CO₂ hydrogenation reaction over pristine Fe, Co, Ni, Cu and Al₂O₃ supported Ru- comparison and activation energy determination

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Abstract

Fe, Co, Ni and Cu are the main non-noble industrially significant catalysts in the CO₂ and CO gas phase hydrogenation reaction towards hydrocarbons and alcohols. These catalysts are typically supported on metal oxides such as SiO₂, TiO₂, Al₂O₃ and ZnO, in order to maximize the activity towards the desired reaction. The role of the supporting material is to stabilize the catalytic nanoparticles and to prevent sintering at the elevated reaction temperatures and pressures. The supporting phase can improve the reaction activity or even have a crucial role in the reaction, as is the case, e.g. for the Methanol synthesis over Cu based catalysts on ZnO. Studying the metals without a supporting oxide phase is of capital importance for the fundamental understanding of the catalytic activity of the metal phase. Therefore, we investigated the pristine transition metals Fe, Co, Ni and Cu (diluted with silica glass beads to avoid sintering) towards their activity in the CO₂ hydrogenation reaction and determined the activation energy. An Al₂O₃ supported Ruthenium catalyst with 0.5 mass percent of Ru loading was taken as reference system. It was found that Co, Ni and Ru/Al₂O₃ are mostly active in the Sabatier reaction, while Fe is active in the reverse water gas shift reaction. Cu as pristine metal shows no catalytic activity. C₂+ hydrocarbons were formed on Co in low concentrations. For the calculation of the activation energy, the kinetically determined temperature range of the reaction is identified with a high resolution in time by means of a quantitative gas analysis method with an online mass spectrometer. The activation energy of the CO₂ hydrogenation reaction was determined to be 50 kJ/mol over Fe, 77 kJ/mol over Co, 74 kJ/mol over Ni and 73 kJ/mol over the Ru/Al₂O₃ catalyst, indicating similar reaction pathways over Co, Ni and Ru/Al₂O₃ and a different reaction mechanism on Fe.

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1. Introduction

Energy storage is crucial for the development of an energy supply based on renewable energy. The energy supply from wind -and solar power plants is intermittent in time due the day/night cycles, weather conditions, and seasonality. Since the supply of electricity must correspond to the demand in the power grid at all times to keep the grid frequency stable, energy storage is required to buffer the fluctuations from the stochastically producing energy converters such as wind- and solar power plants. Batteries are favorable for efficient short term storage, but are too costly to provide long-term storage capacity¹. Liquid synthetic fuels are a promising energy carrier for seasonal energy storage due to their high gravimetric -and volumetric energy density and stability in ambient conditions which is up to a hundred times larger than in batteries^{2,3}. CO₂ extracted from air can be hydrogenated with hydrogen produced by electrolysis driven by renewable energy. The energy is then stored in the chemical bond of the hydrocarbons and is released upon combustion which is net CO₂ emission free. Today's technologies allow CO₂ hydrogenation via the Sabatier reaction to methane or via the reverse water gas shift reaction (RWGS) to CO, followed by the Fischer -Tropsch reaction (FTR)⁴. The FTR is an unselective reaction which leads to a wide hydrocarbon product distribution ranging from low molar weight gaseous hydrocarbons, alcohols and long chained waxes⁵. Therefore, energy intensive refining of the products is required to obtain a specific hydrocarbon fraction. The Sabatier reaction is instead a selective reaction, with methane as the major product. Fe, Co, Ni, Cu, Ru and Rh are the most active elements known for the CO and CO₂ hydrogenation reaction and they are the key building blocks of the industrially significant catalysts^{6,7}. In order to increase the surface area, the catalysts are typically nanosized particles supported on metal oxides such as Al₂O₃, SiO₂, TiO₂, ZnO and ZrO₂ to stabilize the active species, prevent sintering⁸ and adapt the reaction selectivity⁹. In particular in the case of Cu, the support phase has a principal role in the CO₂ hydrogenation reaction mechanism^{6,10}. The metal-support interactions and the influence on the reaction's activity and selectivity are not fully understood yet and a full understanding of these phenomena is crucial for the design of new, more selective catalysts. Therefore, it is of great interest to investigate the direct CO₂ hydrogenation over the unsupported pristine metal catalysts. This has been done on single crystal catalysts in Ultrahigh Vacuum (UHV) conditions^{11,12} and by means of density functional theory calculations (DFT)^{13,14,15} and micro kinetic reaction modelling^{16,17}. The CO₂ hydrogenation reaction on Fe, Co, Ni and Cu catalyst on different supports- and also in their pristine form, was the object of numerous studies in the 1970s after the interest in synthetic fuels increased due to the oil crisis^{18,19,20}. Nevertheless, a direct comparison of the pristine metal catalysts in similar reaction conditions with the determination of the activation energy has not been reported so far.

In this paper the activity of the pristine transition metals Fe, Co, Ni and Cu for the CO₂ hydrogenation reaction is investigated. The reaction was carried out in a micro reactor in quasi equilibrium conditions, meaning that the space velocity (around 1000h⁻¹) and heating rate (1K/min) were relatively low. For

the product gas composition analysis, a quantitative gas analysis method by means of mass spectrometry (MS) has been developed, allowing the determination of the product gas stream composition, and therefore the calculation of the kinetic parameters, with a high resolution in time. The catalyst activity results are discussed in the frame of a thermodynamic reaction analysis.

2. Experimental

The experiments were carried out in a stainless-steel plug flow reactor placed in a tubular furnace. Three thermocouples are placed in -or on the reactor in order to monitor the reaction temperature. The temperature measured in the reaction tube in close vicinity to the catalyst bed is used as reference temperature for the reaction. The gas flows were controlled via three mass flow controllers for CO₂, H₂ and He. The gas lines after the reactor to the analysis instruments were heated to 200°C to avoid condensation of the product or water.

