

## First investigation and absolute calibration of clumped isotopes in N<sub>2</sub>O by mid-IR laser spectroscopy

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## ABSTRACT

**Rationale:** Unravelling the biogeochemical cycle of the potent greenhouse gas nitrous oxide (N<sub>2</sub>O) is an underdetermined problem in environmental sciences due to the multiple involved source and sink processes, which complicates mitigation of its emissions. Measuring the doubly isotopically substituted molecules (isotopocules) of nitrous oxide can add new opportunities to fingerprint and constrain its cycle.

**Methods:** We present a laser spectroscopic technique to selectively and simultaneously measure the eight most abundant isotopocules of N<sub>2</sub>O, including three doubly substituted species – so called “clumped isotopes”. For the absolute quantification of individual isotopocule abundances, we propose a new calibration scheme that combines thermal equilibration of a working standard gas with a direct mole fraction-based approach.

**Results:** This method is validated for a large range of isotopic composition values by comparison with other established methods (laser spectroscopy using conventional isotopic scale and isotope-ratio mass spectrometry). Direct intercomparison with recently developed ultra high-resolution mass spectrometry shows clearly advantages of the new laser technique, especially with respect to site specificity of isotopic substitution in the N<sub>2</sub>O molecule.

**Conclusions:** Our study represents a new methodological basis for the measurements of both singly substituted and clumped N<sub>2</sub>O isotopes. It bears a high potential to stimulate future research in the N<sub>2</sub>O community by establishing a new class of reservoir-insensitive tracers and molecular-scale insights.

## INTRODUCTION

Nitrous oxide (N<sub>2</sub>O) is an important greenhouse gas (GHG) and potent ozone-depleting substance, leading to the thinning of the ozone layer. It contributes to human-induced global warming by up to 6 %, <sup>1</sup> and is currently the major substance responsible for the depletion of stratospheric ozone. <sup>2</sup> The mixing ratio of N<sub>2</sub>O in the atmosphere has increased from a preindustrial value of 270 nmol mol<sup>-1</sup> before the year 1750 to (331.1 ± 0.1) nmol mol<sup>-1</sup> in 2018. <sup>3</sup> Anthropogenic activities, primarily the use of fertilizers in agriculture, substantially increase global N<sub>2</sub>O emissions at an even faster rate than

previously estimated by the IPCC emission factor approach.<sup>4</sup> In order to mitigate emissions of this long-lived GHG and reduce the thinning of the ozone layer, its global budget, sinks, and sources need to be well characterized. However, the major sources of N<sub>2</sub>O, such as ocean, soil, use of fertilizers, or biomass burning, exhibit high spatial and temporal variability that are insufficiently constrained. Despite many extensive studies, mitigation of N<sub>2</sub>O emissions remains a great challenge.

Stable isotopic composition of GHGs is a useful proxy for investigating their sources and sinks.<sup>5</sup> N<sub>2</sub>O is a linear asymmetric molecule with three distinct sites for isotopic substitution, i.e. the central ( $\alpha$ ) and terminal ( $\beta$ ) nitrogen (N) atoms, and the oxygen (O) atom. Substitution of <sup>14</sup>N and <sup>16</sup>O by their heavy isotopes <sup>15</sup>N and <sup>17</sup>O or <sup>18</sup>O, respectively, yields in total 12 isotopically substituted molecules or “isotopocules”. Isotopocule is a collective term of more frequently used terms isotopologue (isotopic analogue) and isotopomer (isotopic isomer).<sup>6</sup> In this article, the HITRAN<sup>7</sup> notation as specified in Supplementary Table 1, e.g. 446 for the isotopocule <sup>14</sup>N<sup>14</sup>N<sup>16</sup>O, is used to represent isotopocule designations.

Usually, the distribution of isotopic species in a sample is reported in the  $\delta$  notation:

$$\delta X = \frac{R_{sample}}{R_{ref}} - 1 \quad (1)$$

where X denotes <sup>15</sup>N, <sup>18</sup>O, <sup>15</sup>N <sup>$\alpha$</sup>  (for the isotopocule 456), <sup>15</sup>N <sup>$\beta$</sup>  (546), 458, etc., and R is the ratio of the abundance of a rare and the most abundant isotopic species 446 for a sample and a reference gas.<sup>8</sup> The international isotope ratio scales of nitrogen and oxygen are referred to atmospheric N<sub>2</sub> (Air-N<sub>2</sub>) and Vienna Standard Mean Ocean Water (VSMOW), respectively, with defined primary reference materials and second scale anchors.<sup>9</sup>

The average <sup>15</sup>N content in the N<sub>2</sub>O molecule ( $\delta^{15}\text{N}^{\text{bulk}} = (\delta^{15}\text{N}^{\alpha} + \delta^{15}\text{N}^{\beta})/2$ ) often carries information of nitrogen substrates and reaction kinetics,<sup>10,11</sup> while  $\delta^{18}\text{O}$  and  $\delta^{17}\text{O}$  values are applied e.g. for determining substrate sources.<sup>12,13</sup> Moreover, the covalent bonds between N <sup>$\beta$</sup> –N <sup>$\alpha$</sup>  and N <sup>$\alpha$</sup> –O are distinct in terms of electron distribution and bond strength, which generally makes <sup>15</sup>N substitution favorable at the  $\alpha$  position.<sup>14</sup> The resulting difference in abundances between isotopocules 456 and 546, expressed as  $\delta^{15}\text{N}^{\alpha} - \delta^{15}\text{N}^{\beta}$ , is denoted as site preference (SP)<sup>15</sup> and comprises valuable information on biogeochemical reaction pathways, as SP values are independent of the <sup>15</sup>N isotopic composition of the reaction substrates. Similarly, SP<sup>17</sup> and SP<sup>18</sup> are defined as  $\delta 457 - \delta 547$  and  $\delta 458 - \delta 548$ , respectively.<sup>16</sup> In the past decades, the  $\delta$  values have been used as fingerprints to disentangle production and destruction pathways of N<sub>2</sub>O, but they have shown limitations with resolving multiple dimensions of the processes involved.<sup>17</sup>

It has been suggested that multiply substituted isotopocules, so called “clumped isotopes”, can provide additional constraints for distinguishing the biogeochemical processes cycling N<sub>2</sub>O. Generally, clumping of heavy isotopes in a molecule is thermodynamically favored in an equilibrium process as bonds between heavier isotopes are more stable.<sup>18</sup> Since the extent of clumping is temperature-dependent for equilibrium processes, the abundance of clumped isotopes reflects the formation temperature for the products.<sup>19</sup> This approach has been used mainly in carbonate paleothermometry to study palaeoclimatic and geological processes on Earth.<sup>20</sup> Similarly, N<sub>2</sub>O clumped isotope analysis has the potential to be used for estimating the formation temperature of N<sub>2</sub>O in industrial processes such as nitric acid synthesis (800 – 900 °C), municipal waste combustion (500 – 1000 °C), or catalytic converters (DeNO<sub>x</sub> catalysts, 200 °C).

In addition, clumped isotopes provide unique information about the reversibility of a process,<sup>21</sup> and thus assist in disentangling biogeochemical production pathways, e.g. fungal denitrification<sup>22</sup> and hydroxylamine oxidation,<sup>23</sup> which are largely unresolved with the conventional isotope approaches.

Furthermore, quantum mechanical calculations of ultraviolet absorption cross sections predict fractionation of the clumped  $\text{N}_2\text{O}$  isotopes by its main destruction process, photolysis in the stratosphere.<sup>24,25</sup> In order to trace these processes, e.g. to resolve a difference of 10 °C in formation temperature (at 100 – 200 °C) or to study photolytic  $\text{N}_2\text{O}$  destruction, the instruments need to be capable of detecting changes of  $\delta$  values of less than 1 ‰ in  $\delta 548$  and  $\delta 458$  and 0.1 ‰ in  $\delta 556$ .<sup>18</sup>

The first analysis of the two most abundant clumped isotopic species of  $\text{N}_2\text{O}$ , 458 and 548, has been recently performed by high resolution gas source isotope ratio mass spectrometry (IRMS, type MAT253 Ultra).<sup>16</sup> The reported measurement precision was about 0.10 ‰ for  $\delta^{15}\text{N}^{\text{bulk}}$ ,  $\delta^{17}\text{O}$ ,  $\delta^{18}\text{O}$ , and  $\delta^{15}\text{N}^{\text{a}}$ , and 0.70 to 1.30 ‰ for SP<sup>18</sup> using 10  $\mu\text{mol}$  of pure  $\text{N}_2\text{O}$ . The mass spectrometric techniques have a fundamental limitation in separating molecules with the same mass, e.g. the two isotopomers 458 and 548. For singly substituted isotopic species, this problem can be resolved by analyzing  $\text{NO}^+$  fragment and  $\text{N}_2\text{O}^+$  molecular ions separately. This, however, is complicated by rearrangement of the nitrogen atoms ( $\text{N}^{\text{a}}$  and  $\text{N}^{\text{b}}$ ) in the ion source of the mass spectrometer. The rearrangement, or so called isotope scrambling,<sup>8</sup> requires the implementation of complex correction schemes and increases the uncertainty of the method.

Mid-infrared (mid-IR) laser absorption spectroscopy is a direct method for the site-specific analysis of singly and doubly substituted isotopocules of GHGs. The method is inherently selective, even for molecules with the same mass but different position-specific isotopic substitution (isotopomers), and offers high measurement sensitivity by accessing the strong fundamental rovibrational transitions of the molecules. With the advent of quantum cascade lasers (QCLs), a number of applications have been realized, including high precision isotope ratio measurements for singly substituted isotopocules of  $\text{CO}_2$ ,<sup>26</sup>  $\text{CH}_4$ ,<sup>27</sup> and  $\text{N}_2\text{O}$ .<sup>28</sup> Moreover, laser spectroscopy has been recently applied to clumped isotopes in  $\text{CH}_4$  ( $\text{CH}_3\text{D}$ ,  $\text{CH}_2\text{D}_2$ )<sup>29,30</sup> and  $\text{CO}_2$  ( $^{13}\text{C}^{16}\text{O}^{18}\text{O}$ ).<sup>31,32</sup> However, no spectroscopic method has been developed so far for measuring clumped isotopocules of  $\text{N}_2\text{O}$ .

