

## Fractionation of Ne and Ar isotopes by molecular diffusion in water

Lina Tyroller<sup>a,b,\*</sup>, Matthias S. Brennwald<sup>a</sup>, Lars Mächler<sup>a</sup>, David M. Livingstone<sup>a</sup>, Rolf Kipfer<sup>a,b,c</sup>

<sup>a</sup>*Eawag, Swiss Federal Institute of Aquatic Science and Technology, Dübendorf, Switzerland*

<sup>b</sup>*ETH Zurich, Institute of Biogeochemistry and Pollutant Dynamics, Zürich, Switzerland*

<sup>c</sup>*ETH Zurich, Institute of Geochemistry and Petrology, Zürich, Switzerland*

---

### Abstract

Molecular diffusion in water is a physical transport mechanism that plays an important role in many environmental processes. As the abundances of the chemically inert noble gases and their isotopes are controlled only by physical processes, they are ideal tracers for gas transfer processes in aquatic systems. Molecular diffusion in water is often thought to cause the mass-dependent fractionation of noble gas isotope ratios, e.g.  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$ , under the assumption that the isotopic fractionation of gases in water can be adequately described in terms of a "square root relation", i.e. in terms of the reciprocal of the square root of the ratio of their atomic masses. To quantify reliably the fractionation of  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  we determined the change in the isotope ratios of Ne and Ar after they had diffused through immobilised water. The Ne isotope fractionation factor, expressed as the ratio of the diffusion coefficients of  $^{20}\text{Ne}$  and  $^{22}\text{Ne}$ , was found to be  $D_{^{20}\text{Ne}}/D_{^{22}\text{Ne}} = 1.010 \pm 0.003$ , which is considerably lower than that predicted

---

\*Corresponding author

*Email addresses:* [lina.tyroller@eawag.ch](mailto:lina.tyroller@eawag.ch) (Lina Tyroller), [matthias.brennwald@eawag.ch](mailto:matthias.brennwald@eawag.ch) (Matthias S. Brennwald), [lars.maechler@eawag.ch](mailto:lars.maechler@eawag.ch) (Lars Mächler), [living@eawag.ch](mailto:living@eawag.ch) (David M. Livingstone), [kipfer@eawag.ch](mailto:kipfer@eawag.ch) (Rolf Kipfer)

from the square root relation, but close to results obtained from recent molecular dynamics calculations. In contrast to this, the Ar isotopic fractionation factor was found to be  $D_{^{36}\text{Ar}}/D_{^{40}\text{Ar}} = 1.055 \pm 0.004$ , agreeing with that predicted from the square root relation. Thus, neither the square root relation nor calculations based on molecular dynamics are capable of giving a general explanation of the isotopic fractionation of both Ne and Ar that results when these gases undergo molecular diffusion through water. Our experimental results do not rely on a theoretical model and are considered to provide an accurate and robust quantification of the isotopic fractionation of Ne and Ar isotopes induced by molecular diffusion through water.

*Keywords:* Graham's Law, noble gases, kinetic fractionation, isotope ratio, excess air

---

## 1. Introduction

Noble gases and their isotopes are used as environmental tracers in aquatic systems because of their sensitivity to the transport and exchange of solutes and fluids. Noble-gas concentration patterns in natural water bodies have been successfully used to reconstruct palaeoclimates, to analyse circulation and mixing within water bodies, to quantify water residence times and to study the geochemical origin of fluids injected into water bodies (for reviews see Kipfer et al., 2002; Schlosser and Winckler, 2002; Aeschbach-Hertig and Solomon, 2013; Brennwald et al., 2013)

Molecular diffusion in water is commonly expected to result in the elemental fractionation of noble gases and in the fractionation of the ratios of noble gas

12 isotopes owing to systematic differences in their diffusion coefficients (e.g., Oz-  
13 ima and Podosek, 2002). The fractionation of the isotope ratios of noble gases  
14 dissolved in water (e.g.  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$ ) has been used to assess the im-  
15 portance of molecular diffusion for various environmental processes, such as: (I)  
16 transport in pore water; (II) degassing in supersaturated pore water; and (III) the  
17 dynamics of excess air in groundwater.

18 I. If the transport of noble gases in pore water (e.g. in lake sediments) is  
19 controlled by molecular diffusion, the noble-gas isotope ratios in the pore  
20 water would be expected to be fractionated relative to the noble-gas isotope  
21 ratios found in air-saturated water. If the transport of noble gases in the  
22 sediment is dominated by advection, however, no fractionation would be  
23 expected.

24 II. Bubble formation and degassing generally results when the partial pressure  
25 of dissolved gases in the pore water exceeds the in situ pressure. In envi-  
26 ronmental systems such as lake sediments (Brennwald et al., 2003, 2005,  
27 2013) and groundwater (for a review see Aeschbach-Hertig et al., 2008),  
28 patterns in the concentrations of dissolved noble gases are used to trace the  
29 formation of bubbles generated by biological processes (e.g. the production  
30 of  $\text{CO}_2$  or  $\text{CH}_4$ ). The difference of the partial pressure of the gases in the  
31 bubble and in the surrounding water results in the diffusion of noble gases  
32 from the water into the bubbles. If the bubbles remain in the water until gas  
33 exchange between the bubbles and the surrounding water reaches steady

34 state, the gas partitioning is controlled by the solubilities of the gases. This  
35 results in the elemental fractionation of the noble gases in the surrounding  
36 water, but in virtually no isotopic fractionation. If the bubbles leave the wa-  
37 ter before steady state is attained, the noble-gas isotope ratios are assumed  
38 to be fractionated relative to air-saturated water (Lippmann et al., 2003;  
39 Brennwald et al., 2005; Zhou et al., 2005; Klump et al., 2006; Visser et al.,  
40 2007).