The gas stream has been analyzed by means of a Mass Spectrometer (Pfeiffer OmniStar 320) with a Faraday and Secondary Electron Detector (MS-SEM) and a Gas Chromatograph (SRI 8610C) equipped with a Flame Ionization Detector (FID) and a Thermal Conductivity Detector (TCD).

For the gas analysis, a software application was developed within MATLAB R2016b for the GC and MS to quantify the partial pressures in the product gas stream as a function of the reaction temperature.

The metal powders of Fe, Co, Ni and Cu were obtained from Goodfellow (Table SI) and examined for their purity by means of X-ray photoelectron spectroscopy (XPS). No impurities were detected by means of XPS. The catalysts were reduced with Hydrogen at elevated temperatures prior to the experiment to obtain a purely metallic surface. The specific weight of the catalyst and the surface area of the catalysts used in this study were determined by means of SEM (to estimate the particle size) and liquid N₂ adsorption isotherms to determine the specific surface area.

Catalyst preparation and packing

In preliminary experiments, it was found that the metal powders can sinter during the reaction at elevated temperatures up to 650°C. In particular, Co and Cu powders are prone to sinter. This caused clogging of the reactor, making the experiment not reproducible. Since it was the aim not to alter the reaction with a supporting phase, the catalyst powders were pressed to 8mm pellets with a weight equivalent of four tons and then broken down to smaller grains with an approximate diameter of 1-1.5mm. The grains were then mixed in an equal weight ratio with glass beads in the same size regime to prevent grain agglomeration. The glass beads are made of borosilicate glass and were purchased by Schäfer Glas. They have a diameter of 1mm and were not affected by the reaction conditions. With this preparation method of the catalyst, no macroscopic sintering effects were observed after the experiments thus enabling comparable reaction conditions among the four pristine metals.

Catalyst pretreatment with Helium and Hydrogen

To evaporate moisture from the catalyst and the tubing, the reactor and tubing were preheated with an applied He gas flow of 10 ml/min for a minimum time of 30min. The reactor was preheated to 150°C, the tubing to 200°C. Subsequently, the following the catalysts were reduced with H₂ to obtain a metallic surface. This was done with a H₂ flow of 7.5 ml/min and 2.5 ml/min of He at a starting temperature of

150°C. The temperature was then ramped up with 10°C/min to a set point of 700°C, while simultaneously measuring the gas composition with the MS. With this TPR, the temperature ranges at which the surface is reduced from oxides and carbides is determined via the formation of water (m/z 18 peak) and methane (m/z 16 peak). In case the surface reduction was not completed at the set point temperature after ramping up, the temperature was kept at the set point of 700°C to further reduce the surface until the m/z 18 and m/z 16 peaks declined.

CO₂ hydrogenation experiment

After reducing the catalyst with H₂, the experimental gas flow was set with the gas stream going through the reactor bypass. The experimental gas flow was: CO₂ 1.5ml/min, H₂ 6ml/min and He 2.5 ml/min. Therefore, the total flow was 10ml/min and the H₂:CO₂ ratio 4:1. The gas flow rate of 10ml/min for the reaction gas stream was chosen as a tradeoff between quasi equilibrium conditions, MFC reliability (MFC models: Bronkhorst El Flow series. Flow range: 0.4-20 ml/min. Absolute measurement error in ml/min: 0.1% of maximum set point (20ml/min) plus 0.5% of set point) and the time the gas product gas stream requires to reach the analysis systems (there is less than a minute of dead time between the reactor and the MS inlet). After the setpoint gas mixture was reached, the valve to the reactor was opened, the bypass closed, the temperature ramping set to 1°C min and the measurement with MS and GC started. The maximum reactor oven temperature was set to 700°C. The total time for the CO₂ hydrogenation experiment therefore takes 550 min since the ramping was started at 150°C. The experiments were carried out in ambient pressure. The reactor is a plug flow reactor with a total length of 180mm. The inner diameter of the reaction zone, which starts 75mm after the inlet, is 7mm in diameter ($d_{i,2}$). Before the reaction zone, the inner tube diameter is 4mm ($d_{i,1}$). The catalyst is hold in place to the inlet site by a sintered steel filter with a pore size of approximatively 60 micrometers (Swagelok SS-2F-K4-60) and a diameter of 7mm, which sits on the step of the inner diameter change at 75mm from the inlet site. To load the catalyst, a small layer of glass wool is inserted on top of the solid filter. Then, the catalyst is loaded and topped with another layer of glass wool to keep the catalyst in place to the outlet site. To calculate the space velocity, the distance $l_{catalyst}$ between the first layer of glass wool and the top of the loaded catalyst is measured. The space velocity is then calculated as follows:

$$SV \left[\frac{1}{h} \right] = \frac{\dot{V}_{reactants} \left[\frac{mL}{h} \right]}{V_{reactor} [ml]} = \frac{\dot{V}_{reactants}}{\left(l_{catalyst} * \left(\frac{d_{i,2}}{2} \right)^2 \pi \right)}$$