Here we extend the laser analytical technique towards the selective and simultaneous measurement of the eight most abundant isotopocules of  $\text{N}_2\text{O}$  – the main isotopocule 446, all the singly substituted isotopocules 456, 546, 447, and 448, and three clumped isotopocules 458, 548, and 556 – using a high-resolution dual-laser QCL absorption spectrometer (QCLAS). The assignment of spectral lines is confirmed by standard addition of in-house synthesized pure clumped  $\text{N}_2\text{O}$ . For referencing  $\text{N}_2\text{O}$  isotopocule concentrations to the international isotope ratio scales and stochastic distribution, we developed a new scheme by combining thermal equilibration and mole fraction-calibration. The QCLAS technique shows competitive or superior precision to the currently prevailing high-resolution IRMS and, in addition, offers the advantage of inherent selectivity, real-time data coverage, and capability for on-site operation. Finally, being a non-destructive technique, the samples can be fully recovered for re- or further analysis. This is especially important for applications with limited sample size.

## METHODS

### Selection of spectral regions

To define the wavelength of the lasers to be used in the instrument, the position of spectral lines had to be determined. Supplementary Figure 1 shows the absorption bands of the asymmetric stretching vibration  $\nu_3$  for ten  $\text{N}_2\text{O}$  isotopocules in the spectral region between 2100 and 2260  $\text{cm}^{-1}$ . Data for 446 and singly substituted isotopocules originate from the HITRAN 2012 database.<sup>7</sup> Line positions and line strengths for doubly substituted isotopocules 556, 458, and 548, as well as 457 and 547, have been simulated using the software PGOPHER<sup>33</sup> as these data were not available in any spectral database at the beginning of this work. PGOPHER predicts the effective Hamiltonian of a molecule from rotational and centrifugal distortion constants. These parameters are available in literature for isotopocules 556,

458, 548, 457, and 547 for the ground-state band 0001–0000 (see Supplementary Table 2).<sup>34–36</sup> To verify the PGOPHER simulations, we simulated the line positions of the isotopocules 446, 456, 546, 448, and 447 with the same procedure and compared them with data published in the HITRAN<sup>7</sup> and GEISA<sup>37</sup> databases. The maximal difference between the simulated lines and line positions in the databases is 0.0012 cm<sup>-1</sup>. Thereafter, we selected two spectral ranges at 2142 and 2182 cm<sup>-1</sup> that offer comparable line intensities for all the studied N<sub>2</sub>O isotopocules and no spectral interferences from other major atmospheric trace gases, mainly CO, CO<sub>2</sub>, H<sub>2</sub>O, and CH<sub>4</sub>. Due to their spectral interference with the main isotopocule 446, the isotopocules 457 and 547 cannot be analyzed in the spectral ranges selected for this study.

The simulated line positions of the clumped species were validated using high-purity N<sub>2</sub>O with natural isotopic composition. The gas was incrementally enriched with either pure 458, 548, or 556 N<sub>2</sub>O (synthesized in-house, see below) using a set of mass-flow controllers (red-y MFC; Vögtlin Instruments GmbH, Aesch, Switzerland) to generate a dynamic gas mixture (Supplementary Fig. 2). The concentration of the respective clumped species was increased stepwise to five times their natural isotopic abundance. The spectra were examined for consistency of peak assignment and possible interference effects of allocated and unknown lines of clumped isotopocules on the other analyzed species.

### QCLAS spectrometer

A commercial dual-laser QCLAS instrument (Aerodyne Research Inc., Billerica, MA, USA; QCLAS I) was modified for this study with two QCL sources (Alpes Lasers SA, St-Blaise, Switzerland). Laser 1 operating at 2142 cm<sup>-1</sup> enables simultaneous analyses of isotopocules 446, 456, 546, and 556 (Fig. 1A) and laser 2 emitting at 2182 cm<sup>-1</sup> is used to analyze 548 and 458, and also 446, 447, and 448 (Fig. 1B). The spectrometer is equipped with a 2.5 L volume astigmatic Herriott multi-pass absorption cell. The recorded absorption spectra were fit with a Gaussian-convoluted Voigt profile, taking into account the optical path length (204 m), the gas temperature (290 K) and pressure (4 hPa) in the absorption cell and the laser line width (approx. 0.001 cm<sup>-1</sup>) to retrieve fractional amounts of isotopocules, with the baseline treated as a low-order polynomial. Laser scanning, signal processing, and quantitative spectral fitting are realized with the software TDLWintel (Aerodyne Research, Inc., Billerica, MA, USA). The measured fractional amounts of isotopocules are normalized to the abundance of the species 446. A second, single-laser QCLAS analyzer (Aerodyne Research Inc., Billerica, MA, USA; QCLAS II) operating at 2203 cm<sup>-1</sup> was used for supportive analysis of singly substituted N<sub>2</sub>O isotopocules.<sup>23</sup>

### Synthesis of 556, 458, and 548

For confirmation of line positions and for thermal equilibration experiments, gas samples of pure doubly substituted N<sub>2</sub>O isotopocules 556, 458, and 548 were prepared by thermal decomposition of correspondingly doubly labelled ammonium nitrate salts (NH<sub>4</sub>NO<sub>3</sub>), according to Eq. 2 to 4:<sup>8</sup>

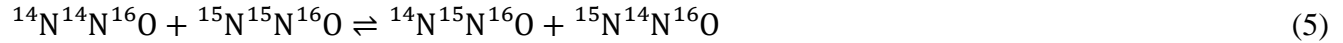


As shown above, the nitrogen atom at the  $\alpha$  position of product  $\text{N}_2\text{O}$  originates from the  $\text{NO}_3^-$  anion, while the  $\beta$  nitrogen comes from the  $\text{NH}_4^+$  cation. Ammonium nitrate  $^{15}\text{NH}_4^{15}\text{N}^{16}\text{O}_3$  (98 %  $^{15}\text{N}$  enrichment) was purchased from Sigma-Aldrich Chemie GmbH (Buchs, Switzerland). Ammonium nitrates labelled with both  $^{15}\text{N}$  and  $^{18}\text{O}$  were not commercially available and were synthesized in-house by first exchanging the oxygen of nitric acid  $\text{HNO}_3$  with  $^{18}\text{O}$ -labelled  $\text{H}_2\text{O}$  (80 %  $^{18}\text{O}$ , Sigma-Aldrich Chemie GmbH, Buchs, Switzerland) and subsequent reaction with  $\text{NH}_3$  to  $\text{NH}_4\text{NO}_3$  using the procedure described in Supplementary Method 1. Experimental details on the thermal decomposition of  $\text{NH}_4\text{NO}_3$  to  $\text{N}_2\text{O}$  are given in Supplementary Method 2.

The isotopic purity of the synthesized gases was tested using a quadrupole mass spectrometer (MKS Instruments, Munich, Germany). The gas decomposed from the commercial  $^{15}\text{NH}_4^{15}\text{N}^{16}\text{O}_3$  contains mainly the isotopocule 556 (95.5 % mass 46 – species 556; 4.4 % mass 45 – species 456 and 546; 0.1 % mass 44 – species 446). Decomposition of the synthesized  $^{14}\text{NH}_4^{15}\text{N}^{18}\text{O}_3$  and  $^{15}\text{NH}_4^{14}\text{N}^{18}\text{O}_3$  salts provided the target 458 (53.6 %) and 548 (54.3 %) isotopocules, respectively, as well as the  $^{16}\text{O}$  labelled isotopocules, 456 (46.4 %) and 546 (45.7 %), respectively. The anticipated presence of residual 456 and 546 is due to the  $^{18}\text{O}/^{16}\text{O}$  content of the used  $^{18}\text{O}$ -labelled water and the exchange equilibrium between  $\text{HNO}_3$  and  $\text{H}_2\text{O}$ . As the natural abundance of 456 and 546 is a factor of 500 higher than the abundance of 458 and 548 (cf. Supplementary Table 1), residual 456 and 546 in the 458 and 548 enriched gases, respectively, do not impair the described applications.

### The $\Delta$ notation for clumped $\text{N}_2\text{O}$

Isotope exchange between the twelve  $\text{N}_2\text{O}$  isotopocules, in accordance with Wang et al.,<sup>18</sup> can be described by eight equilibrium reactions. Eq. 5 provides the equilibrium reaction e.g. between the doubly substituted isotopocule 556 and the most abundant 446, with the equilibrium constant  $K$  (Eq. 6). A formula for computing  $\Delta 556$  (Eq. 7), from  $K$  and  $K^*$  (constant at stochastic composition) can be defined following principles described in the literature; a detailed and illustrative description is provided e.g. by Prokhorov et al. for  $\text{CO}_2$ <sup>38</sup> and Ono et al. for  $\text{CH}_4$ .<sup>29</sup>  $\Delta 458$  and  $\Delta 548$  are derived in like manner.



$$K = \frac{[456][546]}{[446][556]} \quad (6)$$

We define

$$\Delta 556 = -\ln\left(\frac{K}{K^*}\right) = \left(\frac{R556}{R556^*} - 1\right) - \left(\frac{R456}{R456^*} - 1\right) - \left(\frac{R546}{R546^*} - 1\right). \quad (7)$$

$R556$  is the ratio of the abundance of isotopocule 556 relative to 446 in a sample, while  $R556^*$  is the abundance ratio in the same sample gas but with stochastic (random) distribution of isotopes and serves as a reference point.  $R556^*$ ,  $R546^*$ , and  $R456^*$  can be obtained from the total abundance (concentration) of isotopes  $^{14}\text{N}$  and  $^{15}\text{N}$  as given in Eq. 8 to 10, respectively.

$$R556^* = \frac{[556]^*}{[446]^*} = \frac{[^{15}\text{N}]^2[^{16}\text{O}]}{[^{14}\text{N}]^2[^{16}\text{O}]} = \frac{[^{15}\text{N}]^2}{[^{14}\text{N}]^2} \quad (8)$$

$$R456^* = \frac{[456]^*}{[446]^*} = \frac{[^{15}\text{N}]}{[^{14}\text{N}]} \quad (9)$$

$$R546^* = \frac{[546]^*}{[446]^*} = \frac{[^{15}\text{N}]}{[^{14}\text{N}]} \quad (10)$$

