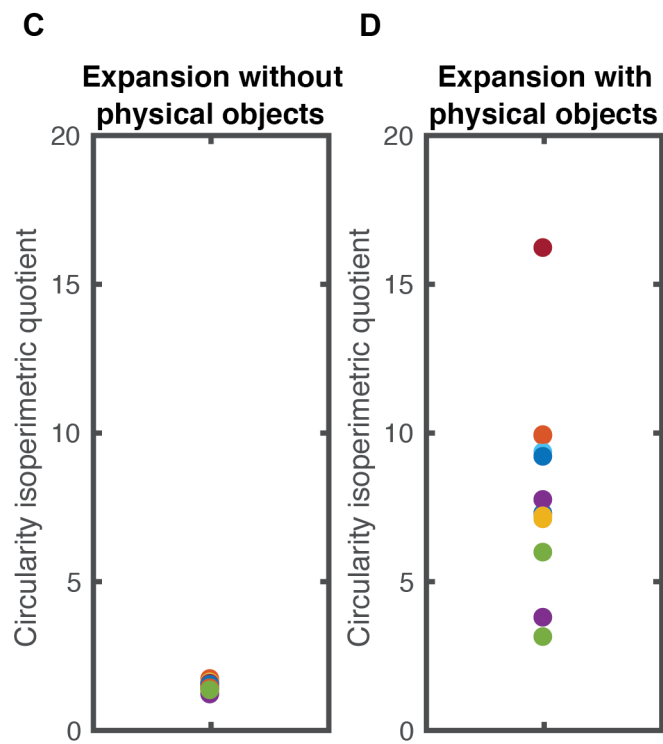
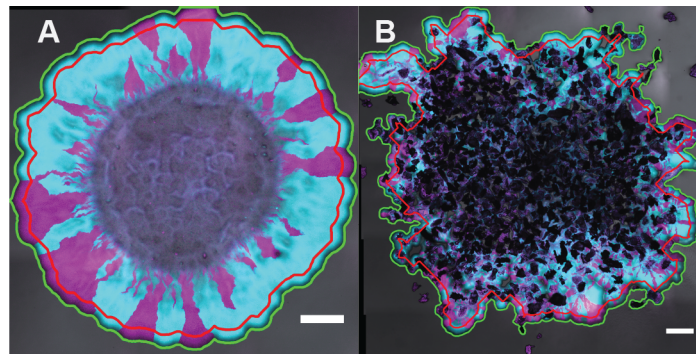
A

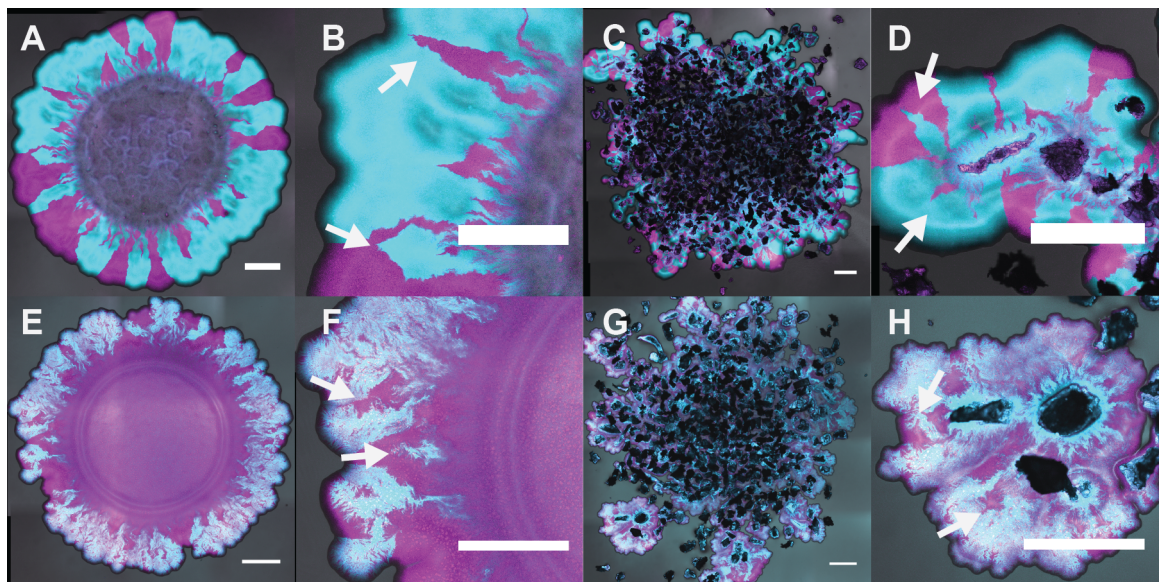


Complete reducers (competitive interaction)