Data acquisition and analysis

The product gas stream was analyzed with the MS and GC. The MS has a sampling rate of approximately 2min per scan, while the GC requires 17.5min for measurement cycle. Since the heating rate was 1°C/min (minimal setpoint possible at the oven), the temperature between two spectra is 2K for the MS and 17.5K for the GC. The kinetically determined temperature ranges are typically around 30 K wide. Therefore, the GC has less than two data points for this range which is not sufficient to determine the kinetic reaction range with a heating ramp of 1K/min. The accurate identification of the kinetic reaction range is the basis for the calculation of the activation energy. To enable the reaction to be carried out in one day, the heating ramp was not to be reduced. Therefore, a quantitative gas analysis by means of mass spectrometry was developed, where a fast data acquisition was achieved. The GC was used as backup instrument and to identify C₂+ hydrocarbon products. Throughout this study, the Faraday detector and a scan width of 1-100 mass/charge (m/z) and a scan speed of 1s per m/z was used for the MS. In the first step after the experiment, the spectra are loaded into an array in MATLAB R2016b, where they were correlated to the reaction temperature. Then the partial pressures of the gases were calculated based on the calibration spectra. Since the internal pressure of the MS can change over the course of the experiment, the signal intensity varies with this pressure change since a higher difference in pressure between the MS and the gas line means a higher gas flow into the MS and therefore a stronger signal. Since this does not influence the composition of the gas, the sum of all partial pressures of the detected species was normalized at the total reaction pressure in every measurement point. With that, the partial pressures of all detected gas species are known for every spectrum. The CO₂ conversion, product yield –and selectivity are calculated based on the principle of mass conservation with the carbon balance. Since methane and carbon monoxide are the only carbon containing reaction products of significant quantity, the CO₂ conversion is calculated based on the partial pressure of the reaction products p_{CH_4} , p_{CO} and the partial pressure of CO₂ after the reaction.

$$p_{\text{products}} = p_{\text{CH}_4} + p_{\text{CO}}$$

$$X_{\text{CO}_2} = \frac{p_{\text{products}}}{p_{\text{products}} + p_{\text{CO}_2, \text{out}}}$$

The yield of Methane Y_{CH_4} is calculated as follows:

$$Y_{\text{CH}_4} = X_{\text{CO}_2} * \frac{p_{\text{CH}_4}}{p_{\text{products}}}$$

The carbon monoxide yield Y_{CO} is then given by:

$$Y_{\text{CO}} = X_{\text{CO}_2} - Y_{\text{CH}_4}$$

The selectivity S_i of each product i is given by:

$$S_i = \frac{p_i}{p_{\text{products}}}$$

The full derivation of the CO₂ conversion calculation is given in the supplementary information.

3. Results and discussion

3.1. Thermodynamics

The maximal conversion of CO₂ at a given pressure and temperature is defined by the thermodynamic equilibrium conversion at this working point. Thermodynamic limitations are independent from the catalyst used, but the nature of the catalyst controls the reaction kinetics and thus the product selectivity at the reactor outlet. In this study, two products containing carbon were detected in significant quantities: CH₄ and CO. The observed reactions are the Sabatier and Reverse Water Gas Shift (RWGS) reactions. In the following, their thermodynamic equilibria are given as well as for the simultaneous formation of CH₄ and CO as functions of temperature and pressure. In all, five gas species are present as reactants and products (CO, CO₂, H₂, H₂O and CH₄), and have to be taken into consideration in the equilibria calculations.

Equilibrium conversion to CH₄ and CO as function of pressure and temperature

The conversion of CO₂ to CH₄ is an exothermic reaction and the product formation is therefore favored at low reaction temperatures. Following the Le-Chatelier principle, an increase in reaction pressure shifts the equilibrium to the product side, since the overall number of moles is decreased during the reaction. Therefore, a higher reaction pressure increases the concentration of the product at thermodynamic equilibrium.

The thermodynamic equilibrium is calculated with the Van't Hoff equation and the equilibrium constant which is given by the partial reaction pressures. With the stoichiometry of the reaction, the equilibrium is expressed as function of the total reaction pressure and the partial pressure of CH₄.

$$-\frac{\Delta G_R(T)}{RT} = -\frac{\Delta H_R(T)}{RT} + \frac{\Delta S_R(T)}{R} = \ln(K_{\text{eq}})$$

With $K_{\text{eq},\text{CH}_4}$ given by (assuming ideal gas behavior)

$$K_{\text{eq},\text{CH}_4} = \frac{p_{\text{CH}_4} \cdot p_{\text{H}_2\text{O}}^2}{p_{\text{CO}_2} \cdot p_{\text{H}_2}^4} = \frac{p_{\text{CH}_4} \cdot 4p_{\text{CH}_4}^2}{\left(\frac{4}{5}(p_{\text{tot}} - 3p_{\text{CH}_4}) \cdot \frac{1}{5}(p_{\text{tot}} - 3p_{\text{CH}_4})\right)}$$

Similarly, the equilibrium constant for the RWGS is calculated independently of the Sabatier reaction:

$$K_{eq,CO} = \frac{p_{CO} * p_{H_2O}}{p_{CO_2} * p_{H_2}} = \frac{p_{CO}^2}{\left(\frac{1}{2} p_{tot} - p_{CO}\right)^2}$$

The equations for K_{eq,CH_4} and $K_{eq,CO}$ are implicit since the reaction enthalpy and entropy are temperature dependent and the equation has to be solved numerically. The parameters to calculate the temperature dependent reaction enthalpy and entropy are from the NIST chemistry WebBook. The calculated equilibria are presented in Figure 1.

Figure 1: Equilibrium conversion of CO₂ to CH₄ and CO for temperatures between 400 K and 1400 K and pressures from 1 bar to 50 bar. The exothermic Sabatier reaction is dependent on pressure. The endothermic RWGS reaction is independent of pressure. The reactions were calculated independent of each other.

Simultaneous equilibrium conversion to CH₄ and CO

To have a thermodynamic foundation for the interplay between the Sabatier and the RWGS reaction, the equilibrium conversion taking into consideration both reactions, was calculated. The result is plotted in Figure 2. The Sabatier reaction is dominant at low reaction temperatures up to approximately 800 K to 900 K (depending also on the reaction pressures). The RWGS is only favored at higher reaction

temperatures since it is an endothermic reaction. This leads to an expected minimum in conversion in the temperature range of 800 K to 900 K. It was found experimentally, according to the results of Figure 2, that the formation of methane is predominant on the Co, Ni and Ru/Al₂O₃ catalyst in the temperature range from approximately 400 K to 800 K. For this reason, almost the entire CO₂ conversion is driven by the methanation reaction. On the other hand, the iron catalyst is less selective to the methanation reaction, showing an activity towards the RWGS at lower temperatures than the other catalysts.