In practice, measurements are usually referenced against a working standard gas (*wstd*). In Eq. 11, we exchange  $\Delta 556$  from Eq. 7 by  $\Delta^{556}_{\text{sample/stoch}}$ , and extend the formula in agreement with Werner et al.:<sup>39</sup>

$$\begin{aligned} \Delta^{556}_{\text{sample/stoch}} = & \delta^{556}_{\text{sample/stoch}} - \delta^{456}_{\text{sample/stoch}} - \delta^{546}_{\text{sample/stoch}} = \delta^{556}_{\text{sample/wstd}} - \delta^{456}_{\text{sample/wstd}} - \\ & \delta^{546}_{\text{sample/wstd}} + \Delta^{556}_{\text{wstd/stoch}} + \delta^{556}_{\text{sample/wstd}} \cdot \delta^{556}_{\text{wstd/stoch}} \cdot 10^{-3} - \delta^{456}_{\text{sample/wstd}} \cdot \delta^{456}_{\text{wstd/stoch}} \cdot 10^{-3} - \\ & \delta^{546}_{\text{sample/wstd}} \cdot \delta^{546}_{\text{wstd/stoch}} \cdot 10^{-3} \end{aligned} \quad (11)$$

where  $\delta_{\text{sample/wstd}}$  values are referred to the *wstd* and a correction for a  $\Delta$  value of the *wstd* is applied ( $\Delta^{556}_{\text{wstd/stoch}}$ , Eq. 12). The multiplicative terms  $\delta_{\text{sample/wstd}} \cdot \delta_{\text{wstd/stoch}} \cdot 10^{-3}$  can be ignored for simplicity, which causes a difference of below 0.5 ‰ for samples with natural isotopic abundances but above 1 ‰ for enriched samples. To obtain the  $\Delta_{\text{wstd/stoch}}$  values, the *wstd* has to be analyzed versus the thermally equilibrated working standard ( $\delta_{\text{wstd/eq}}$ ) and then related to its stochastic composition ( $\delta_{\text{eq/stoch}}$ ) using theoretical predictions<sup>18</sup> following the additive theorem for  $\delta$ -notation (used also in derivation of Eq. 11), e.g. for  $\Delta^{556}_{\text{wstd/stoch}}$ :

$$\begin{aligned} \Delta^{556}_{\text{wstd/stoch}} = & \delta^{556}_{\text{wstd/stoch}} - \delta^{456}_{\text{wstd/stoch}} - \delta^{546}_{\text{wstd/stoch}} = \delta^{556}_{\text{wstd/eq}} + \delta^{556}_{\text{eq/stoch}} + \delta^{556}_{\text{wstd/eq}} \cdot \delta^{556}_{\text{eq/stoch}} \cdot \\ & 10^{-3} - (\delta^{456}_{\text{wstd/eq}} + \delta^{456}_{\text{eq/stoch}} + \delta^{456}_{\text{wstd/eq}} \cdot \delta^{456}_{\text{eq/stoch}} \cdot 10^{-3}) - (\delta^{546}_{\text{wstd/eq}} + \delta^{546}_{\text{eq/stoch}} + \delta^{546}_{\text{wstd/eq}} \cdot \\ & \delta^{546}_{\text{eq/stoch}} \cdot 10^{-3}) \end{aligned} \quad (12)$$

### Thermal equilibration

For the thermal equilibration, a natural abundance  $\text{N}_2\text{O}$  (99.999 %, Messer Schweiz AG, Switzerland) was spiked with one of the three in-house synthesized doubly substituted  $\text{N}_2\text{O}$  isotopocules (556, 458, or 548) to 50 % above their natural abundance, in order to trace the progress of equilibration in time. 250  $\mu\text{mol}$  of the spiked  $\text{N}_2\text{O}$  gas was flame-sealed into a quartz-glass tube (outer diameter 9 mm, length 220 mm) that was filled with 400 mg of aluminium oxide (activated, neutral, type Brockmann I; Sigma-Aldrich Chemie GmbH, Buchs, Switzerland) and topped with silanized glass wool (Sigma-Aldrich Chemie GmbH, Buchs, Switzerland). Before introducing  $\text{N}_2\text{O}$ , the catalyst was heated in the tube attached to a vacuum line with propane flame until the pressure in the system dropped below 0.3 hPa. After filling with  $\text{N}_2\text{O}$  and flame-sealing, the tubes were placed into a muffle furnace for a specified time. The equilibration experiments were done at 100 °C (55 – 790 hours), 200 °C (2.5 – 116 hours), 300 °C (16 hours), 400 °C (20 hours), and 500 °C (46 – 240 hours) with all three spiked  $\text{N}_2\text{O}$  gases. Equilibration at 100 °C was initiated by heating at 200 °C for 14 – 16 hours before the temperature was decreased to 100 °C.<sup>16</sup> After the respective time period at the equilibration temperature, the tubes were taken out of the furnace and quenched immediately in a cold pressurized air flow. The gases were then purified on the vacuum line where  $\text{N}_2\text{O}$  was condensed at 77 K (liquid  $\text{N}_2$ ), while  $\text{N}_2$  and  $\text{O}_2$  were removed by evacuation with an oil sealed rotary vane pump. The purified equilibrated  $\text{N}_2\text{O}$  gases were analyzed by QCLAS I in triplicate versus the unequilibrated gas mixtures to investigate the progress of equilibration. A single-point offset correction scheme on  $\delta$  values was applied, as no second calibration gas with known isotopic composition for clumped isotopocules was available at that point in time.

The data was fitted using exponential functions – for  $\delta^{456}$  and SP, the saturation function  $y = a \cdot (1 - e^{-x/b})$  was used, where  $y$  is  $\delta^{456}$  or SP value,  $a$  is a saturation value at long times (in ‰),  $x$  is the equilibration time ( $t_{eq}$  in Fig. 2), and  $b$  is a time constant of the saturation (in hours). For  $\delta^{546}$  and  $\delta(\text{spike})$ , the decay function  $y = a \cdot (e^{(-x/b)}) + c$  was applied, where  $y$  is  $\delta^{546}$  or  $\delta(\text{spike})$  value,  $a$  and  $c$  are intercepts (in ‰),  $x$  is the equilibration time, and  $b$  is a time constant of the decay (in hours).

## Combined mole fraction-calibration scheme

The new reference frame for N<sub>2</sub>O isotopocules was established by combining thermal equilibration and mole fraction-calibration. In a first step, mole fractions of the clumped species in the *wstd* gas (high purity N<sub>2</sub>O, 99.999 %, PanGas – The Linde Group, Dagmersellen, Switzerland) were obtained. In order to do so,  $\delta^{458}_{wstd/eq}$ ,  $\delta^{548}_{wstd/eq}$ , and  $\delta^{556}_{wstd/eq}$  values were retrieved by analysis of the *wstd* against the equilibrated *wstd* gas.  $\delta$  values for the singly substituted N<sub>2</sub>O isotopocules of the working standard were determined by QCLAS II against reference gases, previously anchored to the international isotope ratio scales by Sakae Toyoda at Tokyo Institute of Technology (Yokohama, Japan).<sup>8</sup> These values were used as input variables for theoretical predictions of  $\delta_{eq/stoch}$ .<sup>18</sup> Detailed description is provided in section Results (Clumped isotope calibration strategies, part B).

In a second step, a set of seven high-accuracy gravimetric mixtures of the N<sub>2</sub>O working standard in N<sub>2</sub> (purity 99.9999 %) was prepared by the National Physical Laboratory (NPL, Teddington, UK). The concentration of the calibration gases (CGs) ranges from 1.50 to 1.85 % N<sub>2</sub>O in N<sub>2</sub> (CG1 – CG7; Supplementary Table 3) to bracket the expected enrichment or depletion of individual isotopocules in natural samples (Supplementary Table 4). Production of the CGs at NPL included the preparation of an intermediate gravimetric mixture of 12 % N<sub>2</sub>O in N<sub>2</sub> that was consecutively diluted to the target N<sub>2</sub>O mole fractions of CG1 – CG7 (Supplementary Table 3). The N<sub>2</sub>O mole fractions of the CGs were validated by an additional gravimetric dilution to 325 nmol mol<sup>-1</sup> in synthetic air and subsequent analysis against NPL in-house standards by cavity ring-down spectroscopy (G5131 I; Picarro Inc., Santa Clara, CA, USA). Possible fractionation effects during production of the CGs were excluded by analysis of CG1 – CG7 by QCLAS II against reference gases anchored to the international scales.<sup>8</sup> Prior to analysis, all gases were diluted to 100  $\mu\text{mol mol}^{-1}$  N<sub>2</sub>O in synthetic air (20.5 % O<sub>2</sub> in N<sub>2</sub>; Messer Schweiz AG, Lenzburg, Switzerland). The isotopic standards used by QCLAS II for the analysis of the CGs and their original pure N<sub>2</sub>O gas were: (1)  $\delta^{15}\text{N}^{\alpha} = (2.06 \pm 0.05) \text{‰}$ ;  $\delta^{15}\text{N}^{\beta} = (1.98 \pm 0.20) \text{‰}$ ;  $\delta^{18}\text{O} = (36.12 \pm 0.32) \text{‰}$ ; and (2)  $\delta^{15}\text{N}^{\alpha} = (-48.59 \pm 0.25) \text{‰}$ ;  $\delta^{15}\text{N}^{\beta} = (-46.11 \pm 0.43) \text{‰}$ ;  $\delta^{18}\text{O} = (27.37 \pm 0.11) \text{‰}$ . The standards used for the analysis of the VG1 and its original pure N<sub>2</sub>O gas were: (1)  $\delta^{15}\text{N}^{\alpha} = (25.73 \pm 0.24) \text{‰}$ ;  $\delta^{15}\text{N}^{\beta} = (25.44 \pm 0.36) \text{‰}$ ;  $\delta^{18}\text{O} = (35.86 \pm 0.22) \text{‰}$ ; and (2)  $\delta^{15}\text{N}^{\alpha} = (-48.59 \pm 0.25) \text{‰}$ ;  $\delta^{15}\text{N}^{\beta} = (-46.11 \pm 0.43) \text{‰}$ ;  $\delta^{18}\text{O} = (27.37 \pm 0.11) \text{‰}$ . The uncertainty is expressed as expanded standard uncertainty at the 95 % confidence interval.

Analytical results by QCLAS II for the pure working standard agree with  $\delta$  values of CG1 – 7 (cf. Supplementary Table 3) within their expanded uncertainty limits, which demonstrates that no significant isotopic fractionation was introduced during the gas mixture preparation by NPL. For the clumped isotopocules, similar behavior, i.e. the absence of fractionation effects during preparation of CG1 – CG7, is assumed. Therefore,  $\delta$  values of the pure working standard were applied for all gas mixtures in the mole fraction-calibration scheme.