41 III. Excess air results from the entrapment of air bubbles in groundwater. Ow-  
42 ing to the increasing hydrostatic pressure during groundwater recharge, the  
43 entrapped bubbles dissolve, leading to the higher noble-gas concentrations  
44 (relative to air-saturated water) that are characteristic of groundwater. The  
45 formation of excess air has been explained using various different concep-  
46 tual models (for a review see Schlosser and Winckler, 2002; Aeschbach-  
47 Hertig and Solomon, 2013). Molecular diffusion plays a role in models that  
48 describe the partial re-equilibration of excess air in groundwater with the  
49 atmosphere. Part of the excess air diffuses through the groundwater body  
50 and to the soil gas of the unsaturated zone. The isotope ratios  $^{20}\text{Ne}/^{22}\text{Ne}$   
51 and  $^{36}\text{Ar}/^{40}\text{Ar}$  have therefore been suggested as tools to determine which  
52 of the different conceptual models for excess-air formation is likely to be  
53 most correct (Holoher et al., 2002; Kipfer et al., 2002; Peeters et al., 2002;  
54 Aeschbach-Hertig and Solomon, 2013). This is important because these  
55 conceptual models are necessary when using noble-gas concentrations to  
56 reconstruct the environmental conditions that prevailed during groundwater

57 recharge.

58 All the above-mentioned applications of noble-gas isotope ratios in aquatic  
59 systems to interpret noble gas concentration patterns in terms of physical gas  
60 transport processes rely on a parameterisation of the diffusion rates in terms of the  
61 reciprocal of the square root of the atomic mass of the gas. This "square root rela-  
62 tion" is implicitly derived from Graham's Law (Graham, 1833), which describes  
63 the fractionation of two gas species undergoing diffusion in a gaseous matrix for  
64 the case where collisions between different gas molecules are rare and pressure  
65 is constant (Schwarzenbach et al., 2003; Cussler, 2009). Because Graham's Law  
66 and the square root relation derived from it are both ultimately based on kinetic  
67 gas theory (Moore, 1999), they lack the theoretical basis that would allow their  
68 application to the diffusion of solutes through water.

69 The square root relation can be stated in the following form (e.g. Richter et al.,  
70 2006) :

$$\frac{D_i}{D_j} = \sqrt{\frac{M_j}{M_i}} \quad (1)$$

71 where  $D_i$  and  $D_j$  are the diffusion coefficients of the diffusing gases  $i$  and  $j$ , and  
72  $M_i$  and  $M_j$  are their molecular masses. If gas-gas collisions are more frequent,  
73 however, the square root relation is modified by introducing the reduced masses  
74  $\mu_i$  and  $\mu_j$  of the diffusing gases (e.g. Craig and Gordon, 1965; Richter et al., 2006):

$$\frac{D_i}{D_j} = \sqrt{\frac{\mu_j}{\mu_i}} \quad \text{with } \mu_i = \frac{M_i M_{\text{ma}}}{M_i + M_{\text{ma}}} \text{ and } \mu_j = \frac{M_j M_{\text{ma}}}{M_j + M_{\text{ma}}} \quad (2)$$

75 where  $M_{\text{ma}}$  is the molecular mass of the matrix gas through which comparatively  
76 low concentrations of gases  $i$  and  $j$  with molecular masses  $M_i$  and  $M_j$ , respec-  
77 tively, are diffusing.

78 Recent molecular dynamics calculations (Bourg and Sposito, 2008) have chal-  
79 lenged the applicability of the square root relation for characterizing the isotopic  
80 fractionation of dissolved noble-gas isotopes by molecular diffusion in water.  
81 Bourg and Sposito (2008) simulated the diffusion of different noble gases and  
82 their isotopes in water on an atomic scale, predicting their behaviour by assum-  
83 ing theoretical intermolecular potential functions. Their results suggest a more  
84 general power-law form of Eq. 1:

$$\frac{D_i}{D_j} = \left( \frac{M_j}{M_i} \right)^\beta \quad (3)$$

85 in which  $0 < \beta < 0.2$  rather than the expected value of  $\beta = 0.5$ .

86 Experimental data on the fractionation of noble gases by molecular diffusion  
87 in water are scarce. Jähne et al. (1987a) measured the elemental diffusivities of  
88 He, Ne, Kr, Xe and Rn in water and found them to be consistent with the square  
89 root relation (Eq. 1). In their experiments, gas diffuses from a gas-filled chamber  
90 through a diffusion cell containing immobilised water into another chamber. The  
91 advantage of this experimental approach is that the system can be described with  
92 a single diffusion equation (Schwarzenbach et al., 2003; Cussler, 2009) that can  
93 be fitted to the experimental data. However this approach has not yet been used to  
94 determine the fractionation of the isotopes of a single noble-gas species.

95 To date the only experimental data available on the kinetic isotopic fraction-  
96 ation of noble-gas isotopes in water have been based on air/water gas exchange  
97 models, where mass transfer at the gas/water interface is related to diffusion (for a  
98 review see Cussler, 2009). Jähne et al. (1987a) studied gas/water mass transfer in  
99 an evasion experiment with a circular wind-wave facility and concluded that the  
100 isotopic fractionation of He was consistent with the square root relation. A recent  
101 study (Tempest and Emerson, 2013) determined gas/water mass transfer for Ne  
102 and Ar in a system in which the gas headspace was connected to degassed water.  
103 In this experiment, the isotopic fractionation observed was weaker than that pre-  
104 dicted by the square root relation, but similar to that predicted by the molecular  
105 dynamics model of Bourg and Sposito (2008). However, the setup used in these  
106 studies was designed to study the transfer of gases across the thin boundary layers  
107 of the air/water interface in natural surface waters, and this is affected by large  
108 -scale mixing on both sides of the interface (Jähne et al., 1987b). The quantitative  
109 relationship between the gas-exchange rates obtained in such mass-transfer exper-  
110 iments and the diffusion coefficients of the gases involved depends on the choice  
111 of a suitable gas-exchange model (Schwarzenbach et al., 2003; Cussler, 2009).  
112 Combining an empirical gas-exchange model for natural waters with gas-transfer  
113 rates obtained in an artificial laboratory experiment with considerably different  
114 turbulence levels in the boundary layers does not provide a direct measurement of  
115 the isotopic fractionation resulting from molecular diffusion in water.