The thermodynamic analysis of the CO₂ hydrogenation reaction with the simultaneous formation of CH₄ and CO has to be carried out using the extent of reaction method. For the system considered, two reactions are required to characterize the thermodynamic equilibrium.

where λ_1 and λ_2 are the fractions of reacted CO₂ for each reaction.

By doing the mass balance for both reactions and respecting the stoichiometry, the partial pressure of CO₂ after the reaction can be expressed as ($p_{\text{H}_2} = 4p_{\text{CO}_2}$)

$$p_{\text{CO}_2, \text{out}} = \frac{p_{\text{CO}_2, \text{in}} - \lambda_1 - \lambda_2}{5p_{\text{CO}_2, \text{in}} - 2\lambda_1} * p_{\text{tot}}$$

λ_1 and λ_2 are given by the equilibrium conversion for each reaction. The solution of the non-linear system:

$$\begin{cases} k_{\text{eq, Met}} = \frac{p_{\text{CH}_4} * p_{\text{H}_2\text{O}}^2}{p_{\text{CO}_2} * p_{\text{H}_2}^4} \\ k_{\text{eq, RWGS}} = \frac{p_{\text{CO}} * p_{\text{H}_2\text{O}}}{p_{\text{CO}_2} * p_{\text{H}_2}} \end{cases}$$

gives the values of λ_1 and λ_2 as a function of temperature. On the basis of these values, the global conversion of CO₂ is determined. At low temperature, the CO₂ conversion is almost entirely due to the Sabatier reaction and thus dependent on the activity of the catalyst in this reaction. At high temperature, the methanation reaction is shifted towards the reactant side, so that the entire CO₂ conversion is due to the RWGS reaction. Furthermore, the different influence of the two reactions is evident in the effect of pressure. While in the low temperature regime an increase of pressure causes a shift in the equilibrium concentration towards the products (and thus towards higher CO₂ conversion), at high temperature the pressure effect is not present. The origin of this difference is found in the different pressure dependence of the two reactions, due to the different stoichiometry (decrease in number of moles for methanation, constant number of moles for RWGS). With this calculation, the ideal working point for a desired product composition can be selected.

Figure 2: Equilibrium conversion of CO₂ to CH₄ and CO as a function of temperature and pressure with the Sabatier and RWGS reaction occurring in parallel.

3.2. Reactivity investigation

CO₂ conversion and CH₄ yield over Fe, Co, Ni and Cu in comparison to Ru/Al₂O₃

The experimental results of the CO₂ hydrogenation reaction over Fe, Co, Ni and Cu are presented in this section. The results are compared to Ru/Al₂O₃ catalysts, since this is considered the state-of-the-art catalyst for the Sabatier reaction. The literature on the Ru/Al₂O₃ catalyst in the CO₂ hydrogenation reaction goes back to 1973, when a catalytic performance study and a kinetic analysis of a 0.5 wt.% Ru on Al₂O₃ was carried out by Lunde and Kester¹⁸. In that study, a maximum CO₂ conversion of 85% and an activation energy of 70.5 kJ/mol for the CO₂ conversion is reported. More recently the performance of 3% Ru/Al₂O₃ catalysts has been compared to a supported 20% Ni catalyst on Al₂O₃²¹. An 86% methane yield with a selectivity close to 100% was found for the CO₂ hydrogenation reaction over the as prepared Ru based catalyst at 623K while on the as prepared Ni based catalyst a 78% methane yield was measured with a 98% selectivity. Through pretreatment with reaction gas, they reported an increase in the methane yield to 96% on the Ru based catalyst. These results are in line with the reported 89% CO₂ conversion with a methane selectivity close to 100% at 573K and ambient pressure²². To ensure catalyst stability, a 24h performance test was carried out with the Ru/Al₂O₃ catalyst (Sigma Aldrich 206199) at 655K and ambient pressure after reducing the surface with H₂. No performance decline was detected after 24h and the catalyst can be assumed to be stable which is in agreement with the findings in the literature²¹. This makes the Ru/Al₂O₃ catalyst an ideal reference for the present study.

In the following, the results of the CO₂ hydrogenation over Fe, Co, Ni, Cu and Ru/Al₂O₃ will be presented and discussed. Figure 3 shows the CO₂ conversion (XCO₂) over the Ru/Al₂O₃ catalyst as a function of temperature at ambient pressure in relation to the equilibrium CO₂ conversion to CH₄ (YCH₄) and CO (YCO) and the equilibrium methane formation. The selectivity to methane is close to 100% at reaction temperatures up to 600K. After the methane formation becomes thermodynamically limited at around 650K, the selectivity towards CO, thermodynamically favored at higher reaction temperatures, drastically increases. From approximately 650K on, the CO₂ conversion follows the shape of the calculated thermodynamic equilibrium. Prior to that temperature, the reaction is limited by kinetics and diffusion. The thermodynamically maximum conversion is not reached above 650K since the reaction conditions are only quasi equilibrium conditions. The space velocity for the Ru/Al₂O₃ catalyst at a total reactant gas flow of 10ml/min is 5305h⁻¹. Therefore, the equilibrium is more closely approximated with a lower space velocity, which is equivalent to a longer residence time of the reactants in the reactor. To verify this assumption, the CO₂ conversion was measured at five different space velocities at 656K with no He dilution (due to limitations in the possible MFC set points). A clear trend is visible (see Figure 4), which shows that the equilibrium CO₂ conversion (88.2%) is closely approximated at a reactant gas flow of 2.5ml/min (86.2%), while the CO₂ conversion decreases at a flow of 20 ml/min (74.7%) in comparison to the 10ml/min reactant gas flow (76.9%). The space velocity

of the Ru catalysts is larger than for the other metals, since the Ru is nanosized on the surface of the Al_2O_3 and therefore less catalyst mass is required to reach a comparable active surface area.