## Validation of the N<sub>2</sub>O reference frame

In order to validate the new reference frame, two validation strategies were applied: (1) a gravimetric gas mixture with 1.53 % N<sub>2</sub>O (gas VG1) with different isotopic composition was produced by NPL using a similar strategy as described above for the calibration gases; (2) three validation gases (VG2,

VG3, VG4) were thermally equilibrated in triplicate at 100 and 200 °C and purified according to the previously described procedure. The preparation of VG2, VG3, VG4 from pure, commercially available N<sub>2</sub>O by volumetric doping with defined amounts of isotopically pure (> 98 %) <sup>14</sup>N<sup>15</sup>N<sup>16</sup>O (NLM 1045 PK), <sup>15</sup>N<sup>14</sup>N<sup>16</sup>O (NLM 1044 PK) (Cambridge Isotope Laboratories, Tewksbury, MA, USA) and <sup>14</sup>N<sup>14</sup>N<sup>18</sup>O (in-house synthesized) using a ten port two position valve (EH2C10WEPH with 20 mL sample loop, Valco Instruments Inc., Schenkon, Switzerland) and synthesis of <sup>14</sup>N<sup>14</sup>N<sup>18</sup>O are described elsewhere.<sup>40</sup>

The measurement sequence applied during the validation experiments was initiated by analysis of CG1, CG5, and CG7 followed by triplicate analysis of a sample and final repeated analysis of CG1, CG5, and CG7. Average values for the CGs were used for the calibration, which reduces also potential drift between the analysis of CGs and the sample. The full sequence was repeated five times for VG1 and once for all three subsamples of VG2 – VG4 equilibrated individually.

### High-resolution mass-spectrometric measurements

The isotopic composition of the equilibrated samples VG2, VG3, and VG4 was also determined by high resolution isotope ratio mass spectrometry with a MAT253 Ultra (Thermo Scientific, Bremen, Germany, here labelled as HR-IRMS) at Tokyo Institute of Technology (Yokohama, Japan). The measurement was made using previously published methods for site specific <sup>15</sup>N analysis and clumped isotope analysis.<sup>16</sup> The method consists of three separate analyses of NO<sup>+</sup> fragment ions and N<sub>2</sub>O<sup>+</sup> molecular ions of the singly and doubly substituted isotopocules, all performed at mass resolutions of approx. 16,000 – 19,000 using a 16 µm slit (middle resolution). For each set of measurements, the detectors were positioned such that the flat tops of every peak of interest were aligned. All measurements were made in dual-inlet mode. Every sample and standard intensity comparison (‘acquisition’) was composed of 8 cycles with 8 s integration time for each individual measurement. The measurement was performed with 9.9 kV accelerating voltage, filament emission current of 1.65 mA, and equilibration time of 35 s. Before each acquisition, a series of 500 s background scans was collected for both sample and reference gases. More information is available in Supplementary Method 3. The Δ values provided by HR-IRMS were referenced to a working standard used at Tokyo Institute of Technology ( $\delta^{15}\text{N}^{\alpha} = (-4.07 \pm 0.06) \text{‰}$ ,  $\delta^{15}\text{N}^{\beta} = (-0.02 \pm 0.14) \text{‰}$ ,  $\delta^{18}\text{O} = (20.63 \pm 0.12) \text{‰}$ ). The uncertainty is expressed as expanded standard uncertainty at the 95 % confidence interval. As the  $\Delta_{\text{wstd/stoch}}$  was not known, no correction to stochastic distribution for the doubly substituted species 458 and 548 could be applied. Instead, a correction based on Eq. 29 was applied.

## RESULTS

### Spectral regions and analysis

The spectral ranges for the eight most abundant N<sub>2</sub>O isotopocules were identified using PGOPHER simulations<sup>33</sup> in combination with spectral data from the database HITRAN.<sup>7</sup> Two distinct spectral windows at 2142 and 2182 cm<sup>-1</sup> (Fig. 1A for laser 1 and Fig. 1B for laser 2, respectively) were selected, offering comparable line intensities for all the studied N<sub>2</sub>O isotopocules and having no spectral interferences from other major atmospheric trace gases. Spectral simulations indicate that the absorption of the interferents is below 1 ‰ of N<sub>2</sub>O absorption (for 1 % N<sub>2</sub>O) up to 30 ppm CO, 2000 ppm CO<sub>2</sub>, 6 % H<sub>2</sub>O, 5 % CH<sub>4</sub>, and 15 ppm O<sub>3</sub>. The line parameters for the spectroscopic measurements using the dual-laser QCLAS (further denoted as QCLAS I) are given in Supplementary Table 5.

The line positions simulated for the clumped species were validated with a number of standard addition experiments. For this, N<sub>2</sub>O of natural isotopic composition was supplemented with either synthesized pure 458, 548, or 556 species (Supplementary Fig. 2). Based on these experiments, the

calculated absorption lines of clumped species were confirmed in both spectral regions. In addition, one previously unknown line of the 458 isotopocule was identified at 2142.647 cm<sup>-1</sup>.

### Optimized experimental conditions and achieved precision

The sensitivity of the QCLAS can be enhanced by increasing the absorption signal, i.e. improving the signal-to-noise ratio either by using higher pressure or increasing the amount fraction of the absorbing molecules. For isotope ratio analysis, however, it is equally important to achieve excellent selectivity and minimize spectral interferences. Generally, low cell pressure is beneficial as it reduces the pressure broadening of absorption lines and thereby interferences between adjacent spectral lines or molecular transitions. This is of particular importance for laser 2, where a strong neighboring line of 446 at 2182.670 cm<sup>-1</sup> (outside of the plotted range in Fig. 1B) with a spectral line intensity of 1.064·10<sup>-19</sup> cm<sup>-1</sup>/(molecule cm<sup>-2</sup>) affects the baseline with increasing pressure. Therefore, experimental conditions for QCLAS I, especially the minimal required amount of N<sub>2</sub>O and pressure in the optical cell, were optimized. Figure 3A indicates that the best Allan precision<sup>41</sup> for δ548 with 1 s spectral averaging can be achieved with 3 – 4 μmol of N<sub>2</sub>O irrespective of the applied cell pressure (between 1 and 7 hPa) and matrix gas (He, N<sub>2</sub>). Similarly, the best precision for δ458 and δ556 was reached with 5 and 7 μmol of N<sub>2</sub>O, respectively.

Thus, the optimal measurement conditions were selected: cell pressure of 4 hPa using approx. 4 μmol of N<sub>2</sub>O in a N<sub>2</sub> gas matrix. Under these conditions, a precision of < 0.40 ‰ for δ548, 0.20 – 0.30 ‰ for δ556, 0.10 – 0.20 ‰ for δ458, δ448, δ447, and 0.10 ‰ for δ456 and δ546 (Fig. 3B and 3C) was achieved for integration times of 600 – 1000 s for laser 1 and of 30 – 100 s for laser 2, respectively. The precision was derived from the square root of the Allan variance.

### Clumped isotope calibration strategies

An often underestimated challenge of clumped isotope ratio measurements is the construction of a primary reference scale, which has not been set up so far for clumped N<sub>2</sub>O isotope analysis. We implemented two alternative, independent approaches: (A) to equilibrate a gas mixture at selected temperatures to adjust clumped isotopocule abundances,<sup>18</sup> (B) to calibrate individual isotopocule mole fractions using high accuracy gravimetric mixtures,<sup>42,43</sup> which are described in detail below. The first approach follows principles of statistical thermodynamics in order to evaluate the equilibrium constants of isotope exchange reactions (e.g. Eq. 5) and to calculate the proportions of all isotopocules that are consistent with the bulk isotopic composition.<sup>18</sup> Abundances of clumped isotopocules deviate from the stochastic distribution as a function of temperature (1/T), which is the basis of their use as geothermometers. In return, this is the standard technique for calibration in clumped isotope science.

However, for N<sub>2</sub>O the equilibration approach has some limitations, e.g. only small sample volumes can be equilibrated, and equilibration succeeds only in a limited temperature range. At the low temperature side, extensive hold times are required, while at higher temperatures thermal decomposition occurs. The second calibration approach, developed for optical analyzers, overcomes these limitations as high-pressure cylinders with calibration gases can be prepared, and a single N<sub>2</sub>O isotopic quality diluted to different mole fractions enables multi-point calibration. However, as a requirement, N<sub>2</sub>O gas with defined abundances of clumped isotopocules is required. In the presented study, we combine the advantages of both approaches: we use the thermal equilibration to provide a reference point for the abundance of clumped isotopocules, and we propagate this information to N<sub>2</sub>O gas applied in the mole-fraction based calibration scheme.

#### A) Thermal equilibration of N<sub>2</sub>O

Firstly, N<sub>2</sub>O was thermally equilibrated using high-surface-area alumina (Al<sub>2</sub>O<sub>3</sub>) following Magyar et al.<sup>16</sup> and the results were compared to the theoretical predictions of Wang et al.<sup>18</sup> Three mixtures of high-purity N<sub>2</sub>O, each mixture spiked with only one of the in-house synthesized pure clumped species (458, 548, or 556) to 50 % above natural abundance, were used to validate the equilibration procedure and to optimize experimental conditions.

Complete thermal equilibration of N<sub>2</sub>O was confirmed for the first two spiked gas mixtures after 48 hours at 200 °C and after 180 hours at 100 °C by the disappearance of the respective clumped isotopocule enrichment (Fig. 2A and 2B), while the 556 spike remained unchanged (Fig. 2C). Additionally, thermodynamic equilibrium of the N–O bond is indicated by the emergence of a stable difference in the <sup>15</sup>N substitution between  $\alpha$  and  $\beta$  position, i.e. stable SP and SP<sup>18</sup>. Figure 2D shows the change of SP during the equilibration experiments and confirms equilibration of the N–O bond in all three spiked gas mixtures. Exponential fitting of the data result in average time constants (*e*-folding times) for  $\delta 456$  of (20.55  $\pm$  9.68) h at 100 °C and (3.49  $\pm$  0.58) h at 200 °C, and for  $\delta 546$  of (25.25  $\pm$  14.09) h at 100 °C and (2.80  $\pm$  0.90) h at 200 °C, respectively.

The <sup>15</sup>N substituted isotopocules in the equilibrated gases were additionally analyzed using a single-laser QCLAS system (further denoted as QCLAS II) with reference to the Air-N<sub>2</sub> scale provided by the Tokyo Institute of Technology<sup>8</sup> (Table 1). A good agreement in SP was found between the two spectroscopic techniques but, in particular for gases equilibrated at 100 °C, experimental results show 4 – 5 ‰ deviation from theoretical predictions.

#### B) Calibration based on individual isotopocule mole fractions

A second calibration strategy, recently suggested for singly substituted isotopocule analysis by infrared optical analyzers,<sup>42,43</sup> was modified for the clumped N<sub>2</sub>O isotopes. This approach, which relies on high-accuracy gravimetric calibration gases, is based on the calibration of individual isotopocule mole fractions rather than conventional calibration of isotopocule ratios or  $\delta$  values. The  $\delta$  values of the calibration gases (CGs; NPL, Teddington, UK) for singly substituted isotopic species were assigned against international isotope ratio scales by QCLAS II.  $\delta_{\text{wstd/stoch}}$  values of doubly substituted isotopic species were derived from the analysis of the *wstd* against the same gas that was thermally equilibrated at 200 °C and relating it to stochastic distribution following Eq. 12. This step signifies the essential connection between the two calibration strategies. Based on the Eq. 12 and the thermal equilibration experiments,  $\Delta_{\text{wstd/stoch}}$  values were determined as:  $\Delta_{\text{wstd/stoch}}^{458} = (-0.06 \pm 0.80) \text{ ‰}$ ,  $\Delta_{\text{wstd/stoch}}^{548} = (0.49 \pm 0.46) \text{ ‰}$ ,  $\Delta_{\text{wstd/stoch}}^{556} = (-0.88 \pm 1.76) \text{ ‰}$  (expanded uncertainties at the 95 % confidence interval, propagated from standard error of the mean for repeated measurement of all  $\delta$  values in Eq. 12, N=9).

