Estimating the concentration of total suspended solids in inland and coastal waters from Sentinel-2 MSI: A semi-analytical approach

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ABSTRACT

Inland and coastal waters provide key ecosystem services and are closely linked to human well-being. In this study, we propose a semi-analytical method, which can be applied to Sentinel-2 Multispectral Instrument (MSI) images to retrieve high spatial-resolution total suspended solids (TSS) concentration in a broad spectrum of aquatic ecosystems ranging from clear to extremely turbid waters. The presented approach has four main steps. First, the remote sensing reflectance (Rrs) at a band lacking in MSI (620 nm) is estimated through an empirical relationship from Rrs at 665 nm. Second, waters are classified into four types (clear, moderately turbid, highly turbid, and extremely turbid). Third, semi-analytical algorithms are used to estimate the particulate backscattering coefficient (bwp) at a reference band depending on the water types. Last, TSS is estimated from bwp at the reference band. Validation and comparison of the proposed method with three existing methods are performed using a simulated dataset (N = 1000), an in situ dataset collected from global inland and coastal waters (N = 1265) and satellite matchups (N = 40). Results indicate that the proposed method can improve TSS estimation and provide accurate retrievals of TSS from all three datasets, with a median absolute percentage error (MAPE) of 14.88 %, 31.50 % and 41.69 % respectively. We also present comparisons of TSS mapping between the Sentinel-3 Ocean and Land Colour Instrument (OLCI) and MSI in Lake Kasumigaura, Japan and the Tagus Estuary, Portugal. Results clearly demonstrate the advantages of using MSI for TSS monitoring in small water bodies such as rivers, river mouths and other nearshore waters. MSI can provide more detailed and realistic TSS estimates than OLCI in these water bodies. The proposed TSS estimation method was applied to MSI images to produce TSS time-series in Lake Kasumigaura, which showed good agreements with in situ and OLCI-derived TSS time-series.

1. Introduction

Over half of the global population live within 3 km of a fresh water body (Kummu et al., 2011), while 23 % live in coastal zones (Small & Nicholls, 2003). Inland and coastal waters provide fundamental ecosystem services such as drinking water provision, fisheries, biodiversity conservation, irrigation water provision, transportation, electricity production, recreation and tourism (Schallenberg et al., 2013; Reynaud & Lanzanova, 2017; Sterner et al., 2020; Heino et al., 2021). Efficient water quality monitoring of inland and coastal waters is required to support water management and decision-making to ensure the sustainable use of these resources.

Ocean colour sensors, such as the Medium Resolution Imaging Spectrometer (MERIS) and Ocean and Land Colour Instrument (OLCI)
with a spatial resolution of 300 m, and the Moderate Resolution Imaging Spectroradiometer (MODIS) with a spatial resolution of 1000 m, have been widely used to monitor water quality in relatively large lakes and coastal waters (Gons et al., 2008; Binding et al., 2012; Vundo et al., 2019; Jiang et al., 2019; Shen et al., 2020). However, 99% of the approximately 171 million lakes on Earth are smaller than 1 km², covering ~40% of the global lake area (Verpoorter et al., 2014). This large number of small lakes highlights that most global lakes are difficult to monitor using medium-resolution satellite images such as the ones acquired from MERIS and OLCI, given that at least nine pixels (0.3 km × 0.3 km × 9 = 0.81 km²) are required (Verpoorter et al., 2014). Furthermore, small bays, lagoons, and estuaries, where water quality can vary on a spatial scale of tens of metres, can be particularly challenging to observe adequately with these sensors. Given the limitations of using medium-resolution satellite data for water quality monitoring in small inland and coastal water bodies, it is imperative to explore solutions using higher spatial resolution satellite data. The MultiSpectral Instrument (MSI) onboard Sentinel-2 has 13 spectral bands with high spatial resolution of up to 10 m. The constellation of two satellites (Sentinel-2A and 2B) has shorted the revisit period to five days at the equator (Drusch et al., 2012). The high spatial and temporal resolution of MSI makes it a suitable candidate for inland and coastal water monitoring (Pahlevan et al., 2017; Warren et al., 2019).

The concentration of total suspended solids (TSS), which influences the water transparency and light availability in the water column (Brown, 1984; McCulloch & Barber, 2007), is a key water quality indicator used in monitoring activities. However, there is limited research on the TSS retrieval capabilities using MSI imagery for inland and coastal waters. Although several empirical methods were developed to retrieve TSS from MSI images (Liu et al., 2017; Li et al., 2019; Ciancia et al., 2020), their applicability to waters with different inherent optical properties (IOPs) is often limited due to the specific conditions for which they were developed. Existing semi-analytical approaches for retrieving TSS from MSI imagery can also be limited by the range of data used to calibrate these models (Nechad et al., 2010; Han et al., 2016). For example, the semi-analytical method developed by Nechad et al. (2010) can be applied to MSI images, but it was developed for turbid waters and is not appropriate for clear waters. Other research includes the use of machine learning (ML) methods to estimate TSS from MSI images (Saberoon et al., 2020; Balasubramanian et al., 2020; Pahlevan et al., 2022), but the generalisation ability of ML methods depends on the dataset used for model training. Considering the bio-optical complexity of inland and coastal waters, it is desirable to use a semi-analytical method which is applicable for clear to extremely turbid water types and does not require recalibration or coefficient tuning.

Recently, Jiang et al. (2021) developed a semi-analytical method that estimates TSS from the particulate backscattering coefficient ($b_{bp}$) at four different bands for clear to extremely turbid waters based on a water type classification. This method was evaluated using a simulated dataset (TSS range 0.01–1100 g/m³ and an in situ dataset collected from global lakes and coastal waters (TSS range 0.09–2627 g/m³), and it outperformed other existing methods (Jiang et al., 2021; Tan et al., 2022). However, applying the approach by Jiang et al. (2021) to MSI imagery presents two main challenges. Firstly, the band at 620 nm, which is required for the water type classification, is not available on the MSI sensor. Secondly, the method was originally designed for MERIS and OLCI sensors, thereby necessitating adaptation of the algorithm to the MSI bands because bandwidths and band centres are different.