Figure 3: CO_2 hydrogenation to CH_4 and CO over the Ru/ Al_2O_3 catalyst in relation to the thermodynamic equilibria.

Figure 4: Influence of the space velocity on the CO₂ conversion over Ru/Al₂O₃. The equilibrium is closer approached with decreasing space velocity.

The pristine transition metals were measured in comparable conditions with approximately 1g of catalyst grains mixed with the same weight of glass beads and at a space velocity of approximately 1000h⁻¹. As summarized in Table 1, it was found that methane is the major product on Co and Ni, where the maximum CH₄ yield of 70.2% (at 661K) on Co and 43.8% (at 786K) on Ni is reached. On Fe, carbon monoxide is the main product and the maximum methane yield on Fe is 4.2% at 813K. The methane yield goes through a maximum over Co, Ni and Ru/Al₂O₃, while the conversion keeps increasing on Fe until the maximum temperature measured. This indicates that on Fe the reaction does not reach the thermodynamic equilibrium within the temperature range considered. This is due to the lower reaction rate on Fe generated by limitation of various nature (e.g. lower activity of the catalyst and influence of diffusional limitations). The CO formation on the other hand is thermodynamically favored and the CO yield increases with temperature on all four metals. The highest CO yield on the active catalysts is measured on Fe with 22.4%, Ni 18.2% and Co with 6.9%. On Ru/Al₂O₃, the maximum CO yield is 26.2% at 813K. C₂+ hydrocarbon products were only synthesized on Co, where a maximum C₂H₄ yield of 0.6% was measured at 528K and a C₃H₆ yield of 0.2% yield at 516K (Figure 6). Anyhow,

the C₂+ hydrocarbons formed contribute less than 1% to the overall CO₂ conversion. Cu as pristine metal showed no catalytic activity. We suppose that this is due to the low CO₂ absorption energy on this metal¹⁴.

Figure 5: The CO₂ conversion and Methane yield over Fe, Co and Ni. The difference between the CO₂ conversion (black) and Methane yield (red) equals the CO yield.

Figure 6: C₂H₄ and C₃H₆ formation over Co as function of temperature.

Table 1: Maximal CO₂ conversion, product yields and selectivity on each catalyst. *CO₂ conversion over Cu is similar to empty reactor.

Catalyst	Catalyst mass [g]	Space Velocity	Max CO ₂ conversion		Max CH ₄ yield		Max CO yield		SCH ₄ [%]	SCO [%]
		[h ⁻¹]	T [K]	X[%]	T [K]	Y [%]	T [K]	Y [%]	At XCO ₂ max	
Fe	1.0	1166	813	26.7	813	4.2	813	22.4	15.9	84.1
Co	1.0	965	661	71.2	661	70.2	817	6.9	98.6	1.4
Ni	1.0	956	792	54.7	786	43.8	829	18.2	79.9	20.1
Cu*	1.0	1200	805	58.9	653	1.2	805	58.0	1.6	98.4
Ru/Al ₂ O ₃	0.190	5305	652	74.7	652	73.4	813	26.2	98.8	1.2

3.3. Determination of the kinetic reaction parameters

The activation energy of the CO₂ hydrogenation and CH₄ formation has been determined using the Arrhenius plot of the Turnover Frequency on Fe, Co, Ni and Ru/Al₂O₃.

Turnover Frequency

The Turnover Frequency (TOF) was calculated to compare the CO₂ conversion over the different catalysts in relation to the active surface sites of each catalyst. The TOF of CO₂ over a catalyst relates the number of moles of CO₂ consumed in the reaction to the available active surface sites per time. The TOF is given by:

$$\text{TOF}_{\text{CO}_2} \left[\frac{1}{\text{s}} \right] = \frac{\sum \dot{n}_p}{n_{\text{cat}}} = \frac{n_{\text{CO}_2, \text{in}} \sum Y_p}{n_{\text{cat}}} \left[\frac{1}{\text{s}} \right]$$

where $\dot{n}_p \left[\frac{\text{mol}}{\text{s}} \right]$ is the molar flow of the reaction products, $n_{\text{cat}} [\text{mol}]$ the number of active surface sites, $n_{\text{CO}_2, \text{in}} \left[\frac{\text{mol}}{\text{s}} \right]$ the inflow of CO₂ and Y_p the yield of a reaction product. The number of active surface sites is calculated based on the assumption that the atoms are closest packed at the surface (face centered cubic –fcc and hexagonal close packing- hcp). The TOF is used for the further kinetic analysis of the reaction. The kinetic temperature range of the reaction is determined based on the linearity of the TOF in the Arrhenius plot.

Arrhenius plot

The Arrhenius equation expresses the relation between the reaction rate, the temperature and activation barrier. The Arrhenius equation is

$$k(T) = k_0 e^{\frac{E_a}{RT}}$$

Where k_0 is the pre-exponential factor, E_a the activation energy, R the gas constant, T the reaction temperature, $k(T)$ is the rate constant in units of 1/s. The pre-exponential factor k_0 has the same unit. The exponential term is dimensionless. In the Arrhenius plot, where $\ln(k(T))$ is plotted versus $\frac{1}{T}$, the slope of the curve is $-\frac{E_a}{R}$ and the y-intercept is $\ln(k_0)$.

A major challenge is to identify the kinetically determined reaction temperature. In this range, the curve has a constant slope in Arrhenius plot. This temperature range has to be identified in order to calculate the activation energy and determine the pre-exponential factor of the reaction. If the slope of the curve in the Arrhenius plot is plotted versus the inverse temperature, the kinetically determined reaction range is approximately constant. This temperature range was found to be about 30 K wide for all catalysts. It is 610-640 K for Fe, 480 -510 K for Co, 600 -630 K for Ni and 510 -540 K for Ru/Al₂O₃ (see also Table 2). In these temperature ranges, k_0 and E_a were calculated based on a linear fit to the experimental data points. A very good data correlation was found for all catalysts with $R^2 \geq 0.999$. Figure 7 shows the

different reaction regions on the example of Co. Besides the kinetical limitations, also presumed diffusional and thermodynamic limitations are visible. Diffusional limitations occur if the reaction kinetics is faster than the molecular exchange between reactants and products on the catalyst surface. At higher reaction temperatures, the thermodynamic limitations become predominant. At low temperature (figure 7, region a), the conversion is low and thus the slope of the CO₂ curve is dominated by measurement noise due to the influence of the experimental error.