116 Instead of a "mass transfer approach", in this study a "diffusion approach"  
117 is used in which the diffusive transport of gases through immobilised water can

118 be expressed by a single diffusion equation. To our knowledge this is the first  
119 time that the isotopic fractionation of noble gases has been measured based on  
120 a diffusion approach using an experimental setup similar to the modified Barrer  
121 method used by Jähne et al. (1987a). We determined directly the fractionation  
122 of  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  resulting from molecular diffusion in bulk water and  
123 measured the relative differences of the isotope fluxes through a diffusion column  
124 containing immobilised water. We compare our experimentally measured isotopic  
125 fractionation with the two versions of the square root relation (Eqs. 1, 2) and  
126 molecular dynamics calculations (Eq. 3) to evaluate the applicability of each.

## 127 **2. Material and methods**

### 128 *2.1. Experimental setup*

129 Our setup (Fig. 1) consisted of a diffusion column comprising two gas-filled  
130 chambers, A and B, separated by a diffusion cell. Before the start of the experi-  
131 ment, both chambers were flushed with carrier gas ( $\text{N}_2$  of 99.999% purity, Carba-  
132 gas, Switzerland) to remove residuals of other gases from the apparatus. During  
133 the experiment, chamber A was continuously flushed with one of the test gases  
134 (Ne or Ar of 99.999% purity, Carbagas, Switzerland; gas flow:  $8\text{cm}^3_{\text{STP}}/\text{min}$ ) and  
135 chamber B with the carrier gas ( $\text{N}_2$  gas flow:  $4\text{cm}^3_{\text{STP}}/\text{min}$ ). The difference in the  
136 partial pressure of the test gas between A ( $\sim 1$  atm) and B ( $\sim 0$  atm) meant that  
137 some of the test gas diffused through the diffusion cell from chamber A to cham-  
138 ber B. The test gas reaching chamber B was flushed out together with the carrier  
139 gas. To prevent turbulent transport within the diffusion cell, the water in the diffu-



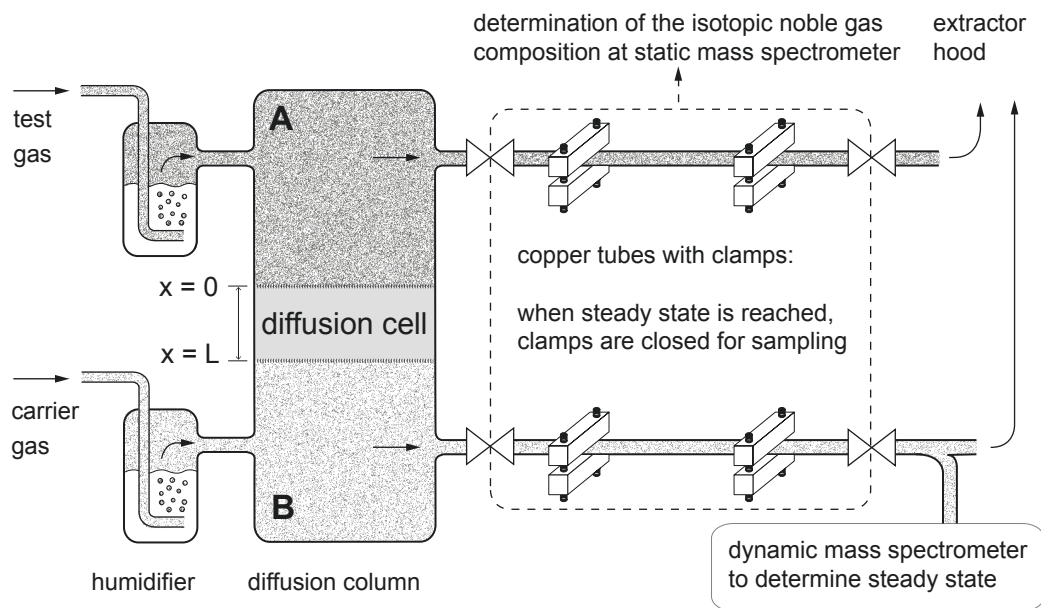


Figure 1: Experimental setup. During the experiment both temperature and pressure were kept constant. A test gas and a carrier gas are flushed continuously through two chambers (A and B, respectively) separated by a diffusion cell containing an agar-water gel. All fittings, valves and connection tubes are gas-tight and made of stainless steel or copper. Desiccation of the agar-water gel in the diffusion cell, which might result in cracks, is prevented by bubbling the gases through pure water in humidifiers to saturate them with water vapour before they are injected into the gas-filled chambers. Bacterial growth in the diffusion cell is inhibited by adding 0.01%  $\text{NaN}_3$  to the gel. The outflowing gases are discharged into an extractor hood. The gas-carrying outlet tubes are always open to ambient air at local atmospheric pressure.

140 sion cell was immobilised by adding 0.5% agar (porosity 99%) as recommended  
 141 by Jähne et al. (1987a). The agar-water gel lay on a glass frit (porosity 42%). Re-  
 142 peated experiments were carried out using different gel thicknesses ( $L = 1.7-2.0$   
 143 cm, see Tab. 1). Turbulent mixing can be assumed to result in homogeneously  
 144 mixed gases in chambers A and B, making additional mechanical homogenisation  
 145 unnecessary.