In order to set up the mole fraction-calibration scheme, ratios of individual singly substituted isotopocules R456, R546, R447, and R448 were calculated from  $\delta$  values of the CGs, e.g.:

$$R456 = R_{\text{N}_2\text{-AIR}}^{15} (1 + \delta^{15}\text{N}^{\alpha}) \quad (13)$$

$$R447 = R_{\text{VSMOW}}^{17} (1 + \delta^{18}\text{O})^{\lambda} \quad (14)$$

where  $R_{\text{Air-N}_2}^{15}$ ,  $R_{\text{VSMOW}}^{17}$ , and  $R_{\text{VSMOW}}^{18}$  are <sup>15</sup>N/<sup>14</sup>N, <sup>17</sup>O/<sup>16</sup>O, and <sup>18</sup>O/<sup>16</sup>O ratios of tropospheric N<sub>2</sub> (Air-N<sub>2</sub>) and VSMOW, respectively, and  $\lambda$  is the mass-dependent factor that relates differences in <sup>17</sup>O and <sup>18</sup>O abundances.<sup>39</sup> Ratios of doubly substituted isotopocules R458, R548, and R556 were derived from  $\delta$  values of the *wstd* normalized against stochastic distribution (obtained by thermal equilibration experiments based on Eq. 12), e.g.:

$$R_{548} = R_{\text{stoch}}^{548} (1 + \delta_{\text{wstd/stoch}}^{548}) \quad (15)$$

where  $R_{\text{stoch}}^{548}$  is the ratio of 548 over 446 in the working standard with stochastic distribution of isotopes. Then, atomic isotopic abundances were calculated following Eq. 16 – 22:

$$X(^{14}\text{N}, \alpha) = \frac{1}{1+R_{456}} \quad (16)$$

$$X(^{15}\text{N}, \alpha) = \frac{R_{456}}{1+R_{456}} \quad (17)$$

$$X(^{14}\text{N}, \beta) = \frac{1}{1+R_{546}} \quad (18)$$

$$X(^{15}\text{N}, \beta) = \frac{R_{546}}{1+R_{546}} \quad (19)$$

$$X(^{16}\text{O}) = \frac{1}{1+R_{447}+R_{448}} \quad (20)$$

$$X(^{17}\text{O}) = \frac{R_{447}}{1+R_{447}+R_{448}} \quad (21)$$

$$X(^{18}\text{O}) = \frac{R_{448}}{1+R_{447}+R_{448}} \quad (22)$$

Using the atomic isotopic abundances and the  $\text{N}_2\text{O}$  mole fractions ( $x_{\text{N}_2\text{O}}$ ), mole fractions of isotopocules in the CGs  $x_{446}$ ,  $x_{456}$ ,  $x_{546}$ ,  $x_{447}$ , and  $x_{448}$  were derived, e.g.:

$$x_{446} = [X(^{14}\text{N}, \alpha) \cdot X(^{14}\text{N}, \beta) \cdot X(^{16}\text{O})] \cdot x_{\text{N}_2\text{O}} \quad (23)$$

$$x_{456} = [X(^{14}\text{N}, \alpha) \cdot X(^{15}\text{N}, \beta) \cdot X(^{16}\text{O})] \cdot x_{\text{N}_2\text{O}} \quad (24)$$

For the clumped isotopocules, the ratios  $R_{458}$ ,  $R_{548}$ , and  $R_{556}$  obtained following Eq. 15 were converted to mole fractions  $x_{458}$ ,  $x_{548}$ , and  $x_{556}$ , e.g.:

$$x_{548} = R_{548} \cdot x_{446} \quad (25)$$

Calculated ( $x_{\text{xyz}}$ ) and analyzed ( $y_{\text{xyz}}$ ) mole fractions of isotopocules in the CGs were used to derive in total 9 linear calibration functions (laser 1 – species 446, 456, 546, 556; laser 2 – species 447, 448, 446, 548, 458) in accordance with Flores et al.<sup>43</sup> Slope  $a$  and intercept  $b$  of the linear calibration functions were retrieved by linear regression and used to calculate isotopocule mole fractions in a sample gas ( $x_{\text{xyz,sam}}$ ) from the corresponding calibration equation:

$$x_{\text{xyz,sam}} = \frac{y_{\text{xyz,sam}} - b}{a} \quad (26)$$

where  $y_{\text{xyz,sam}}$  is the mole fraction of an isotopocule  $\text{xyz}$  in a sample measured by QCLAS I (Supplementary Fig. 3). Finally, the mole fractions  $x_{\text{xyz,sam}}$  were used to calculate  $\delta$  values in a sample related to the international isotope ratio scales or stochastic distribution, e.g.:

$$\delta_{456} = \frac{\frac{x_{456,\text{sam}}}{x_{446,\text{sam}}}}{R_{\text{N}_2-\text{AIR}}^{15}} - 1 \quad (27)$$

$$\delta_{548} = \frac{\frac{x_{548,\text{sam}}}{x_{446,\text{sam}}}}{R_{\text{N}_2-\text{AIR}}^{15} \cdot R_{\text{VSMOW}}^{18}} - 1 \quad (28)$$

### Validation and uncertainty assessment of the combined mole fraction-calibration scheme

Detailed validation and uncertainty assessment were conducted for the combined mole fraction-calibration scheme described above. At first,  $\delta$  values for singly substituted isotopocules analyzed by QCLAS I for a high-accuracy gravimetric validation gas VG1 were compared to values provided by an established analytical approach using QCLAS II with the conventional  $\delta$ -calibration (Table 2, upper part – VG1). The differences between the values assigned by QCLAS I and II, calculated as  $\Delta_{\text{I-II}} = \delta_{\text{QCLAS I}} - \delta_{\text{QCLAS II}}$ , were:  $\Delta^{456}_{\text{I-II}} = (-0.29 \pm 0.55) \text{ ‰}$ ,  $\Delta^{546}_{\text{I-II}} = (-0.53 \pm 0.64) \text{ ‰}$ ,  $\Delta^{448}_{\text{I-II}} = (1.21 \pm 0.64) \text{ ‰}$ . The larger difference in  $\Delta^{448}_{\text{I-II}}$  is caused by an underestimation of  $\delta^{18}\text{O}$  by QCLAS II, as  $\delta^{18}\text{O}$  of VG1 lies outside the  $\delta^{18}\text{O}$  range of available standard gases for QCLAS II. This was already observed earlier<sup>44</sup> and is confirmed by  $\delta^{18}\text{O}$  analysis of VG1 by IRMS at Max Planck Institute for Biogeochemistry (Jena, Germany; Table 2,  $\Delta^{448}_{\text{I-IRMS}} = (-0.83 \pm 0.51) \text{ ‰}$ ). The uncertainty is expressed as the expanded standard uncertainty at the 95 % confidence interval.

In a second validation approach,  $\text{N}_2\text{O}$  gases with no (VG2), strong (50 ‰, VG3) and very strong (100 ‰, VG4) enrichment in the singly substituted isotopocules 456, 546, and 448 were thermally equilibrated at 100 and 200 °C. As a part of the validation, the gases were measured by the presented QCLAS I and also by the competitor high-resolution IRMS instrument (MAT253 Ultra, Tokyo Institute of Technology, Tokyo, Japan; denoted as HR-IRMS onwards). Thereby, the linearity of both instruments over a wide range of  $\delta^{15}\text{N}^{\text{bulk}}$  and  $\delta^{18}\text{O}$  values was intercompared. Moreover, results for equilibrated VG2, VG3, and VG4 at 200 °C by QCLAS I and HR-IRMS analyses were compared to theoretical predictions (Table 2 and Fig. 4). The theoretical predictions were computed based on equilibrium thermodynamics<sup>18</sup> and the known bulk isotopic compositions of the gases (listed in Methods). As the reference gas used by HR-IRMS was not isotopically characterized for the content of the doubly substituted species, the measured values  $\delta^{458}$  and  $\delta^{458+548}$  at 200 °C for HR-IRMS were referenced to the ratio between the measured and the theoretical  $\delta$  values at 100 °C:

$$\delta^{458} = \left( \frac{\left( \frac{\delta_{\text{measured},200^\circ\text{C}}^{458}}{1000} + 1 \right)}{\left( \frac{\delta_{\text{measured},100^\circ\text{C}}^{458}}{1000} + 1 \right)} \left( \frac{\delta_{\text{theory},100^\circ\text{C}}^{458}}{1000} + 1 \right) - 1 \right) \cdot 1000. \quad (29)$$

$\Delta^{458+548}_{\text{avg}}$  and  $\text{SP}^{18}$  presented in Table 2 and Fig. 4 for HR-IRMS were calculated from  $\delta^{458}$  and  $\delta^{458+548}$  values corrected as described in Eq. 29.

Results indicate that the QCLAS I and HR-IRMS reach a similar precision for  $\delta^{15}\text{N}^{\text{bulk}}$  and  $\delta^{458+548}_{\text{avg}}$ , in the range of 0.31 – 0.45 ‰ and 0.49 – 0.56 ‰ (QCLAS I), and 0.14 – 0.15 ‰ and 0.46 – 0.97 ‰ (HR-IRMS), respectively. The precision was expressed as standard deviation for repeated analyses within one measurement run. The average accuracy of QCLAS I and HR-IRMS results of  $\delta^{15}\text{N}^{\text{bulk}}$  and  $\delta^{458+548}_{\text{avg}}$  values, with respect to theoretical predictions, is 0.28 and 3.84 ‰ (QCLAS I), and 1.50 and

1.92 ‰ (HR-IRMS), respectively. The accuracy was calculated as average difference between the measured and the theoretical value.