Figure 7: Slope of the Arrhenius plot of the TOF of the CO₂ conversion over Co versus the inverse temperature. Temperature range a) is the range of low conversion and therefore rich in noise. Section b) is the approximatively linear kinetically determined temperature range, followed by c), the diffusionally -and thermodynamically limited temperature range.

It was found that the observed activation energies on Co, Ni and Ru/Al₂O₃ are in close proximity with 77 kJ/mol for Co, 74 kJ/mol for Ni and 73 kJ/mol for Ru/Al₂O₃. With 50 kJ/mol, Fe has the lowest activation energy. Figure 8 shows the Arrhenius plot for the kinetic temperature range with the linear fit and the experimental data points. Co, Ni and Ru/Al₂O₃ have a comparable slope since their observed activation energies are close. The pre-exponential factor k_0 is calculated from the y- intercept of the Arrhenius plot. The results are shown in Figure 8. It is found that Ru/Al₂O₃ has the highest k_0 (1.5E +

06), followed by Co ($4.2\text{E}+05$) and Ni ($1.0\text{E}+05$). Fe has a k_0 three orders of magnitudes lower than that of Co and Ni. A sensitivity analysis was carried out to investigate the influence of measurement error on the reaction temperature and the determined kinetic reaction range on the activation energy E_a and the frequency factor k_0 . With this analysis it was found that the influence on the activation energy of a temperature error of plus minus 10K is marginal and results in a variation of one to three kJ/mol for the activation energies. The influence of a temperature on k_0 is more pronounced, since k_0 depends exponentially on the y- intercept in the Arrhenius plot, and therefore a small change in the slope of the curve has a significant influence on k_0 . However, the error on k_0 is within the order of magnitude of k_0 for all catalyst and therefore acceptable. The expected errors are indicated in Table 2.

Figure 8: Arrhenius plot with the experimental data of the kinetic temperature range for each catalyst with the extrapolated activation energy plot determined in the kinetic temperature range. The slope of the fitted linear curve is given by $-E_a/R$. The y intercept is $\ln(k_0)$.

Figure 9: Pre-exponential factors for CO₂ conversion on Fe, Ni Co and Al₂O₃ supported Ru .

Table 2: Kinetic temperature range for the determination of the activation energy and the determined activation energy Ea and the pre-exponential factor k₀ for the CO₂ conversion.

Catalyst	Fe	Co	Ni	Ru/Al ₂ O ₃
Kinetic temperature range [K]	610-640 (±10)	480-510 (±10)	600-630 (±10)	510-540 (±10)
Observed Ea [kJ/mol]	50±1	77±3	74±1	73±2
Observed k ₀ [1/s]	(2.7±1)E+02	(4.2±0.6)E+05	(1±0.2)E+05	(1.5±1.5)E+06

Discussion of the Arrhenius parameters E_a and k_0 and catalyst activity

Comparing the activation energies determined in this study to the literature, one sees that the observed activation energy on 0.5wt. % Ru/Al₂O₃ is in good agreement with the values reported in the literature^{18,19,23,24}. The observed activation energy of the CO₂ hydrogenation reaction over Fe determined here, where mainly the RWGS occurs, is also in line with literature values²⁵. Anyway, the literature does not present all the values of the activation energies of the CO₂ hydrogenation reaction on pristine Fe, Co, Ni and Cu. Most of the values of activation energies are reported for supported catalysts and has been shown that the support has a large influence on the activation energy of the CO₂ hydrogenation over Ni supported on SiO₂, Al₂O₃ or TiO₂⁹. The reported activation energies range from 69 kJ/mol for 3wt. % Ni on Al₂O₃ to 97 kJ/mol for an unsupported Ni catalyst. However, these values were not supported with an Arrhenius plot.. In another study¹⁹, the reported activation energies for 15wt. % Fe and Co supported on SiO₂, are 118 kJ/mol for Fe and 93 kJ/mol for Co. a reaction pressure of one bar.

For the Sabatier reaction, the rate constant $k(T)$ calculated from the Arrhenius equation is the apparent rate constant resulting from the difference between the direct and inverse reaction rates. Both of these reaction rates increase with increasing temperature, but the observed kinetic rate decreases with temperature due to the increase in the influence of the thermodynamic equilibrium. This results in an apparent increase of the frequency factor k_0 and in a decrease of the observed activation energy E_a . The reaction activation temperature depends on the reaction conditions. The activation energy and the frequency factor depend on the catalyst. If the catalyst is active for the CO₂ hydrogenation reaction, it provides a path with a lower activation energy compared to the un-catalyzed reaction, thus increasing the rate constant $k(T)$. A higher activation energy results in a greater dependence of the rate constant on the temperature increase. Therefore, the slope of the CO₂ conversion curve as a function of temperature is larger for a higher activation energy. This is in accordance with the experimental findings, where the conversion increases more rapidly on Co, Ni and Ru/Al₂O₃ in comparison to Fe. Furthermore, the similar values of the activation energy over Co, Ni and Ru/Al₂O₃ suggest the presence of a similar mechanism for the reaction on the three catalysts. On the other hand, k_0 expresses the rate constant for an infinite temperature or a reaction without activation (ergo where every reactant collision results in the formation of a product). In practice, k_0 influences the activation temperature of the catalyzed reaction. E.g., if two catalysts with similar activation energies are compared, the catalyst that has a larger k_0 activates at a lower temperature. This is observed for Co and Ni, where Ni activates more than 100K later than Co. However, for the case of Co and Ni, the difference in k_0 (3E+05) is not sufficient to justify this difference of activation temperature. The calculated activation difference based on the Arrhenius parameters is around 20K. The later activation can be explained by the influence of mass transfer limitations at higher temperatures. For 1g of Co and Ni, there are approximately ten times more surface sites available on Co due to the larger specific surface area (Table 1, SI). Therefore, the space velocity of 956h⁻¹, which is globally the same for Co and Ni, is approximately ten times higher