146 The carrier gas flowing out of chamber B was continuously analysed and mon-

147 itored with a quadrupole mass spectrometer operated in dynamic mode (Mächler  
148 et al., 2012) to assess the performance of the experimental apparatus and to deter-  
149 mine when the gas flux through the diffusion cell had attained steady state. These  
150 measurements were not used to determine the  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  ratios be-  
151 cause of interference resulting from doubly charged ions and matrix effects, which  
152 strongly limits the precision of the noble-gas analysis (see Mächler et al., 2012).  
153 When the continuous measurements indicated that the test-gas flux through the  
154 diffusion cell had attained steady state, samples of the gases flowing out of cham-  
155 bers A and B were taken in copper tubes for isotope-ratio analysis by static mass  
156 spectrometry (Beyerle et al., 2000). In brief, the gas samples were separated into a  
157 He-Ne fraction and an Ar-Kr-Xe fraction using a series of cryogenic traps. These  
158 gas fractions were then purified using additional cryogenic traps, zeolite traps and  
159 getter traps, which removed any reactive gases. The purified noble gases were  
160 then analysed in a custom-built, sector-field mass spectrometer by peak-height  
161 comparison relative to an air standard processed using exactly the same procedure  
162 as that used for the sample gas.

## 163 2.2. *Principles of the measuring method*

164 After switching on the flow of test gas through chamber A, the test gas starts to  
165 diffuse through the diffusion cell. In an initial, non-steady-state phase, the test-gas  
166 flux through the diffusion cell increases until it eventually attains steady state.

167 2.2.1. *Non-steady state*

168 By differentiating Eq. 4.24a of Crank (1975) with respect to time, the time-  
169 dependent diffusive flux  $F_i(t)$  of the test-gas species  $i$  from the diffusion cell into  
170 chamber B can be calculated as follows:

171

$$F_i(t) = \frac{D_i C_i(0)}{L} \left( 1 + 2 \sum_{n=1}^{\infty} (-1)^n \exp\left(-D_i n^2 \pi^2 \frac{t}{L^2}\right) \right) \quad (4)$$

172

173 where  $t$  is time ( $t = 0$  at the start of the experiment, when chamber A is  
174 completely flushed by the flow of test gas);  $D_i$  is the diffusion coefficient of species  
175  $i$  in the diffusion cell; and  $C_i(x)$  is the concentration of species  $i$  in the diffusion  
176 cell at position  $x$  ( $x = 0$  at the top of the diffusion cell and  $x = L$  at the bottom;  
177 see Fig. 1). The assumptions underlying Eq. 4 are that  $C_i(0 \leq x \leq L) = 0$  for  
178  $t < 0$ ; that  $C_i(0) > 0$  and is time-independent for  $t \geq 0$ , and that  $C_i(L) \ll C_i(0)$  for  
179  $t \geq 0$ . The breakthrough time  $T$  (the characteristic time required for  $F_i$  to undergo  
180 a substantial increase) is given by Eq. 4.26 of Crank (1975):

$$T = \frac{L^2}{6D_i} \quad (5)$$

181 2.2.2. *Steady state*

182 The gas flux  $F_i(t)$  from the diffusion cell into chamber B is considered to have  
183 attained steady state when  $t \gtrsim 3T$  (Daynes, 1920; Crank, 1975). Eq. 4 can then  
184 be simplified to:

$$F_i = D_i \frac{C_i(0)}{L} \quad (6)$$

185 The isotopic fractionation factor for two different species  $i$  and  $j$  – i.e., the  
186 ratio of their diffusion rates or, equivalently, of their diffusion coefficients – can  
187 be obtained from the concentration ratio  $R_{i,j}^0 = C_i(0)/C_j(0)$  at the upper interface  
188 of the diffusion cell and the flux ratio  $R_{i,j}^L = C_i(L)/C_j(L) = F_i/F_j$  at the lower  
189 interface of the diffusion cell, according to Eq. 6:

$$\frac{R_{i,j}^L}{R_{i,j}^0} = \frac{F_i/F_j}{C_i(0)/C_j(0)} = \frac{D_i}{D_j} \quad (7)$$

190 Note that the isotopic fractionation of Ne and Ar at solubility equilibrium in  
191 water is very small (see Beyerle et al., 2000). If  $i$  and  $j$  are two isotopes of the same  
192 element,  $R_{i,j}^0$  can therefore be assumed to be identical to the isotope concentration  
193 ratio in the pure test gas flowing through chamber A, and  $R_{i,j}^L$  can be assumed  
194 to be identical to the concentration ratio of the two isotopes in the carrier gas  
195 leaving the system via chamber B. We were therefore able to determine the isotope  
196 fractionation factor from Eq. 7 simply by measuring the isotope ratios in chambers  
197 A and B using static mass spectrometry. The advantage of this approach is that  
198 quantification of the fractionation factor is virtually independent of the geometry  
199 of the diffusion column, as it relies only on the isotope concentration ratios in  
200 chambers A and B, which can be measured precisely and straightforwardly using  
201 a standard noble-gas analysis protocol (Beyerle et al., 2000).