Consequently, the objectives of this study are to: (1) develop a semi-analytical method for MSI imagery to accurately estimate TSS across a range of water optical conditions; (2) validate the proposed TSS estimation method using simulated data, in situ data and satellite matchups; and (3) assess the potential of MSI for monitoring TSS in inland and coastal waters.

2. Data acquisition

2.1. In situ data collection

We collected 1265 in situ remote sensing reflectance ($R_s$) and corresponding TSS measurements from 69 lakes in Japan, Indonesia, China, USA, Switzerland, Sweden, UK and Italy, and 11 coastal waters (including rivers) in Japan, Indonesia, Germany, France, Argentina, Belgium, USA and Portugal (Fig. 1). The in situ TSS covers a wide range from 0.1 g/m³ to 1400 g/m³ with a median value of 9.9 g/m³ (Fig. 1a). $R_s$ spectra were measured using either in-water ($N = 478$) or above-water approaches ($N = 767$). Using the in-water method, the upwelling radiance below the water surface ($L_u$) and downwelling irradiance ($E_d$) were measured with a pair of intercalibrated miniature fibre optic spectrometers. Water-leaving radiance ($L_w$) was obtained by correcting for the air–water interface effects assuming a constant upward Fresnel transmittance of the air–water interface of ~0.975 (Mueller et al., 2003), and a water temperature and wavelength specific refractive index of water (Quan and Fry, 1995), and $R_s$ was calculated as $L_w/E_d$ (Gurlin et al., 2011). In the above-water approach, the total radiance from the water surface ($L_s$), sky radiance ($L_d$) and $E_d$ were measured, and $R_s$ was calculated as $(L_s - L_d)/E_d$, where $\rho$ is the water surface reflectance factor (Mobley, 1999). In addition, we obtained 20 $R_s$ spectra from airborne imagery collected with the Portable Remote Imaging SpectroMeter (PRISM) at ~6 km altitude (Fichot et al., 2016). Finally, the residual reflected skylight effects were removed from all above-water measured $R_s$ using the method proposed from Jiang et al. (2020). All in situ $R_s$ were convolved to Sentinel-2 MSI bands using the MSI spectral response functions. These 1265 in situ $R_s$-TSS pairs were used to develop the model for estimating $R_s$ at 620 nm, and validate the proposed TSS method.

We also used monthly in situ TSS data from seven stations at Lake Kasumigaura (Fig. 1b), which is a turbid shallow lake with an average depth of 4 m and a surface area of 171 km² (Oyama et al., 2009), representing the period of 2015–2020 to evaluate the TSS time-series estimated from satellite images. Those in situ TSS data were collected from the National Institute for Environmental Studies, Japan (NIES, 2020). In addition, typhoon information including location and time, meteorological data including wind speed and precipitation at the Tsuichiura meteorological station (nearshore of Lake Kasumigaura) were also collected from the Japan Meteorological Agency (JMA, https://www.jma.go.jp) and used to study the causes of high TSS events observed in Lake Kasumigaura.

2.2. Synthetic data generation

Two synthetic datasets were used in this study. Synthetic Dataset I includes 1,711,875 TSS and TSS-specific particulate backscattering coefficient ($b_{bp}$) pairs in 1 nm intervals. The simulated Chl-a concentration ranges from 0.01 mg/m³ to 1000 mg/m³, and tripton ranges from 0.01 g/m³ to 100 g/m³. Synthetic Dataset I was used to recalibrate the coefficient of $b_{bp}$ for MSI bands. Synthetic Dataset II includes 1000 $R_s$-TSS pairs with the TSS ranging from 0.01 g/m³ to 1100 g/m³, which were simulated based on a bio-optical model. Synthetic Dataset II was used to validate the developed TSS method. Details describing the equations and parameters for the two synthetic dataset simulations can be found in Jiang et al. (2021); Synthetic Dataset I and III in that work).

2.3. Satellite data acquisition and processing

We downloaded 17 Sentinel-2 MSI Level-1C satellite images over lakes Kasumigaura and Hibara in Japan, Lake Poygan and the Plum Island Estuary in the USA, Loch Lomond in the UK, Lake Garda in Italy, and the Tagus Estuary in Portugal from USGS (https://earthexplorer.usgs.gov). These satellite images were used to validate the TSS
estimation method for satellite matchups (Table 1).

We also downloaded 314 Level-1C MSI images acquired over Lake Kasumigaura from 2015 to 2020 to produce a MSI-based TSS time-series derived with the TSS method proposed in this study. In addition, we downloaded 674 Sentinel-3 OLCI Level-1 images acquired over Lake Kasumigaura from 2016 to 2020 to produce an OLCI-based TSS time-series using the method of Jiang et al. (2021). The two time-series datasets were used to explore the consistency of TSS monitoring between MSI and OLCI. One MSI and one OLCI image acquired over the Tagus Estuary on 19 October 2021 were also included in this study to demonstrate the differences in TSS monitoring with the different spatial resolutions between OLCI and MSI.

The Case 2 Regional Coast Colour (C2RCC) processor in the Sentinel Application Platform (SNAP) version 8.0 was used for atmospheric correction of MSI and OLCI Level-1 products. Clouds and cloud shadows were identified and removed using the IdePix module in SNAP. All MSI images in this study were resampled at a 20 m spatial resolution. The average TSS in a 3 × 3-pixel window was extracted and compared with in situ TSS, and produced the TSS time-series. Satellite matchups were defined as that in situ data collected within one hour of satellite overpass. In total, we obtained 40 MSI matchups (Table 1), which were then used for the proposed TSS estimation method validation.