The repeatability of QCLAS I results for  $\delta^{15}\text{N}^{\text{bulk}}$  and  $\delta^{458+548}_{\text{avg}}$  values is 0.14 – 0.20 ‰ and 0.22 – 0.25 ‰, respectively. For HR-IRMS results, it is 0.06 ‰ and 0.19 – 0.40 ‰ for  $\delta^{15}\text{N}^{\text{bulk}}$  and  $\delta^{458+548}_{\text{avg}}$  values, respectively. The repeatability was calculated as standard deviation of the mean from multiple measurement sequences (see Table 2 for details). There is a clear trend in the  $\Delta^{458+548}_{\text{avg}}$  with increasing  $^{15}\text{N}$  and  $^{18}\text{O}$  enrichment (Table 2) for both QCLAS I and HR-IRMS (without the additional referencing by Eq. 29), which could be due to a scale expansion. For laser spectroscopy, this can be caused by the presence of weak absorption lines of either 456, 546, or 448 beneath the 458 and 548 lines, or by incomplete thermal equilibration of oxygen atoms between different  $\text{N}_2\text{O}$  molecules that gets hindered by some so far unknown mechanism.

Regarding site-selectivity, i.e. the difference in abundances between isotopomers 456 versus 546 and 458 versus 548, expressed as SP and  $\text{SP}^{18}$  (Fig. 4B and 4D, respectively, and Table 2), the average accuracy (deviation from the theoretical value) is 1.62 and 4.26 ‰ for QCLAS I but as high as 3.95 and 10.39 ‰ for HR-IRMS, respectively. This indicates that the measurement of  $\text{SP}^{18}$  remains a challenge for the IRMS technique, as the HR-IRMS instrument used in this study could not accurately distinguish the two isotopomers 458 and 548 from each other. The repeatability of SP and  $\text{SP}^{18}$  provided by QCLAS I is in the ranges 0.28 – 0.40 ‰ and 0.44 – 0.50 ‰, respectively. For values obtained by HR-IRMS, it is 0.11 ‰ and 0.37 – 0.79 ‰, respectively. The above results do not include equilibration at 100 °C because of the lower consistency in those results compared to 200 °C, which may be due to incomplete isotope-exchange equilibrium.

In accordance with Flores et al.,<sup>43</sup> the uncertainty of the isotope ratio ( $R$ ) for a sample gas derived using the combined mole fraction-calibration scheme was estimated from a model equation (Eq. 25; Supplementary Table 6). Taking  $R_{548}$  as an example, the uncertainty of the isotopocule (548, 446) mole fractions ( $x$ ) of a sample gas is derived from the analytical uncertainty of the analyzed mole fractions ( $y_{548}$ ,  $y_{446}$ ) and the uncertainty in the slope  $a$  and the intercept  $b$  of the calibration function. The uncertainty contributions of the latter are derived from the reference values of the CGs ( $x_{548}$ ,  $x_{446}$ ) calculated from the uncertainty in  $\text{N}_2\text{O}$  mole fraction,  $\delta^{15}\text{N}^{\text{b}}$ , and  $\delta^{18}\text{O}$  (Supplementary Table 3) and its analytical uncertainty, estimated from the Allan deviation, using the MATLAB function *linfitxy*.<sup>45</sup> Propagation of uncertainties into the ratio  $R_{548}$  results in a relative combined standard uncertainty around 5 ‰. Main uncertainty contributions are allocated to the uncertainties of the slope  $a$  and the intercept  $b$  of the calibration functions and to a much lower extent to the Allan precision of sample or calibration gas measurements.

## DISCUSSION

The QCLAS technique for simultaneous and site selective analysis of the eight most abundant singly and doubly substituted  $\text{N}_2\text{O}$  isotopocules provides a precision of 0.10 – 0.40 ‰ for all  $\delta$  values using 4  $\mu\text{mol}$   $\text{N}_2\text{O}$  in a  $\text{N}_2$  gas matrix. This is superior to values previously reported using HR-IRMS, achieving 0.10 – 1.30 ‰ with a minimum of 10  $\mu\text{mol}$   $\text{N}_2\text{O}$ .<sup>16</sup> Another advantage of QCLAS lies in its ability of continuous data collection (typically 1 Hz) over extended periods as compared to discrete sampling and measurement by IRMS. Laser spectroscopic analysis is non-destructive, therefore offers a possibility for recovering the analyte.<sup>30</sup> Furthermore, triplicate analysis of a sample by laser spectroscopy requires 2 hours (the bracketing calibration scheme included), which is much faster than HR-IRMS where the sample is measured in six acquisition blocks for 8 – 10 hours.<sup>16</sup>

Analytical results were related to the stochastic distribution by thermal equilibration of  $\text{N}_2\text{O}$  over high-surface alumina. A progressive decrease in the 458 and 548 but not in the 556 enrichment (Fig. 2)

confirms an isotope-exchange equilibrium for the N–O bond only, in accordance with previous literature.<sup>46,47</sup> It is proposed that the N<sub>2</sub>O molecule undergoes reversible adsorption to the surface of Al<sub>2</sub>O<sub>3</sub> by the O atom. This results in the weakening and cleavage of the N–O bond and subsequent reversal of the N–N unit. The observed equilibration in the NO moiety only can be rationalized by dissociation energies of the respective bonds. The Gibbs free energy ( $\Delta G$ ) associated with the dissociation of the N–N bond is a factor of four higher than of the N–O bond, e.g. at 200 °C:  $\Delta G_{\text{N-O}} = 100.2 \text{ kJ mol}^{-1}$ ,  $\Delta G_{\text{N-N}} = 408.3 \text{ kJ mol}^{-1}$ , and persists independently of the presence of a catalyst.

The SP and SP<sup>18</sup> values of the thermally equilibrated gases with artificial spikes of 458, 548, and 556 (Table 1) gradually approached a constant value in accordance with the work of Magyar et al.<sup>16</sup> A comparison of SP values for equilibration results at 200 °C measured by the two laser spectrometers (QCLAS I, QCLAS II) with reference to the Air-N<sub>2</sub> scale<sup>8</sup> displays a reasonably good agreement with theoretical equilibrium distribution of N<sub>2</sub>O isotopocules<sup>18</sup> with differences of up to 2 ‰, within expanded uncertainty limits. For equilibration at 100 °C, analytical results are consistently up to 5 ‰ too low, which may attribute to incomplete equilibration (imprint of preheating) or to inconsistencies of the current reference scale for the N<sub>2</sub>O SP.<sup>48</sup> Further equilibration experiments were performed at temperatures up to 500 °C in order to identify alternative equilibration temperatures. However, at temperatures higher than 200 °C, more than 10 % of N<sub>2</sub>O is thermally decomposed into N<sub>2</sub> and O<sub>2</sub>, which affects the N<sub>2</sub>O isotopic composition due to isotopic fractionation. At lower temperatures, i.e. at 100 and 200 °C, more than 95 % of N<sub>2</sub>O is retrieved after the equilibration step, minimizing the effect of fractionation on the abundance of isotopocules. Therefore, we suggest that for future referencing of clumped isotopes in N<sub>2</sub>O, thermal equilibration experiments should be preferentially performed at 200 °C.

A new calibration scheme was implemented combining thermal equilibration and calibration of individual isotopocule mole fractions using high-accuracy gravimetric mixtures. This represents the first application of a mole fraction-based calibration scheme for clumped isotopes. It has a number of advantages over previous thermal equilibration-based  $\delta$ -calibration approaches. Namely, only one N<sub>2</sub>O source gas is required for multi-point calibration and high volumes of calibration standards can be produced, enabling the frequent calibration that is required for optical analyzers (calibration included in every sample measurement sequence). In addition, no post-correction of the analyzer response for dependencies on N<sub>2</sub>O mole fractions is needed, which is a usual requirement using the  $\delta$  calibration approach in laser spectroscopy.

Parallel measurements of the equilibrated validation gases VG2, VG3, and VG4 by QCLAS I and HR-IRMS indicate similar performance for bulk isotopic composition ( $\delta^{15}\text{N}^{\text{bulk}}$ ,  $\delta^{458+548}_{\text{avg}}$ ), and highlight the advantages of QCLAS for site specificity (SP and SP<sup>18</sup>). The HR-IRMS results of SP<sup>18</sup> were largely out of the ranges as predicted by theory, which can be attributed to the current inability of the IRMS technique in differentiating the clumped isotopomers 458 and 548 (Fig. 4D). Such deficiency may be caused by underestimated isotope scrambling in the ion source<sup>8,49</sup> and calls for even more complex correction schemes than those used to date (applied on the values  $\Delta^{458+548}_{\text{avg}}$  and SP<sup>18</sup> at 200 °C). Therefore, we recommend to limit the usage of HR-IRMS for SP<sup>18</sup> only for samples with natural isotopic abundance. On the contrary, the QCLAS technique does not need such corrections because it directly detects both pairs of isotopomers (456–546, 458–548). This is demonstrated by the good agreement between the measured and theoretical SP and SP<sup>18</sup> values (Fig. 4B and 4D).

The discrepancy of  $\Delta^{458+548}_{\text{avg}}$  measured with QCLAS I and HR-IRMS with the theoretical predictions of the samples highly enriched in <sup>15</sup>N and <sup>18</sup>O indicates that oxygen atoms may not be equilibrated in these gases as predicated by statistical thermodynamics. However, the measurements of SP and SP<sup>18</sup> were consistent with the theoretical results. It is possible that the exchange of oxygen atoms between different N<sub>2</sub>O molecules, which determines  $\Delta^{458+548}_{\text{avg}}$ , may not be complete due to an unknown

mechanism. This would call for an alternative equilibration approach for calibration of the  $\Delta^{458+548}_{\text{avg}}$  value.

Nonetheless, the standard uncertainty of the QCLAS technique for repeated measurements, i.e. 0.1 to 0.2 ‰ for both  $\Delta 458$  and  $\Delta 548$ , is sufficient to resolve 10 °C temperature differences of thermal production of N<sub>2</sub>O, to follow partial destruction by UV photolysis and to study kinetically controlled microbial processes. For  $\Delta 556$ , the current repeatability around 0.6 ‰ is adequate to detect photolytic N<sub>2</sub>O destruction and probably microbial disequilibrium processes but has to be further improved to resolve temperature differences in thermal equilibrium processes.

In the spectral regions used by our QCLAS technique, minimal interferences from other atmospheric trace (e.g. CO, CO<sub>2</sub>, H<sub>2</sub>O, CH<sub>4</sub> or O<sub>3</sub>) were identified by spectral simulations. Nonetheless, analysis of environmental samples requires pre-concentration to enhance the N<sub>2</sub>O mole fraction,<sup>50</sup> to adjust the gas matrix (N<sub>2</sub>), and to remove surplus of other trace gases. Alternatively, correction algorithms can be developed to account for spectral interferences as published by Harris et al.<sup>40</sup>

First applications of the developed QCLAS technique are currently on-going to identify the clumped isotopic signatures of N<sub>2</sub>O generated from bacterial nitrification (*Nitrosococcus oceani*) and denitrification (*Pseudomonas aureofaciens*). Furthermore, the imprint of UV photolysis on the clumped isotopic composition will also be assessed. This will provide insight into N<sub>2</sub>O sink processes occurring in the stratosphere and an independent proof for theoretical predictions.<sup>24</sup>

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## ACKNOWLEDGEMENTS

We would like to thank Paul Magyar for his initial support regarding the N<sub>2</sub>O thermal equilibration experiments, Heiko Moossen for the IRMS measurements, and Ivan Prokhorov for discussion about the  $\Delta$  notation. This work was supported by the Swiss National Science Foundation (Grant F200021\_166255) and by a young researchers exchange fellowship granted K.K. within the bilateral Japanese Swiss Science and Technology Program (JSPS International Fellowship for Research in Japan, fellowship ID: GR18108). L.Y. was supported by the EMPAPOSTDOCS-II programme, which received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement number 10754364.