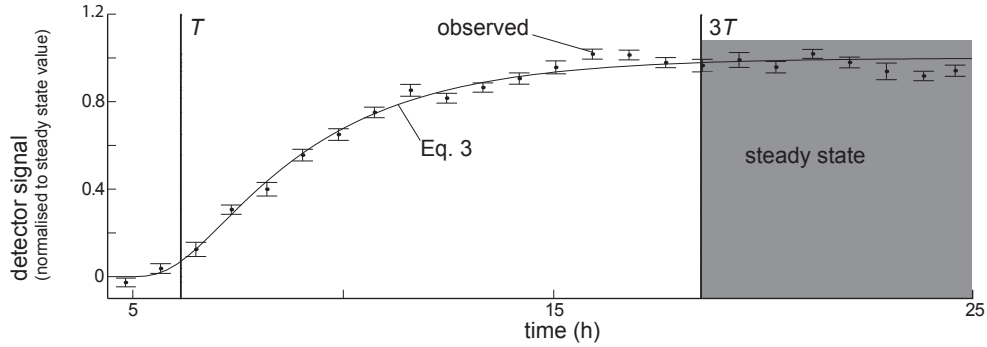


Figure 2: Breakthrough curves of  $^{20}\text{Ne}$ . Dots indicate "observed" data, measured in the outlet of chamber B with a quadrupole mass spectrometer (error bars indicate standard errors). The curve shown is the theoretical breakthrough curve, calculated from Eq. 4 with  $D_{^{20}\text{Ne}} = 3.0 \times 10^{-9} \text{ m}^2/\text{s}$  (Wise and Houghton, 1968) and  $L = 2.0 \text{ cm}$ . The breakthrough time  $T = 6.2 \text{ h}$  was calculated from Eq. 5 based on the same values for  $D_{^{20}\text{Ne}}$  and  $L$ . Steady state is considered to be attained at time  $3T$  (Daynes, 1920; Crank, 1975).

### 202 3. Results and discussion

#### 203 3.1. Experiment performance

204 Fig. 2 shows the observed and theoretical breakthrough curves calculated using  
 205 Eq. 4. The curves are in excellent agreement, as are the breakthrough times,  
 206 indicating that the experiment performs exactly as would be expected based on  
 207 the description given above (Sect. 2.2). By inserting the isotope ratios measured  
 208 in chambers A and B into Eq. 7, an accurate quantification of the isotopic frac-  
 209 tionation resulting from diffusive transport through the diffusion cell can therefore  
 210 be obtained.

#### 211 3.2. Fractionation factors

212 The flux of the test gas through the diffusion cell attained steady state ap-  
 213 proximately 18 h after the start of the experiment ( $3T$  in Fig. 2).  $^{20}\text{Ne}/^{22}\text{Ne}$  and

Table 1:  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  ratios and their standard errors measured in chambers A and B at steady-state conditions in different experimental runs (2 runs with Ne, 4 runs with Ar) using diffusion cells with different thicknesses  $L$ .

	$^{20}\text{Ne}/^{22}\text{Ne}$	$^{36}\text{Ar}/^{40}\text{Ar} \times 10^{-3}$
Chamber A ( $R_{i,j}^0$ )		
Test gas (dry):	$9.76 \pm 0.02$	$3.36 \pm 0.01$
Test gas (humidified):	$9.76 \pm 0.02$	$3.36 \pm 0.01$
Mean, error of the mean:	$9.76 \pm 0.02$	$3.36 \pm 0.01$
Chamber B ( $R_{i,j}^L$ )		
$L = 1.7$ cm	$9.86 \pm 0.02$	$3.54 \pm 0.01$
$L = 1.7$ cm	—	$3.54 \pm 0.01$
$L = 2.0$ cm	$9.86 \pm 0.02$	$3.54 \pm 0.01$
$L = 2.5$ cm	—	$3.56 \pm 0.01$
Mean, error of the mean:	$9.86 \pm 0.02$	$3.545 \pm 0.006$

214  $^{36}\text{Ar}/^{40}\text{Ar}$  ratios measured in the test gas leaving chamber A were equal to the ra-  
215 tios measured in the test gas before it passed through the humidifier. The results of  
216 different replicate experiments are given in Tab. 1.  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  ratios  
217 were measured at steady state in chambers A and B. For the Ne test gas in cham-  
218 ber A the measured isotope ratio was slightly lower than in air ( $^{20}\text{Ne}/^{22}\text{Ne} = 9.80$ ;  
219 Ozima and Podosek, 2002), which is consistent with the findings of Pavese et al.  
220 (2005) that purified atmospheric Ne from different commercial sources tends to  
221 be enriched in  $^{22}\text{Ne}$ . The  $^{36}\text{Ar}/^{40}\text{Ar}$  ratio in the test gas in chamber A showed no  
222 fractionation relative to the  $^{36}\text{Ar}/^{40}\text{Ar}$  ratio of air ( $^{36}\text{Ar}/^{40}\text{Ar} = 3.384 \times 10^{-3}$ ; Oz-  
223 ima and Podosek, 2002). Note that for consistency with previous data measured  
224 in our noble gas laboratory we used the  $^{36}\text{Ar}/^{40}\text{Ar}$  value of Ozima and Podosek

225 (2002) (as recommended by the IUGS Subcommittee on Geochronology) rather  
226 than the more recent values reported by Lee et al. (2003) and Mark et al. (2011).

227 For both the  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  ratios the results obtained from the in-  
228 dividual replicate gas samples agreed to within their respective standard errors. In  
229 agreement with the theory, the ratios determined were found to be independent of  
230 the thickness of the diffusive layer (Tab. 1). Diffusion through the diffusion cell  
231 resulted in increases of  $1.0 \pm 0.3\%$  and  $5.5 \pm 0.4\%$ , respectively, in the experimen-  
232 tally observed  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  ratios.

233 Tab. 2 lists the fractionation factors calculated from Eq. 7 using the mean val-  
234 ues of the  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  ratios measured in chambers A and B (Tab. 1)  
235 and compares the experimentally determined isotopic fractionation with the iso-  
236 topic fractionation predicted by the square root relation (Eq. 1), by the modified  
237 square root relation (Eq. 2) and by the results of the molecular dynamics sim-  
238 ulation of Bourg and Sposito (2008) (Eq. 3). Our experimentally determined  
239  $^{20}\text{Ne}/^{22}\text{Ne}$  fractionation factor is significantly smaller than that calculated from  
240 the square root relation (Eq. 1), but agrees with the predictions based on the  
241 molecular dynamics calculations of Bourg and Sposito (2008), (Eq. 3). In con-  
242 trast to this, our experimentally determined  $^{36}\text{Ar}/^{40}\text{Ar}$  fractionation factor agrees  
243 with that calculated from the square root relation (Eq. 1), but *not* with that based  
244 on the molecular dynamics calculations. The  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  fractiona-  
245 tion factors predicted by the modified square root relation (Eq. 2) are inconsistent  
246 with all our experimental results.