3. Algorithm development

3.1. TSS estimation algorithm

TSS can be estimated from the particulate backscattering coefficient and TSS-specific particulate backscattering coefficient following the equation by Nechad et al. (2010) and Jiang et al. (2021):

\[
TSS = \frac{1}{b_{bp}(\lambda)} b_{bp}(\lambda)
\]  

(1)

where \(b_{bp}\) can be obtained from simulations, \(b_{bp}\) can be estimated from \(R_{a}\), and \(\lambda\) denotes the wavelength used for TSS estimation. The response of \(R_{a}\) to changes in TSS varies across wavelengths depending on the water turbidity. For example, \(R_{a}\) at short wavelengths (e.g., blue, green) are sensitive to TSS variations in clear waters, but they may become saturated in extremely turbid waters. In these turbid waters, \(R_{a}\) at a longer wavelength (e.g., in the red or near-infrared (NIR)) is more sensitive to changes in TSS than at shorter wavelengths (Knaeps et al., 2015; Novoa et al., 2017). This characteristic suggests that accurate estimation of TSS requires the use of an appropriate reference band that is sensitive to TSS changes and necessitates employing different wavelengths for different types of water.

\(b_{bp}\) can be calculated using the quasi-analytical algorithm (QAA; Lee et al., 2002) as follows:

\[
r_{a}(\lambda) = \frac{R_{a}(\lambda)}{0.52 + 1.7R_{a}(\lambda)}
\]

(2)

\[
\omega(\lambda) = \frac{-0.089 + \sqrt{0.089^2 + 4 \times 0.125 \times r_{a}(\lambda)}}{2 \times 0.125}
\]

(3)

\[
a(\lambda_{0}) = a(\lambda_{0}) + \Delta a(\lambda_{0})
\]

(4)

\[
b_{bp}(\lambda_{0}) = \frac{u(\lambda_{0}) \times a(\lambda_{0})}{1 - u(\lambda_{0})} - b_{bw}(\lambda_{0})
\]

(5)

where \(a(\lambda_{0})\) is the total absorption coefficient at a reference band \(\lambda_{0}\), \(\Delta a(\lambda_{0})\) is the absorption coefficient contributed by optically active components at the reference band, \(b_{bw}(\lambda_{0})\) is the backscattering coefficient at the reference band and finally used for TSS estimation. \(a_{bw}\) is the absorption coefficient of pure water (Kou et al., 1993; Pope and Fry, 1993).
extremely turbid water (water type IV) by comparing classified into four types (Fig. 2): clear water (water type I), moderately turbid water (water type II), highly turbid water (water type III) and extremely turbid water (water type IV) by comparing \( R_{rs}(620) \) at 490 nm, 560 nm, 620 nm and 740 nm (Jiang et al. 2021).

For water type I, the band at 560 nm can be chosen as the reference band, and the absorption coefficient at 560 nm can be estimated using (Lee et al., 2009):

\[
a(560) = a_w(560) + 10^{-1.146 - 1.3665 - 0.4690a_w^2}, \quad (6)
\]

\[
x = \log\left( \frac{R_{rs}(490) + R_{rs}(443)}{R_{rs}(560) + 5 + \frac{R_{rs}(665)}{R_{rs}(665)}} \right), \quad (7)
\]

For water type II, the band at 665 nm can be chosen as the reference band, and the absorption coefficient at 665 nm can be estimated through (IOCCG, 2014):

\[
a(665) = a_w(665) + 0.39 \left( \frac{R_{rs}(665)}{R_{rs}(490) + R_{rs}(443)} \right)^{1.14}, \quad (8)
\]

For water type III, the band at 740 nm can be chosen as the reference band, because \( a_w \) at 740 nm is high (2.7 m\(^{-1}\), Kou et al., 1993) and it is assumed that:

\[
a(740) \approx a_w(740) \quad (9)
\]

For water type IV, the band at 865 nm can be chosen as the reference band, because \( a_w \) at 865 nm reaches 4.6 m\(^{-1}\) (Kou et al., 1993), thus we can assume that:

\[
a(865) \approx a_w(865) \quad (10)
\]

However, two problems emerge when attempting to apply this TSS retrieval approach to MSI: first, \( R_{rs}(620) \) at 620 nm is necessary for water type classification (Fig. 2), but is not available from MSI; second, because the band centres and widths are different between MSI and MERIS (and OLCI), it is necessary to recalibrate the coefficient of \( b_{bp}^* \) for use with MSI. We therefore propose a model to estimate \( R_{rs}(620) \), and recalibrate \( b_{bp}^* \) for MSI in this study.

### 3.2. Algorithm and parameter re-tuning for TSS estimation from MSI

We chose \( R_{rs}(665) \) to estimate \( R_{rs}(620) \) in this study, because it is the closest band on MSI. We built an empirical relationship to estimate \( R_{rs}(620) \) from \( R_{rs}(665) \) using the in situ Dataset (\( N = 1265, \) Fig. 3). When \( R_{rs}(665) \) has values between 0 and 0.02 sr\(^{-1}\), \( R_{rs}(665) \) is generally lower than \( R_{rs}(620) \). When \( R_{rs}(665) \) spans between 0.02 and 0.04 sr\(^{-1}\), \( R_{rs}(665) \) is generally similar to \( R_{rs}(620) \). When \( R_{rs}(665) \) is higher than ~0.04 sr\(^{-1}\), \( R_{rs}(665) \) is generally higher than \( R_{rs}(620) \). This characteristic indicates that for clearer waters, \( R_{rs} \) decreases from short to longer wavelengths, and when water is extremely turbid, \( R_{rs} \) at long wavelengths (such as red and NIR) will be higher than at short wavelengths because of high suspended solids or phytoplankton. Therefore, to model the relationship between \( R_{rs}(620) \) and \( R_{rs}(665) \), we fitted a third-order polynomial to the data and derived the following equation:

\[
R_{rs}(620) = 169.385 R_{rs}(665)^3 - 15.576 R_{rs}(665)^2 + 1.317 R_{rs}(665) + 0.000148 \quad (11)
\]

We convoluted the original simulated 1 nm \( b_{bp}^* \) data (Synthetic Dataset I, \( N = 1,171,875 \)) using the MSI spectral response functions to optimise the \( b_{bp}^* \) for MSI. The median 1/\( b_{bp}^* \) values at MSI bands shown in Table 2 were finally used to estimate TSS from MSI.