## STATEMENT OF AUTHOR CONTRIBUTIONS

K.K. guided by S.M.B., L.E., and J.M. designed the study. L.Y. performed isotopic analyses using the single-laser QCLAS system. K.K. and D.Z. synthesized the doubly isotopically labelled ammonium nitrate salts; K.K. synthesized the samples of nitrous oxide from these salts. M.S.Z. and D.D.N designed and manufactured the dual-laser QCLAS instrument; B.T. supported the setup and optimization of the system at Empa and discussed the results. K.K., M.N., S.T., and N.Y. analyzed the equilibrated gases VG2, VG3, and VG4 on IRMS MAT253 Ultra at ELSI. K.K. performed the thermal equilibration experiments and calibration as well as validation experiments with QCLAS, analyzed the data and wrote the manuscript with input from all the co-authors.

## ADDITIONAL INFORMATION

Competing interests: The authors declare that they have no competing interests.

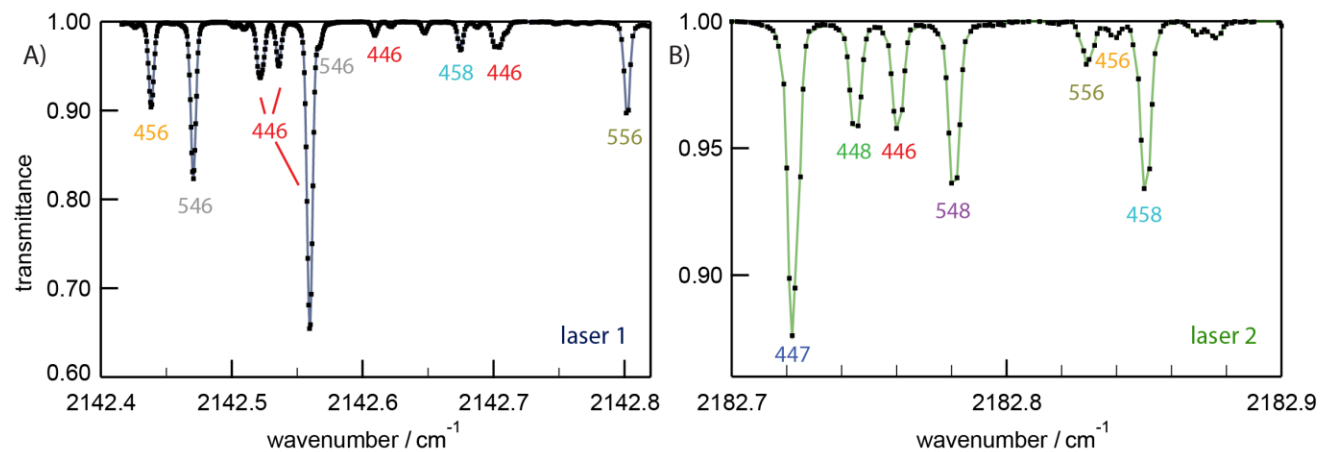


Figure 1. Measured (dots) and fitted (solid line) spectra of the N<sub>2</sub>O isotopocules for laser 1 (A) and laser 2 (B) in QCLAS I. Spectra were measured with 1.5 % N<sub>2</sub>O in a high-purity N<sub>2</sub> gas matrix.

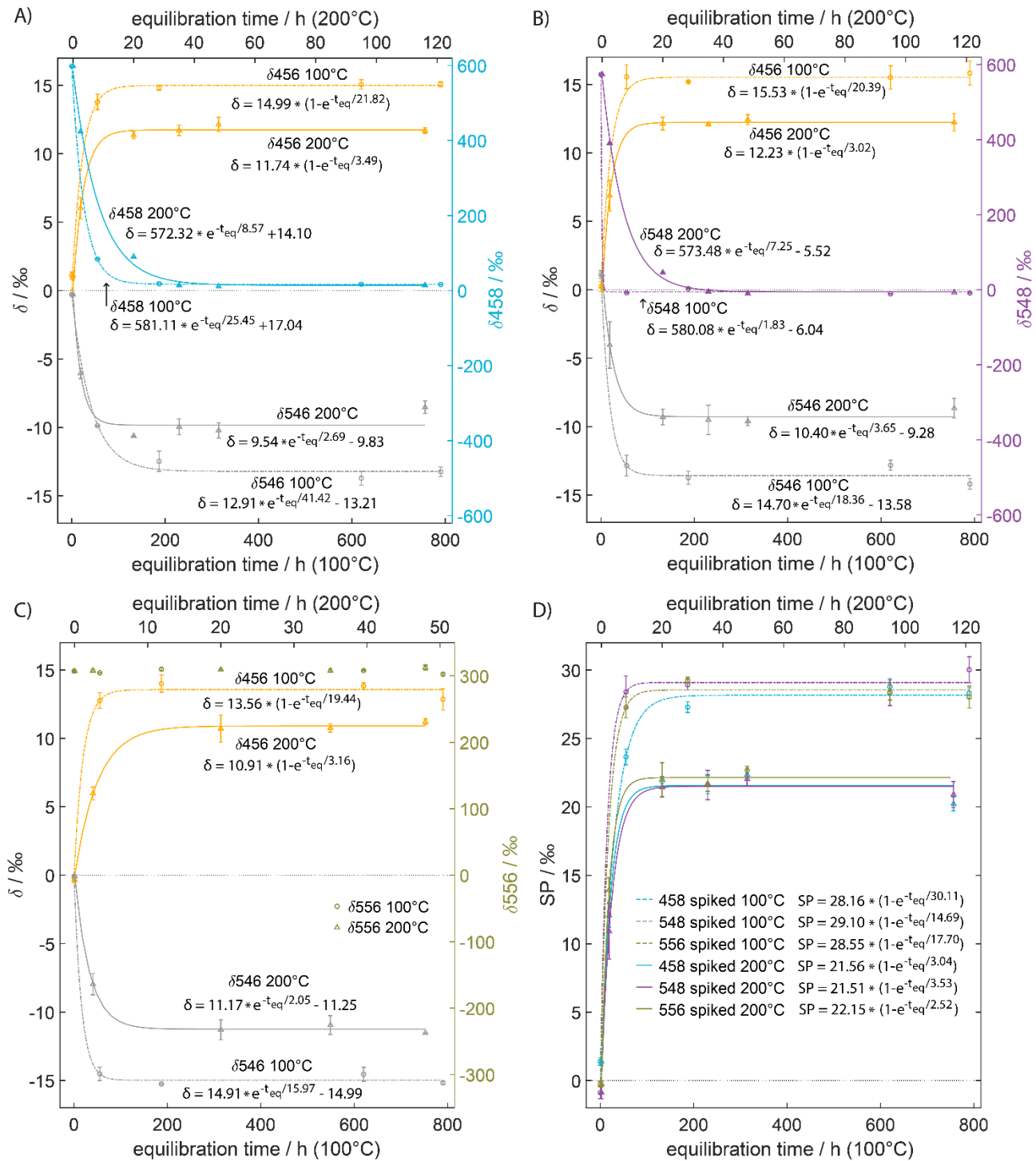


Figure 2. Progressive thermal equilibration of mixtures of N<sub>2</sub>O with enrichment of 458 (A), 548 (B), and 556 (C) isotopocules, heated at 100 °C (dashed lines) and 200 °C (full lines) over Al<sub>2</sub>O<sub>3</sub>. (D) Evolution of site preference (SP) in N<sub>2</sub>O mixtures during thermal equilibration at 100 °C (dashed lines) and 200 °C (full lines). The data is fitted using exponential decay and saturation functions.

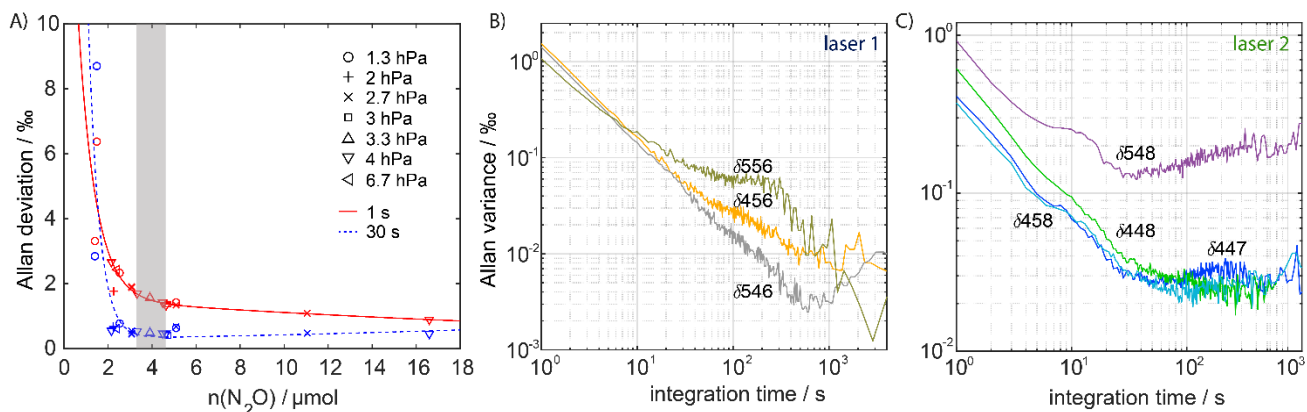


Figure 3. Allan variance plots. (A)  $\delta^{548}$  ( $^{15}\text{N}^{14}\text{N}^{18}\text{O}$ ) as a function of  $\text{N}_2\text{O}$  molar amount in the multipass cell for 1 s (red, solid line) and 30 s (blue, dashed line) spectral averaging. The grey-shaded area indicates the range of  $\text{N}_2\text{O}$  molar amounts yielding optimal measurement precision expressed as Allan deviation (3–4  $\mu\text{mol}$ ). (B, C) Allan variance of  $\delta$  values of all  $\text{N}_2\text{O}$  isotopocules measured by the QCLAS I.

