Evidence for Condon domains in white tin with two de Haas–van Alphen periods

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The observation of Condon domains in white tin, obtained by muon spin rotation spectroscopy, is reported. The experiment at $T=0.08$ K for external magnetic fields between 1 and 2.6 T perpendicular to the (100) crystal plane reveals two “active” extremal cross sections of the Fermi surface, leading to domain formation with two different de Haas–van Alphen frequencies $F(\tau_2^1)$ and $F(\pi_2^1)$ at different field ranges and having a crossover region with no periodicity.

The periodic phase transitions generating dia- and paramagnetic domains in nonmagnetic (*sp*) metals in a homogeneous magnetic field $\mathbf{H}$, predicted by Condon,¹ arise because of the instability of the spatially uniform state of the electron system against “too large” de Haas–van Alphen (dHvA) oscillations. This is the case for

$$\chi_a(B, T) = (\partial M / \partial B)_{\max} > 1/4\pi \quad (1)$$

(where χ_a is the amplitude of the oscillating susceptibility $\chi = \partial M / \partial B$ and B , M are components along $\mathbf{H}$), implying that the induction B as a function of H is multivalued. For a rod oriented parallel to the field, a discontinuous change of B from a lower (B_1) to a higher (B_2) value takes place in *each* dHvA period^{1,2} with a jump of the magnetization from a diamagnetic [$M(B_1) \equiv M_d < 0$] to a paramagnetic [$M(B_2) \equiv M_p > 0$] state, the ascending $\chi > 0$ sections of the cycles are not realized. For a platelike sample set normal to $\mathbf{H}$, the discontinuity of B and the requirement of flux conservation lead, for $B_1 < H < B_2$, to the break-up of the uniform state and the coexistence of alternating oppositely magnetized regions with $B=B_1$ and $B=B_2$, the relative volumes of the dia- and paramagnetic domains adjusting themselves to satisfy $\bar{B}=H$.

In the limit $T, T_D \rightarrow 0$ (T_D is the Dingle temperature) the crossing of the edge of a Landau subband with the Fermi level can be interpreted as an electronic topological transition (ETT)^{3,4} at a Lifshitz-type singularity. Since this ETT would, however, be associated with an infinite susceptibility² corresponding, by Eq. (1), to an unstable region, it is preceded (and replaced) by a first-order ETT leading to the Condon domain state. For a quasi-two-dimensional (2D) band structure the chemical potential is pinned⁵ in both the para- and diamagnetic domains at equally high, exactly filled Landau levels [the n th and $(n+1)$ th, respectively], and zero resistivity within each domain has been predicted. In normal metals with overlapping Landau subbands the situation is more complex, the subject keeps attracting intense theoretical interest.^{3,6–8}

Up to now direct, spectroscopic evidence for Condon domains was obtained only in two cases: for silver, by NMR,⁹ and recently for Be by muon spin rotation (μ SR) spectroscopy.^{10,11} Yet this scarcity of data does not mean that Condon domains are “exotic,” it is due to experimental dif-

ficulties (a need for highly perfect single crystals, detecting small field splittings $\Delta B = B_2 - B_1 \approx 10 - 50$ G in applied fields of some T, at temperatures $\lesssim 1$ K). In the “normal” 3D case (when the Lifshitz-Kosevich formula² applies), Eq. (1) for the first harmonic of a given dHvA mode i has the form

$$\chi_a^{(i)} = (B_0/B)^{3/2} \exp(-B_D/B) (B_T/B) / \sinh(B_T/B) > 1/4\pi, \quad (2)$$

where $B_0 \equiv B_0^{(i)}$ is entirely determined by the Fermi surface (FS) parameters (cyclotron mass m_i^* , extremal cross-sectional area $\mathcal{A}_i$ normal to $\mathbf{H}$, derivative $\mathcal{A}_i' = \partial^2 \mathcal{A}_i / \partial k_z^2$ along the field direction), $B_D \equiv B_D^{(i)} = (2\pi^2 k_B m_i^* c / \hbar e) T_D$ and $B_T \equiv B_T^{(i)} = (2\pi^2 k_B m_i^* c / \hbar e) T$. This inequality is always satisfied for some interval of B provided T_D and T are sufficiently low.^{2,8,12} The results below show this in the case of metallic (white) tin.

Tin has several low lying dHvA frequencies $F_i = (\hbar c / 2\pi e) \mathcal{A}_i$ for which the dHvA period $\Delta H = H^2 / F$ is sufficiently long even for moderate fields of $H < 3$ T. This facilitates a fine mapping of the oscillatory cycle, which is necessary, since the “domain” section may be only a very small fraction of the dHvA period. This is certainly so for $4\pi\chi_a \gtrsim 1$, but may be the case also for $4\pi\chi_a \gg 1$ when both T and T_D are very low ($B_T, B_D \ll B$), due to the cusps of the oscillating magnetization M in this case² even when its amplitude M_0 is much smaller than the period ($8\pi^2 M_0 \ll \Delta H$). The FS of white tin^{13–19} accommodates eight electrons, with electron sheets in the 4th, 5th, and 6th Brillouin zones (BZ). For $\mathbf{H} || [100]$, one has five low-frequency dHvA oscillations, out of which *three* modes with the orbits τ_2^1, π_2^1 , and ϵ_2^2 have sizeable amplitudes.^{17,18} The lowest frequency $F(\tau_2^1) = 446.8 \pm 0.1$ T (Ref. 19) is related to the central cross-sectional area of the “molar tooth” shaped FS sheet in the sixth zone,¹⁵ with cyclotron mass $m^*/m_0 = 0.29 \pm 0.06$.¹⁶ Besides the small m^* , the low “longitudinal” curvature $\mathcal{A}'' \approx 0.7$ at this cross section¹⁹ is also favorable for satisfying Eq. (2) [$B_0 \propto 1/(m^* \mathcal{A}'')^{1/3}$ (Ref. 2)]. The mode π_2^1 , with frequency $F(\pi_2^1) = 2080 \pm 20$ T and with m^*/m_0 between 0.55 and 0.79^{16,17} corresponds to the extremal cross section of the “pears and tubes” FS sheet in the fifth BZ, and the orbit ϵ_2^2 [$F(\epsilon_2^2) = 3400 \pm 50$ T] lies on the “earring” section in the fourth BZ.