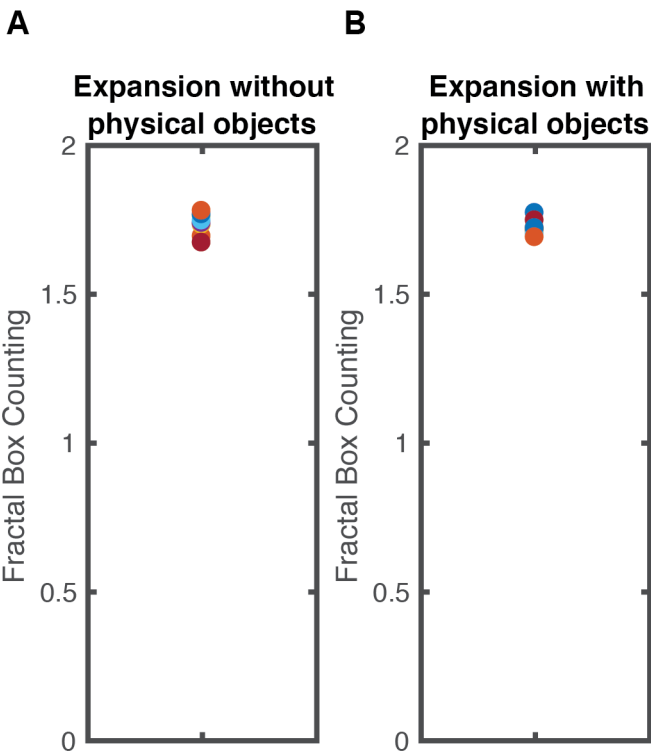


Complete reducers (competitive interaction)

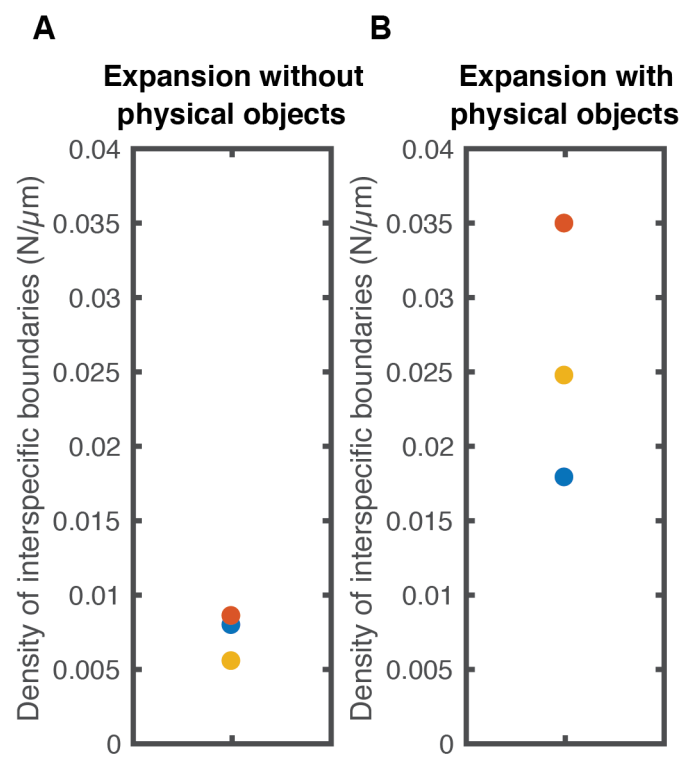




Producer and consumer (cross-feeding interaction)



Complete reducers (competitive interaction)



Producer and consumer (cross-feeding interaction)