247 Note that the  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  fractionation factors inferred from the

Table 2: Comparison of fractionation factors determined experimentally in this study with fractionation factors determined from the square root relation or molecular dynamics calculations (including standard errors; the  $2\sigma$  errors reported by Bourg and Sposito (2008) were converted to  $1\sigma$  errors) and from the square root relation\*, treating water as if it were a gas of molecular weight 18.

	$D_{^{20}\text{Ne}}/D_{^{22}\text{Ne}}$	$D_{^{36}\text{Ar}}/D_{^{40}\text{Ar}}$
This study (from means in Tab. 1)	$1.010 \pm 0.003$	$1.055 \pm 0.004$
Square root relation (Eq. 1)	1.049	1.054
Modified square root relation* (Eq. 2)	1.022	1.017
Molecular dynamics (Bourg and Sposito, 2008) (Eq. 3)	$1.014 \pm 0.001$	$1.008 \pm 0.002$

248 square root relation (Eq. 1) are very similar, because the mass ratios of the two  
249 isotope pairs are almost the same ( $20/22 \approx 0.909$  and  $36/40 \approx 0.900$ ). This close  
250 agreement is in contrast to the difference in the fractionation behaviour of the Ne  
251 and Ar isotopes observed in our experiments. It is possible that this discrepancy  
252 results from the fact that square root relation is based on the kinetics of diffusion  
253 in gases rather than in water. We also note that for Ar, the results of the molec-  
254 ular dynamics calculations of Bourg and Sposito (2008) are not consistent with  
255 the experimental results of our study. As pointed out by the authors, the accu-  
256 racy of the molecular dynamics calculations is limited by our knowledge of the  
257 intermolecular potential functions used in the model.

258 Therefore, and because the results obtained from the modified square root rela-  
259 tion (Eq. 2) are also inconsistent with the experimental results, neither of the forms  
260 of the square root relation nor the molecular dynamics simulation would seem to  
261 provide an adequate, generally valid, physically sound description of the isotopic  
262 fractionation of both Ne and Ar that results from molecular diffusion in water.



263 However, our results do provide clear evidence that the square root relation is able  
264 to describe adequately the isotopic fractionation of  $^{36}\text{Ar}/^{40}\text{Ar}$ . Arguments on the  
265 transport of dissolved substances in water by molecular diffusion that are based  
266 primarily on the  $^{36}\text{Ar}/^{40}\text{Ar}$  ratio (e.g., Peeters et al., 2002; Brennwald et al., 2005)  
267 therefore remain valid and can still be used to determine whether molecular dif-  
268 fusion controls noble gas abundances in natural water, as the assumed behaviour  
269 of the Ar isotopes is consistent with our newly determined isotopic fractionation  
270 factor.

271 We hypothesize that different intermolecular forces between noble gases and  
272 dipole water molecules might explain our experimental findings. This hypoth-  
273 esis is supported by quantum-chemical calculations supplemented by structural  
274 parameters describing the geometry of noble gas-water complexes in liquid water  
275 (Bagno, 1998; Sun et al., 2013), with water molecules clustering around dissolved  
276 noble gases as a result of intermolecular interactions (Ludwig, 2001). Bagno  
277 (1998) found the intermolecular force between Ne and liquid water to be 40–  
278 60% lower than that between Ar and liquid water. A recent study by Sun et al.  
279 (2013) found the geometry of the Ne-(liquid)water complex to differ from the ge-  
280 ometry of the Ar-(liquid)water, Kr-(liquid)water and Xe-(liquid)water complexes.  
281 In Ne-(liquid)water complexes, Ne is orientated away from the hydrogen bonds,  
282 implying that the internal rotation of the  $\text{H}_2\text{O}$  molecule is hindered less than in  
283 the case of Ar, Kr and Xe, which are orientated towards the hydrogen bonds. Sun  
284 et al. (2013) also found that the prevailing geometry of Ne-water complexes was  
285 almost the same for  $^{20}\text{Ne}$  and  $^{22}\text{Ne}$ , and concluded therefore that the isotopic effect

286 on the structures of the Ne-water complex was small. These findings might estab-  
287 lish a conceptual framework for understanding why diffusive transport through  
288 water fractionates Ne and Ar isotopes differently.

#### 289 4. Conclusions

290 We empirically quantified the fractionation of  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  ratios  
291 in response to the molecular diffusion of Ne and Ar in water. For  $^{20}\text{Ne}/^{22}\text{Ne}$  the  
292 experimentally determined fractionation factor ( $D_{^{20}\text{Ne}}/D_{^{22}\text{Ne}} = 1.010 \pm 0.003$ )  
293 agrees well with the results of the molecular dynamics calculations of Bourg and  
294 Sposito (2008) ( $D_{^{20}\text{Ne}}/D_{^{22}\text{Ne}} = 1.014 \pm 0.001$ ). However, it is significantly lower  
295 than that predicted either by the square root relation, Eq. 1 ( $D_{^{20}\text{Ne}}/D_{^{22}\text{Ne}} = 1.049$ )  
296 or the modified square root relation with reduced masses, Eq. 2 ( $D_{^{20}\text{Ne}}/D_{^{22}\text{Ne}} =$   
297 1.022).