To summarise, the TSS estimation method proposed in this study for MSI includes four main steps: (1) estimate \( R_{rs}(620) \) from \( R_{rs}(665) \) using Eq. (11); (2) classify water types as shown in Fig. 2; (3) estimate \( b_{bp}^* \) at

![Fig. 2. Flow chart of water type classification for TSS estimation. An example spectral shape is displayed for each water type, where black dots represent the Sentinel-2 MSI bands.](image-url)
the reference band (λ₀) according to water types (Eqs. (2)–(10)); and (4) estimate TSS using Eq.1, where \( b^*_{bp} \) is taken from Table 2. The source code of the proposed TSS estimation method is available via https://github.com/DalinJiang/TSS.

### 3.3. Accuracy assessment

We used the root mean square error (RMSE), the median absolute percentage error (MAPE), Bias, and the slope of regression analysis (in log scale) to evaluate the TSS estimation results. The use of log scale is because of the log distribution of TSS data in this study (Fig. 1a).

\[
\text{RMSE} = \sqrt{\frac{\sum_{i=1}^{N} [\log_{10}(X_{\text{estimated},i}) - \log_{10}(X_{\text{measured},i})]^2}{N}}
\]  \hspace{1cm} (12)

\[
\text{MAPE} = \text{median}\left(\frac{|X_{\text{estimated},i} - X_{\text{measured},i}|}{X_{\text{measured},i}} \cdot 100\%\right)
\]  \hspace{1cm} (13)

We compared our proposed TSS estimation method with three recently published methods: the semi-analytical algorithm from Nechad et al. (2010), the SOLID method from Balasubramanian et al. (2020), and the MDN method from Pahlevan et al. (2022). The semi-analytical algorithm from Nechad et al. (2010) was developed for turbid waters. This algorithm uses a single band (changeable from visible to NIR bands) for TSS estimation and can be applied to different sensors. We convolved the model coefficients (\( A^\rho, B^\rho \) and \( C^\rho \)) to MSI bands using MSI spectral response functions based on the hyperspectral values provided in that publication, and then tested the performance of using 665 nm, 704 nm, 740 nm, 783 nm and 865 nm for TSS estimation. Finally, we used 740 nm-estimated TSS for comparison in this study as this band showed the best performance. SOLID is a method for estimating TSS based on \( b_{bp} \), where \( b_{bp} \) is estimated from a semi-analytical algorithm (QAA), machine-learning and empirical models according to water type classification (Balasubramanian et al., 2020). MDN is a machine-learning method, which is trained using a large number of in situ data collected from global inland and coastal waters, and can retrieve Chl-a, TSS and coloured dissolved organic matter (CDOM) simultaneously (Pahlevan et al., 2022). For SOLID and MDN methods, we directly used the code provided in these publications without any re-calibrating or re-training.

### Table 2

Median 1/\( b^*_{bp} \) values at MSI bands convolved from Synthetic Dataset I.

<table>
<thead>
<tr>
<th>Band (nm)</th>
<th>1/( b^*_{bp} ) (g/m²)</th>
<th>Band (nm)</th>
<th>1/( b^*_{bp} ) (g/m²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>443</td>
<td>61.875</td>
<td>490</td>
<td>75.352</td>
</tr>
<tr>
<td>490</td>
<td>75.352</td>
<td>560</td>
<td>94.488</td>
</tr>
<tr>
<td>560</td>
<td>94.488</td>
<td>665</td>
<td>113.875</td>
</tr>
</tbody>
</table>

Fig. 4. Validation of the proposed TSS estimation method and comparison with methods from (a) Nechad et al. (2010), (b) SOLID, (c) MDN by using Synthetic Dataset II.
4. Results

4.1. Evaluation of TSS estimation methods using synthetic data

Results using Synthetic Dataset II demonstrate that our proposed method can accurately estimate TSS concentration in clear to extremely turbid waters (Fig. 4d) with a MAPE of 14.88%. The algorithm slightly underestimated TSS concentration in extremely turbid waters (water type IV) and extremely clear waters (TSS < ~0.03 g/m$^3$) with an overall bias of ~0.17. The water type classification sharply separated the four water types showing each in a different TSS range, approximately: clear waters (<1 g/m$^3$), moderately turbid waters (1–10 g/m$^3$), highly turbid waters (10–100 g/m$^3$), and extremely turbid waters (>100 g/m$^3$). Results from the use of Nechad et al. (2010) show good estimates in turbid waters when TSS > 2 g/m$^3$ but overestimations in clear waters when TSS < 2 g/m$^3$ (Fig. 4a). SOLID obtained good estimates in most of the waters but some uncertainties were observed in highly and extremely turbid waters, and nine negative estimates were also found in the results (Fig. 4b). Results from MDN show some overestimations in clear waters and underestimations in turbid waters (Fig. 4c).

4.2. Evaluation of TSS estimation methods using in situ data

For the in situ Dataset, the proposed method performs well for all four water types (Fig. 5d), with a MAPE of 31.50%, and no apparent over- or underestimations (Bias = 0.02). The in situ data were not as evenly distributed among the four water types as the data in Synthetic Dataset II (Fig. 4d), with more than half of the data (59%) classified into water type III, 24% and 10% classified into water types II and IV, and only 7% belonging to water type I. The classification of the in situ data into water types did not separate them as clearly as for Synthetic Dataset II. In particular, water types II and III have some overlaps. Similar to the results using Synthetic Dataset II, the estimated TSS using the methods from Nechad et al. (2010) and MDN show overestimations in clear waters when in situ TSS < 2 g/m$^3$ (Fig. 5a, 5c). The estimated TSS using SOLID shows some uncertainties in highly and extremely turbid waters, and 24 negative estimates were obtained (Fig. 5b). It should be noted that about half of the in situ data in this study were used in MDN training.