than the available surface sites for Ni, which then results in the later reaction activation of Ni. This interpretation is supported by an experiment, where the activity of 0.1g of Co was compared to 1g of Ni. The 0.1g of Co, which has approximately the same number of available surface sites as 1g of Ni, activated at a higher temperature than 1g of Co, close to the activation temperature of 1g Ni. The thermodynamic influence on the reaction is stronger at elevated temperatures. The Sabatier reaction is still predominant at the temperature of activation of Ni and at the point of maximal conversion, at 792K, results in an increasing shift to the reactant side. Therefore, the later activation of the catalysts results in a limited maximal conversion due to the thermodynamic influence on the reaction. Furthermore, the concentration of the gases has an influence on the observed activation energy. In fact, the absence of He as a carrier gas generates an increase in the observed activation energy to 96 kJ/mol for Co, 91 kJ/mol for Ru/Al₂O₃ and 78 kJ/mol for Ni. This is due to the stronger influence of the reaction hotspot of the exothermic methanation reaction in the non-diluted reaction gas. The effect is less pronounced with Ni, where the observed activation energy increases by only 4 kJ/mol since the influence of the hotspot is weaker at the higher reaction temperature of Ni. The results of the experiments in the absence of helium shows how the temperature management and consequently the determination of the activation energy is a challenging task in a highly exothermal reaction as the CO₂ methanation. He as a diluting agent is used to enable a better temperature control by reducing the reaction hotspot.

These findings lead to the interpretation, that Co, Ni and Ru/Al₂O₃ have comparable abilities to catalyze the CO₂ hydrogenation reaction, while Fe has only little activity in the Sabatier reaction and Cu exhibits no catalytic activity in the CO₂ hydrogenation reaction. The differences between the investigated systems mostly comes from the availability of surface sites, the actual space velocity with respect to the surface sites and the diffusional limitations based on the shape and size distribution of the catalyst.

4. Conclusion

In this study we have investigated the catalytic activity of the pristine transition metal catalysts Fe, Co, Ni, Cu along with the reference system 0.5wt.% Ru supported on Al₂O₃. The experiments were carried out in comparable conditions for all catalysts and were framed with a thermodynamic reaction analysis. With the precise determination of the kinetically limited temperature range, the Arrhenius parameters of the reaction were calculated.

It was found that Co and Ni are the most active catalysts in the CO₂ hydrogenation reaction with a high selectivity to methane. Fe on the other hand was mostly active in the CO formation and therefore in the reverse water gas shift reaction. Cu showed no catalytic activity as a pristine metal.

The kinetically determined reaction range was identified based on a quantitative gas analysis method by means of mass spectrometry. With this method, rapid gas sampling can be achieved and the kinetic reaction range can be identified with high accuracy due to the high density of the data-points.

The activation energies of the reaction were found to be comparable for Co, Ni and Ru/Al₂O₃, suggesting a similar reaction path. A different reaction path presumably occurs for Fe, since both its activation energy and the frequency factor were significantly lower in comparison to the other active catalysts. The space velocity and the availability of active surface sites have a critical influence on the activation temperature of the catalysts, and due to thermodynamic limitations at higher reaction temperatures, on the maximum CO₂ conversion.

With this work we contribute to the better fundamental understanding of the industrially significantly important catalyst building blocks Fe, Co, Ni and Cu. This study sets the basis for further investigations of the reaction kinetics.

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Supplementary information

Catalyst properties

Table 1 SI: Catalyst properties of the as bought catalysts. The nominal size given by the manufacturer is the maximum particle size. By means of SEM image analysis, it was found that the average particle size is smaller than the nominal particle size. By means of BET adsorption isotherms, the specific surface area of the catalysts is determined.

Catalyst	Product Code Goodfellow	Nominal maximal particle size by manufacturer [μm]	Average particle size estimation based on SEM (and TEM for Ru/Al ₂ O ₃) [μm]	Specific surface area determined by means of BET isotherms [m ² g ⁻¹]
Fe	LS461922 I M, CU006024/2	50	20	5.4E-02
Co	LS461922 I M, NI006015/2	45	1	1.1E+00
Ni	LS461922 I M, CO006040/5	45	10	6.9E-02
Cu	LS461922 I M, FE006020/34	60	30	2.8E-02
Ru/Al ₂ O ₃	Sigma Aldrich 206199	Cylindrical pellets Length: 5mm Diameter: 3.2mm	0.0115 (Ru particles only)	6.8E+01 (of the Ru/Al ₂ O ₃)

CO₂ conversion, product yield and selectivity calculation

The mass balance for Carbon in the CO₂ hydrogenation reaction must be fulfilled anytime. Therefore, the number of Carbon atoms in the reactants $n_{C,i}$ must equal the number of Carbon atoms in the products $n_{C,o}$ after the CO₂ hydrogenation reaction.

$$\sum n_{C,in} = \sum n_{C,out}$$

Therefore, the CO₂ conversion X_{CO_2} can then be written as:

$$X_{CO_2} = \frac{n_{CO_2,i} - n_{CO_2,o}}{n_{CO_2,i}} = 1 - \frac{n_{CO_2,o}}{n_{CO_2,i}}$$

$n_{CO_2,i}$ is the molar CO₂ inflow to the reactor and $n_{CO_2,o}$ is the molar outflow. The molar inflow $n_{CO_2,i}$ is known, $n_{CO_2,o}$ must be calculated via the partial pressure of CO₂ in the product gas stream which is measured.