298 By contrast, for  $^{36}\text{Ar}/^{40}\text{Ar}$ , the experimentally determined fractionation factor  
299 ( $D_{^{36}\text{Ar}}/D_{^{40}\text{Ar}} = 1.055 \pm 0.004$ ) agrees well with that predicted by the square root  
300 relation ( $D_{^{36}\text{Ar}}/D_{^{40}\text{Ar}} = 1.054$ ) (implying that models relying on this relationship  
301 remain valid). However, it is significantly higher than that predicted either by the  
302 modified square root relation ( $D_{^{36}\text{Ar}}/D_{^{40}\text{Ar}} = 1.017$ ) or by the molecular dynamics  
303 calculations of Bourg and Sposito (2008) ( $D_{^{36}\text{Ar}}/D_{^{40}\text{Ar}} = 1.008 \pm 0.003$ ).

304 Thus, neither the square root relation nor the molecular dynamics approach  
305 of Bourg and Sposito (2008) is capable of giving a general explanation of our  
306 experimental results for the fractionation of both  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$ . We  
307 speculate that the different fractionation behaviour of  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  in

308 water is related to intermolecular interactions between water molecules in the liq-  
309 uid phase and dissolved noble gases (Bagno, 1998; Sun et al., 2013). To expand  
310 our knowledge of the molecular diffusion of noble gas isotopes, we suggest mea-  
311 suring the isotopic fractionation resulting from diffusion for all noble gases and  
312 their isotopes in water and in other liquids with different physico-chemical prop-  
313 erties (e.g., oils or alcohols). Despite the lack of a theoretical model that is able to  
314 explain quantitatively the fractionation factors determined in our experiments, we  
315 consider that our direct measurements provide a robust basis for studies that use  
316 the fractionation of the noble-gas isotope ratios  $^{20}\text{Ne}/^{22}\text{Ne}$  and  $^{36}\text{Ar}/^{40}\text{Ar}$  to assess  
317 molecular diffusion in water bodies.

### 318 **Acknowledgements**

319 This work was financed by the Swiss National Science Foundation (SNF-  
320 project 200020 – 132155). We thank Frank Richter and an anonymous reviewer  
321 for their helpful criticism, which greatly helped in improving the manuscript.

### 322 **References**

- 323 Aeschbach-Hertig, W., El-Gamal, H., Wieser, M., and Palcsu, L. (2008). Model-  
324 ing excess air and degassing in groundwater by equilibrium partitioning with a  
325 gas phase. *Water Resour. Res.* **44**, 1–12.
- 326 Aeschbach-Hertig, W. and Solomon, D. (2013). Noble Gas Thermometry  
327 in Groundwater Hydrology. In *The Noble Gases as Geochemical Tracers*.  
328 Springer, Berlin, Heidelberg, pp. 81–122.

- 329 Bagno, A. (1998). The ab initio neon-water potential-energy surface and its re-  
330 lationship with the hydrophobic hydration shell. *J. Chem. Soc. Faraday Trans.*  
331 **94**, 2501–2504.
- 332 Beyerle, U., Aeschbach-Hertig, W., Imboden, D. M., Baur, H., Graf, T. and  
333 Kipfer, R. (2000). A mass spectrometric system for the analysis of noble gases  
334 and tritium from water samples. *Environ. Sci. Technol.* **34**, 2042–2050.
- 335 Bourg I. and Sposito G. (2008). Isotopic fractionation of noble gases by diffusion  
336 in liquid water: Molecular dynamics simulations and hydrologic applications.  
337 *Geochim. Cosmochim. Acta* **72**, 2237–2247.
- 338 Brennwald, M. S., Hofer, M., Peeters, F., Aeschbach-Hertig, W., Strassmann, K.,  
339 Kipfer, R., and Imboden, D. M. (2003). Analysis of dissolved noble gases in  
340 the pore water of lacustrine sediments. *Limnol. Oceanogr.: Methods* **1**, 51–62.
- 341 Brennwald, M. S., Kipfer, R., and Imboden, D. M. (2005). Release of gas bubbles  
342 from lake sediment traced by noble gas isotopes in the sediment pore water.  
343 *Earth Planet. Sci. Lett.* **235**, 31–44.
- 344 Brennwald, M. S., Vogel, N., Scheidegger, Y., Tomonaga, Y., Livingstone, D. M.,  
345 and Kipfer, R. (2013). Noble gases as environmental tracers in sediment pore  
346 waters and in stalagmite fluid inclusions. In *The Noble Gases as Geochemical*  
347 *Tracers*. Springer, Berlin, Heidelberg, pp. 123–153.
- 348 Craig H. and Gordon L. (1965). Deuterium and oxygen 18 variation in the ocean  
349 and marine atmosphere. In *Stable Isotopes in Oceanographic Studies and Pa-*  
350 *leotemperatures* (eds. E. Tongiogi). Spoleto, Pisa, pp. 9–130.
- 351 Crank, J. (1975). *The mathematics of diffusion, 2nd ed.* Clarendon Press, Oxford.
- 352 Cussler, E. L. (2009). *Diffusion: Mass transfer in fluid systems, 3rd ed.* Cambridge  
353 Univ. Press, Cambridge.
- 354 Daynes, H. (1920). The process of diffusion through a rubber membrane. *Proc.*  
355 *Royal Soc. London.* **97**, 286–307.
- 356 Graham, T. (1833). On the law of the diffusion of gases. *Philos. Mag.* **2**, 175–190,  
357 269–276, 351–358.

