





Fig. 2. Measured and computed absorption spectra of: (a) the  $\nu_1$  fundamental band of  $\text{N}_2\text{O}$  and (b) the  $\nu_4$  fundamental band of  $\text{CH}_4$ . Line centre frequency errors relative to: (c) the values in [7] and (d) the values in HITRAN2016 [8].

### 3. Results and discussion

We measured the  $\nu_1$  fundamental band of  $\text{N}_2\text{O}$  at 1.5 mbar in the MPC (Fig. 2a) and the  $\nu_4$  fundamental band of  $\text{CH}_4$  at 1.8 mbar (Fig. 2b). Accurate published transition frequencies for  $\text{N}_2\text{O}$  [7,9] allow us to test the accuracy of our frequency scale. The frequency scale is accurate to within  $\pm 1$  MHz between 1269 and 1281  $\text{cm}^{-1}$  and between 1288 and 1303  $\text{cm}^{-1}$  (Fig. 2c). Only three of the 43 measured transitions exhibit an error greater than 2 MHz, and each of these exceptions is located in a region of poor signal-to-noise ratio (SNR). For methane, we compare the measured line centre frequencies with the HITRAN2016 database [8] (Fig. 2d). The discrepancy between our measurement and the HITRAN database is up to 10 MHz. Since it qualitatively matches a recent measurement [10], we account for it through the uncertainty of the database, given as between 30 and 300 MHz.

### 4. Conclusions

We have demonstrated dual-comb spectroscopy in 54 ms with a resolution of 630 kHz and with frequency accuracy better than 2 MHz over almost the entire spectral coverage of the comb source.

### 5. References

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