4.3. Evaluation of TSS estimation methods using satellite matchups

Using the 40 matchups collected within one hour of MSI overpasses, our proposed method shows an overall good estimation (Fig. 6d). Although the MAPE (41.69%) is higher than the results from MDN (26.92%), it shows a better slope and RMSE than all other three methods. The estimated TSS using our proposed method align with the 1:1 line in the graph, while Nechad et al. (2010) and MDN generated overestimations in clear waters (Fig. 6a, 6c), and SOLID generated underestimations in turbid waters and three negative estimates (Fig. 6b). Those are generally the same phenomena as found using Synthetic Dataset II (Fig. 4) and the in situ Dataset (Fig. 5). For our proposed method, some largely scattered values were also observed for the estimated TSS in the Plum Island Estuary (blue points in Fig. 6d), and some underestimated TSS for the data from Lake Hibara. These inaccuracies of estimated TSS are possibly caused by the atmospheric correction for MSI images, which resulted in different spectral shapes and/or magnitudes compared to the in situ spectra (see discussion for more details).

Fig. 5. Validation of the proposed TSS estimation method and comparison with methods from (a) Nechad et al. (2010), (b) SOLID, (c) MDN by using the in situ Dataset.
4.4. Advantages of MSI for monitoring TSS in inland and coastal waters

4.4.1. Coastal waters

Application of the proposed TSS method to OLCI and MSI images from 19 October 2021 in the Tagus Estuary (Portugal) shows very similar spatial distributions of TSS, i.e., high TSS in the north because of the Tagus River inflow, medium TSS in the centre, and low TSS in the south because of the ocean connection (Fig. 7c, 7d). TSS values retrieved from OLCI and MSI agree with each other across most of the estuary, but TSS values obtained from OLCI are higher than those obtained from MSI in coastal areas (in the east of the estuary). Possible causes are the overpass difference of ~50 min between OLCI and MSI, the lower tide when OLCI overpassed the estuary, which may have led to more sediment resuspension or bottom reflection. Another reason may be the spatial resolution difference between OLCI and MSI (see discussion for more details).

Compared with OLCI, MSI provides more details of TSS spatial variations. For example, TSS is very high in the Tagus River channel, and decreases when reaching the river mouth. This TSS gradient is clearly shown in the MSI-based map (Fig. 7d), but less clearly displayed in the OLCI-based one (Fig. 7c). Another interesting example is the influence of the bridge in the Tagus Estuary, which may have led to more sediment resuspension. The bridge can clearly be seen on the MSI image, but it does not appear on the OLCI one.

Examining Fig. 7f, we can observe that the spatial pattern of TSS in the MSI image reveals clear strips after the bridge, particularly in the south-eastern part of the estuary as indicated by the black circle. These TSS strips are caused by the sediment resuspension generated by tidal currents in the piers supporting the bridge, as shown in Fig. 7g. However, this influence on the TSS pattern is not observable in the OLCI image (Fig. 7e).

Station 1 (St.1) to Station 5 (St.5) (white points in Fig. 7e, 7f) represent in situ sampling locations visited on the day of satellite overpass in the Tagus Estuary. Fig. 8 shows the transect of TSS across the five in situ sampling stations in the Tagus Estuary (white lines in Fig. 7e, 7f). Several interesting observations can be made. Firstly, TSS retrievals from MSI generally agreed with those from OLCI, i.e., TSS is higher close to shore and lower in offshore waters, while some disagreements between the data from the two sensors were observed at both ends of the transect (close to St.1 and St.5). Secondly, the transect of TSS from the MSI image reveals larger and more subtle variations offering detailed information about TSS across the estuary. For instance, the TSS levels between Station 3 (St.3) and Station 4 (St.4) as highlighted by the black box in Fig. 8, correspond to the influence by the bridge as marked by the black circle in Fig. 7f. Thirdly, the TSS values retrieved from OLCI and MSI are very close to in situ TSS at St.3 and St.4, but biases were observed for the other three stations. There could be because in situ TSS at St.3 and St.4 were collected at a time closer to the satellite overpass (~2h) than at the other stations. Lastly, in situ TSS values are generally closer to MSI-derived TSS than OLCI-derived TSS for all five stations.
Fig. 7. TSS spatial distribution in the Tagus Estuary on 19 October 2021. (a) OLCI false colour image acquired at 10:41 UTC on 19 October 2021. (b) MSI false colour image acquired at 11:33 UTC on 19 October 2021. (c) TSS estimated from OLCI. (d) TSS estimated from MSI. (e)-(f) TSS maps of subareas of B1 and b1, where white dots are in situ sampling stations visited on the day of satellite overpass. (g) Photo of the Vasco da Gama bridge over the Tagus Estuary taken on 19 October 2021 during the CERTO (Copernicus Evolution: Research for harmonised Transitional water Observation) campaign.
By examining Fig. 9 j, we can clearly see the extremely high TSS in the
these features are not observable using OLCI, as shown in Fig. 9 g. However,
Warada River mouth in the MSI image, as well as the river plume (and/
water area, but its variations can be clearly observed from MSI (Fig. 9 i). In the Koise River mouth, TSS showed in the MSI-based map (Fig. 9 h), but this change in TSS cannot be
found in the OLCI-based map (Fig. 9 e). In the Sakura River mouth, the change of TSS from the river channel to the lake is clearly
expectedly higher than in other parts of the lake. In the Sakura River
mouth, the change of TSS from the river channel to the lake is clearly
shows similar TSS values and spatial distributions with low TSS in the
northeast and centre of the lake, and high TSS in the north, west
and south of the lake (Fig. 9 c, d). Compared to OLCI, MSI provides a more
detailed spatial distribution of TSS. For example, the TSS eddies in the
centre of the lake (Fig. 9 d) and the south-eastern lake (Fig. 9 i) were
clearly observed from MSI but not through OLCI.