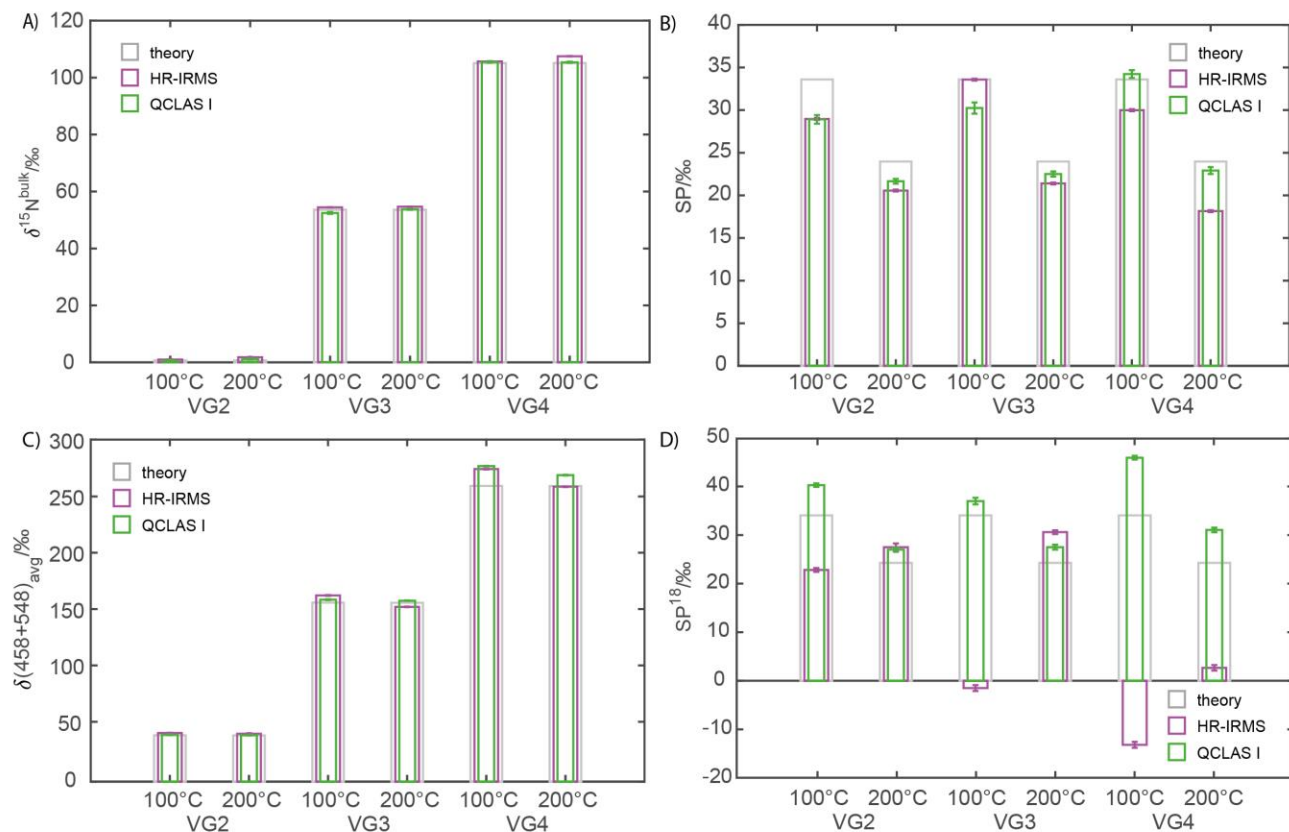


Figure 4. Comparison of theoretically predicted isotopic values (wide, grey columns) of equilibrated validation gases with experimental values from QCLAS I (narrow, green columns) and HR-IRMS (magenta columns).

Table 1. Site-specific isotopic composition of N<sub>2</sub>O gases spiked with clumped isotopocules and equilibrated at 100 and 200 °C over Al<sub>2</sub>O<sub>3</sub>. In comparison to results from Magyar et al.<sup>16</sup> and values derived from theoretical statistical thermodynamics by Wang et al.<sup>18</sup>

| temperature<br>/ °C | spike | SP / ‰<br>QCLAS I | SP / ‰<br>QCLAS II | SP / ‰<br>HR-IRMS <sup>16</sup> | SP / ‰<br>theory | SP <sup>18</sup> / ‰<br>QCLAS I | SP <sup>18</sup> / ‰<br>theory <sup>18</sup> |
|---------------------|-------|-------------------|--------------------|---------------------------------|------------------|---------------------------------|----------------------------------------------|
| 100 °C              | 458   | 28.70±0.39        | 28.94±0.16         |                                 |                  | 26.25±0.58                      |                                              |
|                     | 548   | 28.33±0.38        | 29.11±0.22         | 34.19±0.43                      | 33.75            | 26.48±0.37                      | 34.06                                        |
|                     | 556   | 28.65±0.23        | 30.00±0.17         |                                 |                  | 27.53±0.53                      |                                              |
| 200 °C              | 458   | 21.76±0.42        | 21.77±0.09         |                                 |                  | 20.31±0.54                      |                                              |
|                     | 548   | 21.60±0.49        | 23.53±0.19         | 23.28±0.43                      | 24.07            | 21.74±0.54                      | 24.27                                        |
|                     | 556   | 22.75±0.22        | 22.42±0.12         |                                 |                  | 22.04±0.38                      |                                              |

Table 2: Experimental results to validate QCLAS results applying the mole fraction calibration scheme. First, results for VG1 by QCLAS I were compared to QCLAS II and IRMS using conventional  $\delta$ -calibration. Second, for VG2, VG3, and VG4 equilibrated at 200 °C, theoretically predicted  $\delta$  and  $\Delta$  values were compared to experimental  $\delta$  and  $\Delta$  values analyzed by QCLAS I and IRMS MAT253 Ultra (HR-IRMS). Given uncertainty: QCLAS I – repeatability for multiple sample measurement sequences (VG1: N = 15, five triplicates; VG2, VG3, VG4: N = 5); QCLAS II – repeatability for multiple sample measurement sequence (N = 12, three quadruplicates); IRMS: fully propagated standard error of a sample; HR IRMS – repeatability for one measurement sequence (N = 6).

\* deviation due to limited span of available standards for  $\delta^{18}\text{O}$

† correction described in the main text

|                                   | $\delta 456$ / ‰ | $\delta 546$ / ‰ | $\delta 447$ / ‰ | $\delta 448$ / ‰ | $\Delta 556$ / ‰ | $\Delta(458+548)_{\text{avg}}$ / ‰ | $\text{SP}^{18}$ / ‰ |
|-----------------------------------|------------------|------------------|------------------|------------------|------------------|------------------------------------|----------------------|
| <b>VG1</b>                        |                  |                  |                  |                  |                  |                                    |                      |
| QCLAS I                           | 15.53±0.16       | 16.27±0.17       | 21.41±0.09       | 55.13±0.24       | 0.68±0.65        | -0.66±0.14                         | 4.70±0.09            |
| QCLAS II                          | 15.82±0.06       | 16.80±0.08       | -                | 53.93±0.06*      | -                | -                                  | -                    |
| IRMS                              | -                | -                | -                | 55.96±0.07       | -                | -                                  | -                    |
| <b>VG2</b>                        |                  |                  |                  |                  |                  |                                    |                      |
| QCLAS I                           | -1.75±0.20       | -0.62±0.31       | 21.28±0.18       | 40.46±0.52       | 0.95±0.66        | 0.86±0.55                          | 3.26±0.59            |
| QCLAS II                          | 0.30±0.20        | 1.05±0.38        | -                | 38.90±0.36*      | -                | -                                  | -                    |
| IRMS                              | -                | -                | -                | 39.79±0.07       | -                | -                                  | -                    |
| <b>VG2 equilibrated at 200 °C</b> |                  |                  |                  |                  |                  |                                    |                      |
| theory                            | 12.74            | -11.32           | 20.54            | 39.78            | 0.12             | 0.12                               | 24.26                |
| QCLAS I                           | 11.98±0.19       | -9.77±0.20       | 21.86±0.15       | 40.69±0.21       | -1.49±0.64       | -0.77±0.25                         | 27.00±0.44           |
| HR-IRMS                           | 12.08±0.06       | -8.56±0.10       | 20.84±0.03       | 41.32±0.01       | -                | -0.96±0.40†                        | 27.49±0.79†          |
| <b>VG3</b>                        |                  |                  |                  |                  |                  |                                    |                      |
| QCLAS I                           | 52.54±0.28       | 55.89±0.18       | 24.60±0.24       | 105.96±0.27      | 7.60±1.53        | 1.40±0.72                          | 1.96±0.22            |
| QCLAS II                          | 51.02±0.16       | 54.99±0.06       | -                | 99.68±0.34*      | -                | -                                  | -                    |
| IRMS                              | -                | -                | -                | 104.14±0.07      | -                | -                                  | -                    |
| <b>VG3 equilibrated at 200 °C</b> |                  |                  |                  |                  |                  |                                    |                      |
| theory                            | 65.11            | 41.05            | 24.49            | 104.14           | 0.12             | 0.12                               | 24.26                |
| QCLAS I                           | 64.54±0.26       | 41.93±0.16       | 26.17±0.30       | 102.35±0.34      | 7.65±0.59        | 3.76±0.37                          | 27.50±0.50           |
| HR-IRMS                           | 64.87±0.06       | 43.38±0.10       | 24.41±0.02       | 100.05±0.01      | -                | -0.46±0.20†                        | 30.59±0.37†          |
| <b>VG4</b>                        |                  |                  |                  |                  |                  |                                    |                      |
| QCLAS I                           | 101.23±0.34      | 100.22±0.85      | 29.39±0.17       | 157.22±0.09      | 24.54±1.33       | 8.03±0.90                          | 5.17±0.11            |
| QCLAS II                          | 102.71±0.16      | 104.93±0.50      | -                | 148.02±0.70*     | -                | -                                  | -                    |
| IRMS                              | -                | -                | -                | 155.86±0.14      | -                | -                                  | -                    |
| <b>VG4 equilibrated at 200 °C</b> |                  |                  |                  |                  |                  |                                    |                      |
| theory                            | 116.11           | 92.04            | 27.63            | 155.86           | 0.12             | 0.12                               | 24.26                |
| QCLAS I                           | 115.87±0.40      | 92.86±0.05       | 29.95±0.15       | 152.02±0.28      | 21.83±0.63       | 13.44±0.42                         | 31.05±0.49           |
| HR-IRMS                           | 115.59±0.05      | 97.36±0.10       | 28.16±0.09       | 149.22±0.18      | -                | 3.74±0.31†                         | 2.67±0.56†           |