The partial pressure of CO₂ in the product gas stream $p_{CO_2,o}$ is given by the ratio of $n_{CO_2,o}$ to the total number of moles (also species not containing carbon) in the product gas $n_{tot,o}$

$$p_{CO_2,o} = \frac{n_{CO_2,o}}{n_{tot,o}}$$

Depending on the reaction, the total number of moles changes over the course of the reaction. Therefore, $n_{tot,o}$ is not immediately known based on the gas inflow controlled by the MFCs. But with the relation:

$$p_{C,products} = \frac{\sum n_{C,out}}{n_{tot,o}}$$

The relation between $p_{C,products}$ and $p_{CO_2,o}$ can be written as:

$$\frac{p_{CO_2,o}}{p_{C,products}} = \frac{n_{CO_2,o}}{\sum n_{C,out}}$$

Where $p_{C,products}$ is the partial pressure of all carbon containing reaction products.

With this the mass balance

$$n_{CO_2,i} = \sum n_{C,out} + n_{CO_2,o}$$

can be modified to

$$n_{CO_2,i} = \sum n_{C,out} \left(1 + \frac{p_{CO_2,o}}{p_{C,products}}\right)$$

Inserting the found relations to the CO₂ conversion equation, results in an expression based only on the partial pressures of the Carbon containing reaction products and the partial pressure of CO₂ in the product gas stream. The partial pressures can be calculated based on quantitative methods using the mass spectrometer or gas chromatograph.

$$\begin{aligned}
 X_{\text{CO}_2} &= 1 - \frac{n_{\text{CO}_2,0}}{n_{\text{CO}_2,i}} = 1 - \frac{\frac{p_{\text{CO}_2,0}}{p_{\text{C,products}}} * \sum n_{\text{C,out}}}{\sum n_{\text{C,out}} (1 + \frac{p_{\text{CO}_2,0}}{p_{\text{C,products}}})} = 1 - \frac{\frac{p_{\text{CO}_2,0}}{p_{\text{C,products}}}}{1 + \frac{p_{\text{CO}_2,0}}{p_{\text{C,products}}}} \\
 &= 1 - \frac{p_{\text{CO}_2,0}}{p_{\text{C,products}} + p_{\text{CO}_2,0}} = \frac{p_{\text{C,products}}}{p_{\text{C,products}} + p_{\text{CO}_2,0}} \\
 X_{\text{CO}_2} &= \frac{p_{\text{C,products}}}{p_{\text{C,products}} + p_{\text{CO}_2,0}}
 \end{aligned}$$

The reaction yield of Carbon containing products Y_p can be calculated with the CO_2 conversion and the partial pressures $p_{p,i}$ of the individual products.

$$Y_p = X_{\text{CO}_2} * \frac{p_{p,i}}{\sum p_{p,i}}$$

The selectivity S_p for a specific Carbon containing product is given by

$$S_p = \frac{p_{p,i}}{\sum p_{p,i}}$$

Therefore, the CO_2 conversion can also be written as:

$$X_{\text{CO}_2} = \frac{Y_p}{S_p}$$

Turnover frequency calculation

The volume occupied by one particle on the surface is given by

$$V_P[\text{m}^3] = \frac{M_{\text{cat}} \left[\frac{\text{kg}}{\text{mol}} \right]}{\rho_{\text{cat}} \left[\frac{\text{kg}}{\text{m}^3} \right] * N_A \left[\frac{1}{\text{mol}} \right]}$$

The unit cell of one particle is

$$a[\text{m}] = \sqrt[3]{4 * V_T}$$

In average, two particles occupy one -unit cell when for closest packed. Therefore, the surface area occupied by one particle is

$$S_P[\text{m}^2] = \frac{1}{2} a^2 = \frac{1}{2} (4V_T)^{\frac{2}{3}}$$

By multiplying S_P by Avogadro's number, we get the surface area occupied by one mole of catalyst:

$$S_M \left[\frac{\text{m}^2}{\text{mol}} \right] = S_P * N_A$$

$$N_A \left[\frac{1}{\text{mol}} \right] = 6.022 * 10^{23}$$

The surface area is given by the specific surface area and the mass of the catalyst. The active surface sites of the catalyst are therefore

$$n_{\text{cat}} = \frac{m_{\text{cat}}[\text{g}] * a_{\text{s,cat}} \left[\frac{\text{m}^2}{\text{g}} \right]}{S_M \left[\frac{\text{m}^2}{\text{mol}} \right]} [\text{mol}]$$

It is important to note that the number of active sites is linear in the mass of the catalyst

The inflow of CO_2 is $1.5 \frac{\text{ml}}{\text{min}}$ and the molar inlet flow of CO_2 at a pressure of 0.98bar and temperature of 298K is

$$n_{\text{CO}_2,1} = \frac{V_{\text{CO}_2,1} * p}{R * T_{\text{in}}} = 9.8887 \text{e} - 07 \left[\frac{\text{mol}}{\text{s}} \right]$$

Table 2 SI: Catalyst properties to calculate the TOF. For the Ru supported on Al₂O₃, only the mass of Ru is considered for the calculation, since the supporting phase Al₂O₃ is assumed to be covered with Ru.

Catalyst	Fe	Co	Ni	Cu	Ru
Mass [g]	1.005	1.005	1.000	1.005	0.000955
Specific surface area [m ² /g]	5.40E-02	1.09E+00	6.83E-02	2.76E-02	6.77E+01
Molar mass [g/mol]	55.85	58.93	58.69	63.55	101.07
Density [kg/m ³]	7874	8900	8908	8960	12370
Active surface sites [mol]	1.381E-06	2.918E-05	1.826E-06	7.063E-07	1.498E-06