One of the most important advantages of MSI over OLCI is the provision of a detailed TSS distribution map for nearshore waters (e.g., river
mouths), which are more influenced by the proximity to land compared to the lake centre, and are essential habitats for aquatic macrophytes and
animals. A1, A2 and A3 in Fig. 9 c (OLCI) cover the same area as a1, a2
and a3 in Fig. 9 d (MSI), and are adjacent to three river mouths (Sakura River, Koise River and Shintone River) in Lake Kasumigaura. Due to the heavy precipitation three days before the satellite overpass, a stream of particles entered the lake from rivers together with sediment resus-
pension in shallow river mouths. TSS in the vicinity of the river mouths is expectedly higher than in other parts of the lake. In the Sakura River
mouth, the change of TSS from the river channel to the lake is clearly
shown in the MSI-based map (Fig. 9 h), but this change in TSS cannot be
observed in the OLCI-based map (Fig. 9 e). In the Koise River mouth, TSS distribution can be hardly seen from OLCI (Fig. 9 f) because of the small
water area, but its variations can be clearly observed from MSI (Fig. 9 i). By examining Fig. 9 j, we can clearly see the extremely high TSS in the
Shintone River mouth in the MSI image, as well as the river plume (and/
resuspension) along the south coast of the lake. However, these features are not observable using OLCI, as shown in Fig. 9 g.

### 4.4.2. Inland waters

Fig. 9 shows the TSS maps from OLCI and MSI on 2 February 2020 in Lake Kasumigaura, Japan, just after a heavy precipitation event (35
mm/day and maximum wind speed of 6.1 m/s on 28–29 January 2020). Although the time difference between OLCI and MSI overpasses is ~50
min, they show similar TSS values and spatial distributions with low TSS in the northeast and centre of the lake, and high TSS in the north, west
and south of the lake (Fig. 9 c, d). Compared to OLCI, MSI provides a more
detailed spatial distribution of TSS. For example, the TSS eddies in the
centre of the lake (Fig. 9 d) and the south-eastern lake (Fig. 9 i) were
clearly observed from MSI but not through OLCI.

The use of \( R_{620} \) for water type classification is necessary. We tested the use of \( R_{665}(665) \) instead of \( R_{620}(620) \) for water type classification,
but misclassifications of water type and clear underestimations of TSS were found for waters at the boundary between water types II and III and
in situ data. We empirically constructed a model for estimating \( R_{620}(620) \) based on \( R_{620}(620) \) in situ spectra, where although a good non-
linear relationship between \( R_{620}(620) \) and \( R_{665}(665) \) was obtained (Fig. 3),
some uncertainties in the estimated \( R_{620}(620) \) are inevitable. However, the estimated \( R_{620}(620) \) is only used to distinguish water types II and III (Fig. 2), and is not used in TSS estimation. Therefore, its accuracy only
influences the distinction of those waters which are close to the
boundary between water types II and III. As such waters share similar
turbidity levels, misclassification of water type due to errors in estimated
\( R_{620}(620) \) is not likely to significantly influence TSS estimation. For example, when we added ±15 % errors to the estimated \( R_{620}(620) \) in Synthetic Dataset II, the results of estimated TSS showed very similar
accuracy (RMSE = 0.11) to the results in Fig. 4d (RMSE = 0.10). In addition, for those waters which are close to the boundary between water types II and III, estimating TSS using either 665 nm or 740 nm will provide similar results. For example, for the data for which the difference between \( R_{620}(490) \) and \( R_{620}(620) \) was less than \(-0.002 \text{ sr}^{-1} \) in Synthetic Dataset II (N = 152), the difference between TSS estimated using 665 nm and 740 nm was 5.7 %.
Fig. 9. TSS spatial distribution across Lake Kasumigaura on 2 February 2020, just after a heavy precipitation event on 28–29 January 2020. (a) OLCI false colour image acquired at 00:39 UTC on 2 February 2020. (b) MSI false colour image acquired at 01:28 UTC on 2 February 2020. (c) TSS map from OLCI. (d) TSS map from MSI. (e)-(g) TSS in the Sakura, Koise and Shintone River mouths from OLCI. (h)-(j) TSS in the Sakura, Koise and Shintone River mouths from MSI.
Fig. 10. Long-term TSS during 2015–2020 for Lake Kasumigaura in Japan. Blue dots are in situ TSS, green dots are estimated TSS from OLCI images, red dots are estimated TSS from MSI images. Black dots on the map are the locations of monitoring stations in Lake Kasumigaura as in Fig. 1b.

Fig. 11. Comparison of validations using matchups from (a) MSI and (b) OLCI in Lake Kasumigaura, where matchups are in situ data collected on the same day of MSI or OLCI overpasses. Blue dots represent matchups that are from the same station and the same day for MSI and OLCI (where ‘MSI-OLCI matched’ shows ‘yes’, N = 13).
To test the uncertainty of TSS estimation at water type boundaries, we compared TSS estimated from $R_{rs}$ at two different reference bands corresponding to two neighbouring water types (e.g., 560 nm and 665 nm for water types I and II). Highly consistent TSS estimates at all three water type boundaries indicate that the proposed method can estimate TSS seamlessly between different water types (Fig. 13). However, we observed an inconsistency of TSS estimates between using 665 nm and 740 nm as reference bands for waters at the boundary between water types II and III when $|R_{rs}(490) - R_{rs}(620)| > 0.002$ sr$^{-1}$ (Fig. 13b, c). That means inaccurate atmospheric correction or $R_{rs}(620)$ estimation may lead to misclassification of water type, and finally cause uncertainties of TSS estimation, but only when the error of the relative

Fig. 12. (a) Typhoons passing over Lake Kasumigaura, where the size of the blue dots indicates the relative magnitude of the typhoon, and the y-axis indicates the distance between typhoon and lake centre while passing. (b)–(c) Precipitation and maximum wind speed at Tsuchiura meteorological station, which is at the nearshore of Lake Kasumigaura. (d) Average in situ, OLCI estimated and MSI-estimated TSS at the seven monitoring stations in Lake Kasumigaura.