- 358 Holocher, J., Peeters, F., Aeschbach-Hertig, W., Hofer, M., Brennwald, M. S.,  
359 Kinzelbach, W., and Kipfer, R. (2002). Experimental investigations on the for-  
360 mation of excess air in quasi-saturated porous media. *Geochim. Cosmochim.*  
361 *Acta* **66**, 4103–4117.
- 362 Jähne, B., Heinz, G., and Dietrich, W. (1987a). Measurement of the diffusion  
363 coefficients of sparingly soluble gases in water. *J. Geophys. Res.* **92**, 10767–  
364 10776.
- 365 Jähne, B., Münnich, K. O., Bösinger, R., Dutzi, A., Huber, W and Libner, P.  
366 (1987b). On the parameters influencing air-water gas exchange. *J. Geophys.*  
367 *Res.* **92**, 2156–2202.
- 368 Kipfer, R., Aeschbach-Hertig, W., Peeters, F., and Stute, M. (2002). Noble gases  
369 in lakes and ground waters. In *Noble Gases in Geochemistry and Cosmochem-*  
370 *istry* (eds. D. Porcelli, C. J. Ballentine and R. Wieler). Mineralogical Society of  
371 America, pp. 615–700.
- 372 Klump, S., Kipfer, R., Cirpka, O., Harvey, C., Brennwald, M. S., Ashfaq, K.,  
373 Badruzzaman, A., Hug, S., and Imboden, D. M. (2006). Groundwater dynamics  
374 and arsenic mobilization in Bangladesh assessed using noble gases and tritium.  
375 *Environ. Sci. & Technol.* **40**, 243–250.
- 376 Lee, J.-Y., Marti, K., Severinghaus, J.P., Kawamura, K., Yoo, H.-S., Lee, J.B.,  
377 Kim, J.S. (2006). A redetermination of the isotopic abundances of atmospheric  
378 Ar. *Geochim. Cosmochim. Acta* **70**, 4507–4512.
- 379 Lippmann, J., Stute, M., Torgersen, T., Moser, D., Hall, J., Lin, L., Borcsik, M.,  
380 Bellamy, R., and Onstott, T. (2003). Dating ultra-deep mine waters with noble  
381 gases and <sup>36</sup>Cl, Witwatersrand Basin, South Africa. *Geochim. Cosmochim. Acta*  
382 **67**, 4597 – 4619.
- 383 Ludwig, R. (2001). Water: From Clusters to the Bulk. *Angewandte Chemie*  
384 *International Edition* **40**, 1808–1827.
- 385 Mächler, L., Brennwald, M. S., and Kipfer, R. (2012). Membrane inlet mass spec-  
386 trometer for the quasi-continuous on-site analysis of dissolved gases in ground-  
387 water. *Environ. Sci. Technol.* **46**, 8288–8296.

- 388 Mark, D.F., Stuart, F.M., de Podesta, M., (2011). New high-precision measure-  
389 ments of the isotopic composition of atmospheric argon. *Geochim. Cosmochim.*  
390 *Acta* **75**, 7494–7501.
- 391 Moore, J. (1999). *Physical chemistry, 5th ed.* Prentice Hall.
- 392 Ozima, M. and Podosek, F. (2002). *Noble gas geochemistry.* Cambridge Univ.  
393 Press, Cambridge.
- 394 Pavese, F., Fellmuth, B., Head, D. I., Hermier, Y., Hill, K. D., and Valkiers, S.  
395 (2005). Evidence of a systematic deviation of the isotopic composition of neon  
396 from commercial sources compared with its isotopic composition in air. *Anal.*  
397 *Chem.* **77**, 5076–5080.
- 398 Peeters, F., Beyerle, U., Aeschbach-Hertig, W., Holocher, J., Brennwald, M. S.,  
399 and Kipfer, R. (2002). Improving noble gas based paleoclimate reconstruction  
400 and groundwater dating using  $^{20}\text{Ne}/^{22}\text{Ne}$  ratios. *Geochim. Cosmochim. Acta* **67**,  
401 587–600.
- 402 Richter, F., Mendybaev, R., Christensen, J., Hutcheon, I., Williams, R., Sturchio,  
403 N., and Beloso Jr., A. (2006). Kinetic isotopic fractionation during diffusion of  
404 ionic species in water. *Geochim. Cosmochim. Acta* **70**, 277–289.
- 405 Schlosser, P. and Winckler, G. (2002). *Noble gases in geochemistry and cos-*  
406 *mochemistry*, In *Noble Gases in Geochemistry and Cosmochemistry* (eds. D.  
407 Porcelli, C. J. Ballentine and R. Wieler). Mineralogical Society of America,  
408 pp. 701–730.
- 409 Schwarzenbach, R. P., Gschwend, P. M., and Imboden, D. M. (2003). *Environ-*  
410 *mental Organic Chemistry (2nd ed.)* New York: John Wiley & Sons, Inc.
- 411 Sun, X., Hu, Y., and Zhu, H. (2013). Ab initio potential energy surface and predicted  
412 rotational spectra for the Ne–H<sub>2</sub>O complex. *J. Chem. Phys.* **138**, 1–7.
- 413 Tempest, K. E. and Emerson, S. (2013). Kinetic isotopic fractionation of argon  
414 and neon during air-water gas transfer. *Mar. Chem.* **153**, 39 – 47.
- 415 Visser, A., Broers, H., and Bierkens, M. (2007). Dating degassed groundwater  
416 with  $^3\text{H}/^3\text{He}$ . *Water Resour. Res.* **43**.

- 417 Wise, D. and Houghton, G. (1968). Diffusion coefficients of neon, krypton, xenon,  
418 carbon monoxide and nitric oxide in water at 10–60 °C. *Chem. Eng. Sci.* **23**,  
419 1211 – 1216.
- 420 Zhou, Z., Ballentine, C. J., Kipfer, R., Schoell, M., and Thibodeaux, S. (2005).  
421 Noble gas tracing of groundwater coalbed methane interaction in the San Juan  
422 Basin, USA. *Geochim. Cosmochim. Acta* **69**, 5413–5428.