Fig. 13. Comparison of estimated TSS between using two reference bands corresponding to two neighbouring water types for waters at water type boundaries. A water type boundary was defined as having an absolute $R_{rs}$ difference between the two wave bands used for water type classification smaller than 0.005 sr$^{-1}$. (a)-(c) are results from Synthetic Dataset II, (d)-(f) are results from in situ Dataset. Colour indicates the $R_{rs}$ difference between the two wave bands used for water type classification.
The $b_{bp}$ values were re-calibrated to optimise them for MSI (Table 2), although we didn’t find significant improvements in TSS estimation for the data used in this study by using the re-calibrated $b_{bp}$ rather than the $b_{bp}$ for MERIS and OLCI in Jiang et al. (2021). It was nonetheless necessary to do, because the difference of bandwidths and band centres between MSI and the other sensors (e.g., the large difference of the 740 nm band for MSI and 754 nm band for OLCI (MERIS) used in the TSS estimation for water type III) may lead to errors in TSS estimation (Cao et al., 2019; Ford & Vodacek, 2020). Following the same approach as in Jiang et al. (2021), we used the median $b_{bp}$ values for simulations for TSS estimation from MSI. There might have been some instances where $b_{bp}$ are different from our simulated values or $b_{bp}$ doesn’t follow a power function (Binding et al., 2019; Xu et al., 2021), such as the one we adopted in our simulations, and users are encouraged to replace the median $b_{bp}$ with more realistic or in situ measured values where available to improve the TSS estimation accuracy.

The semi-analytical method proposed in this study improved TSS estimation compared to the other existing methods (Figs. 4, 5, 6), with more accurate estimates in clear waters compared to the semi-analytical method from Nechad et al. (2010) and MDN as well as more accurate and valid estimates compared to SOLID. These improvements make the proposed method applicable from clear to extremely turbid waters with less uncertainties and benefit the water quality monitoring of inland and coastal waters as these waters cover a wide range of turbidity levels. The proposed method can also increase the confidence when estimating TSS for a water body without prior knowledge of turbidity levels. Some underestimations, especially for extremely turbid waters, were observed for the proposed method (Fig. 4d), because $a$ might be higher than $a_w$ due to high turbidity, but we assumed $a \approx a_w$. Further studies are needed to address this problem. It should also be emphasised that the accuracy of the proposed method will highly depend on the accuracy of the $R_a$ magnitude of the reference band used for TSS estimation (Jiang et al., 2020; Jiang et al., 2021). Our test using seven MSI matchups in Lake Kasumigaura revealed that the error of estimated $b_{bp}$ has a very high correlation with the error of $R_a$ (Fig. 14). This necessitates an accurate measurement of in situ $R_a$ or atmospheric correction of the satellite images when using our proposed method.

5.2. Advantages of MSI in TSS monitoring

MSI has clear advantages in TSS monitoring over ocean colour sensors (e.g., MERIS and OLCI), because of its high spatial resolution, which can make small water bodies observable and provide more details of TSS spatial distributions. The use of MSI and the method proposed in this study can expand TSS monitoring to water bodies with a minimum observable area of $\sim 0.0036 \text{ km}^2$ [$0.02 \text{ km} \times 0.02 \text{ km} = 0.0036 \text{ km}^2$ accounting for 20 m $\times$ 20 m spatial resolution and at least 9 pixels for a water body]. This will make at least $\sim 2.3 \times 10^7$ more lakes, i.e., $\sim 20 \%$ of the global lakes with an area between 0.01 and 0.1 km$^2$ (Verpoorter et al., 2014) observable compared to using OLCI images (considering a minimum observable area of more than 0.1 km$^2$ for OLCI). In addition to small lakes, TSS monitoring with MSI can expand to small bays, estuaries, rivers and lagoons where ocean colour sensors are not applicable, or can provide more details of TSS spatial variations where such sensors cannot. The examples in Figs. 7 and 9 in this study clearly show the advantage of TSS mapping using MSI for rivers, river mouths, and nearshore waters and detecting those detailed spatial variations near bridges, which are not observable in OLCI images. It is well known that the above-mentioned inland and coastal waters are closely linked to human activities (Kummu et al., 2011; Small & Nicholls, 2003) and TSS observations from MSI can provide valuable supporting information for environmental management and decision-making for those water bodies.

We found that the MSI image-derived TSS are closer to in situ TSS when compared to OLCI image-derived TSS although both of them agree well with in situ TSS (Figs. 8, 11). For Synthetic Dataset II and in situ spectra, we also found the estimated TSS using MSI bands showed higher accuracies than the ones using OLCI bands for water types I and II. The reasons why MSI-derived TSS are closer to in situ TSS than OLCI-derived TSS may include: (1) the spectral resolution (band width) effect, which influences the sensitivity of sensors in detecting TSS (Cao et al., 2019; Ford & Vodacek, 2020). MSI has wider bands, which will result in higher $R_a$ compared to OLCI when convolving 1 nm spectra to its bands, where the higher $R_a$ will compensate underestimations from the assumption of $a \approx a_w$ in our proposed method, which is more influential for water type II than the other three water types. For example, the average $R_a$ (665 nm) of water type II of the in situ Dataset ($N = 301$) is 0.00260 sr$^{-1}$ for MSI, which is higher than that for OLCI (0.00246 sr$^{-1}$); (2) the spatial resolution effect, which influences the estimated TSS particularly in non-uniformly spaced TSS data (Fearns, 2017; Fisher et al., 2018). MSI has higher spatial resolution, so the average TSS within 3 $\times$ 3 MSI pixels covering a smaller area (0.0036 km$^2$) is closer to in situ TSS than that within 3 $\times$ 3 OLCI pixels covering a wider area (0.81 km$^2$). Fig. 15 shows an example of estimated TSS in the 900 m $\times$ 900 m area surrounding St.1 in the Tagus Estuary (Fig. 7) and from both the OLCI image (Fig. 15a) and MSI image (Fig. 15b), it can be seen that the MSI-estimated TSS has more spatial variations compared to OLCI-estimated TSS in the same area. Moreover, near St.1 there is a channel with lower TSS (blue pixels in Fig. 15b) than to the northwest and southeast (green to yellow pixels in Fig. 15b). This spatial variation can be observed from MSI but not from OLCI. Therefore, when extracting TSS from a 3 $\times$ 3-pixel window for validation, the estimated TSS from MSI is closer to in situ TSS than that from OLCI for this station (Fig. 8). This confirms that the influence of spatial resolution cannot be ignored as it may lead to uncertainties when using satellite-derived $R_a$ and in situ collected TSS as input for empirical model calibration or machine learning model training, because they are not corresponding to each other, especially for coarse spatial resolution images.

Although some slight differences were observed between MSI-derived and OLCI-derived TSS, the results in this study showed that these sensors can provide overall consistent TSS time-series (Fig. 10) and TSS spatial distributions on the same overpass dates (Figs. 7, 8, 9). This indicates that OLCI and MSI can be used collaboratively for TSS monitoring in inland and coastal waters, where OLCI can provide high

![Fig. 14.](image-url) Relationship between $R_a$ error and estimated TSS error for seven MSI matchups obtained on 27 October and 29 November 2016 in Lake Kasumigaura, Japan. X-axis is the difference between C2RCC-derived $R_a$ and in situ $R_a$. Y-axis is the difference between estimated TSS using C2RCC-derived $R_a$ and in situ TSS.
monitoring frequency and MSI can provide high spatial resolution, which can enhance the ability of TSS monitoring from satellite images and provide more potential for water pollution or extreme event monitoring. In the example of Lake Kasumigaura, OLCI can monitor high TSS events because of heavy precipitation and/or sediment resuspension (Fig. 12), and MSI can provide more details as to where such high TSS is located (Fig. 9). In addition, as there is a time difference between OLCI and MSI overpasses (e.g., ~50 mins in Figs. 7, 9), these two sensors can be used to monitor TSS changes on the same day in highly dynamic waters.

5.3. Atmospheric correction and satellite matchups

This study used the C2RCC atmospheric correction method, which is based on comparisons of four different atmospheric correction methods, namely ACOLITE (Vanelhellemont, 2019), C2RCC (Brockmann et al., 2016), Polymer (Steinmetz et al., 2011) and Sen2cor (Main-Knorn et al., 2017). In a comparison of satellite-derived $R_\text{rs}$ to in situ $R_\text{rs}$ collected within one hour of satellite overpasses from our studied waters, C2RCC and Polymer showed similar accuracy and better performance than the other two methods (Figure S1 in supplementary). Moreover, C2RCC produced more accurate results than Polymer in retrieving TSS time-series in Lake Kasumigaura (Figure S2 in supplementary) because of its higher accuracy in the NIR bands, which were used for estimating TSS in this lake (mainly 740 nm). However, C2RCC still showed some uncertainties in derived $R_\text{rs}$. For example, the atmospherically corrected spectra showed reflectance peaks at 490 nm in Lake Hihara, which were then classified as water type I. Contrarily, the reflectance peaks from in situ spectra were at 560 nm, which were classified as water type II. This misclassification of water type led to underestimations of TSS (yellow points in Fig. 6d). Some of the spectra from atmospherically corrected MSI images showed similar shapes to in situ spectra from the Plum Island Estuary, but their magnitudes were lower than those of the in situ spectra, which finally led to underestimations of TSS (blue points below 1:1 line in Fig. 6). Some TSS underestimations observed in sites 3 and 4 in Lake Kasumigaura (Fig. 10) are also possible because of underestimated $R_\text{rs}$ from C2RCC. Those uncertainties could constrain the application of the proposed TSS method to MSI images in inland and coastal waters. Because of their small size, adjacency to land and optical complexity (Palmer et al., 2015; Jiang et al., 2023), an atmospheric correction method which can accommodate waters with a wide range of bio-optical properties, different aerosol types and adjacency effects is necessary for inland and coastal water applications. This requires further developments on the atmospheric correction methodology.

Matchups for TSS validation in this study are restricted to within one hour of satellite overpass. This restriction is very important for highly dynamic waters such as estuaries or river mouths, where the bio-optical properties can change within a short period of time due to tides or currents (Eleveld et al., 2014). This is exemplified for the Tagus Estuary shown in Fig. 8, where in situ TSS at St.3 and St.4 were collected within ~23 min and ~66 min difference to the MSI overpass respectively, and agreed with satellite retrievals. However, in situ TSS at St.2 and St.5 were collected 3.4 and 2.1 h after the MSI overpass respectively, when water in the estuary had changed considerably because of tides. Thus, they showed large disagreement with satellite retrievals. Some TSS differences were observed between OLCI and MSI in Fig. 7c and d, and these differences may also be due to the quick change in water conditions. Therefore, it is important to consider the time difference between in situ data collection and satellite overpass when performing satellite product validations, especially for highly dynamic waters.

6. Conclusions

We proposed a semi-analytical method for estimating TSS from Sentinel-2 MSI images in this study with the aim of providing high spatial resolution TSS for inland and coastal waters. Validation and comparison using a simulated dataset, globally collected in situ data and satellite matchups showed that our approach outperformed other existing methods and can be applied from clear to extremely turbid waters resulting in accurate TSS estimation. Results also showed the significant advantages of MSI images in TSS mapping for rivers, river mouths and other nearshore waters. Applying the proposed TSS method for MSI with prior C2RCC atmospheric correction led to reasonable long-term TSS estimates in Lake Kasumigaura, which showed good agreement with in situ and OLCI-derived TSS time-series. Although MSI-derived TSS are closer to in situ TSS than OLCI-derived TSS, both of them agree well with in situ data and can be used collaboratively for TSS monitoring. When it comes to highly dynamic waters, it is essential to restrict the time difference between in situ data collection and satellite overpass for validating satellite products.
Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Appendix A. Supplementary material

Supplementary data to this article can be found online at https://doi.org/10.1016/j.isprsjr.2023.09.020.

References