FIG. 1. Variation of the exponential damping rate $\lambda(H)$ (line broadening) for $T=0.08$ K for white tin, $\mathbf{H}||[100]$. The observed period $\Delta H \approx 23$ G agrees with the value of 22.6 G corresponding to the dHvA frequency $F(\tau_2^1) = 446.8$ T (Ref. 19). The periodic peak regions are interpreted as due to the Condon domain state with oppositely magnetized regions, with $4\pi\Delta M = \Delta B \approx \lambda/2\gamma_\mu \approx 2.5$ G.

In the experiment, an ultrahigh purity Sn crystal plate [$18 \times 12 \times 0.56$ mm³, electron mean free path $\approx$ some mm (Ref. 13)] grown parallel to the plane (100) was put into the field $\mathbf{H}||[100]$ and cooled down to $T=0.08$ K. Transverse field μ SR measurements,²⁰ monitoring the time-dependent polarization [frequency(ies), damping rate(s), and amplitude(s)] of the precessing μ^+ spins were performed at the surface muon beamline π M3 of PSI, Villigen, as in Refs. 10 and 11, by varying H in small steps in different regions between 1 and 2.6 T. The background noise was reduced by use of the MORE (muons-on-request) technique.²¹

Field scans were done first at $H=1$ T, where preliminary, low resolution data indicated an oscillating component in the linewidth.²² Mapping of a few adjacent dHvA cycles [with period $\Delta H \approx H^2/F(\tau_2^1) \approx 23$ G] gives the result shown in Fig. 1, where the damping rate λ (line broadening in frequency space) is plotted against the applied field H . The sharp peaks are evidence of a periodic, sudden broadening of the field distribution in the bulk of the sample, which is difficult to reconcile with *any* single-phase state. [Should, for example, the variation of λ reflect a spread $|\delta B|$, due to the nonellipsoidal shape of the sample and oscillating with χ , the period for λ would be that of $|\chi(B)|$, i.e., $\Delta H/2$.] Moreover, the peaks in λ are similar to those observed in Be,^{10,11} where the “broad” lines turned out to be doublets, with distinct frequencies for the dia- and paramagnetic domains. This suggests that the peaks in Fig. 1 are equally signs of the domain splitting, with the corresponding $\Delta B \approx 2\lambda/\gamma_\mu \approx 2.5$ G too small to allow resolution of the doublet. (Here $\gamma_\mu = 2\pi \times 13.554$ kHz G⁻¹ is the gyromagnetic ratio of the muon; the experimental resolution was $\Delta B \approx 6-8$ G.) The next scans were done in successively higher fields, with the aim to increase ΔH and, eventually, also ΔB . At $H=1.41$ T, the oscillation of λ looks the same as in Fig. 1 but with a period $\Delta H=46$ G twice as long, the peak values $\lambda \approx 0.14$ μ s⁻¹ are still too small for an assumed doublet to be resolved.

By a further increase of the field at $H=2$ T, unexpectedly, a radically different picture seen in Fig. 2 was obtained:

FIG. 2. Loss of periodicity in the damping rate $\lambda(H)$ near $H=2$ T. The peaks mark, as before, the presence of highly inhomogeneous magnetization and possibly domains, but these cannot be related to any single dHvA mode.

the points for $\lambda(H)$ seem to be randomly scattered within the range of $0.1-0.2$ μ s⁻¹, showing *no periodicity at all*. Though the large peaks of λ indicate, here also, the presence of highly inhomogeneous structures, the relation to quantum oscillations seems to be lost.

At the still higher field $H=2.6$ T, as seen in Fig. 3, the periodicity of $\lambda(H)$ reappears, but the period $\Delta H=33$ G shows that the “active” dHvA frequency has changed: instead of $F(\tau_2^1)$ as in Fig. 1, one has $F=H^2/\Delta H=2064$ T. This agrees with the value $F(\pi_2^1)=2080 \pm 20$ T for the π_2^1 mode in the *fifth* BZ, for which the curvature of the FS along $\mathbf{H}||[100]$ is also small,¹⁴ favorizing domain formation.

The appearance of the second “domain active” dHvA mode gives the explanation for the absence of periodicity near $H=2$ T. Equation (1) predicts *periodic* instabilities when a single mode, with amplitude $\chi_a^{(i)} > 1/4\pi$, is “dominant” in the given field range. The prevalence of one mode in certain field ranges is due to the fact that, by Eq. (2), $\chi_a^{(i)}(B)$ has a maximum for each mode, with the positions of

FIG. 3. Periodicity reappearing in the damping rate $\lambda(H)$ near $H=2.6$ T, related to the dHvA mode π_2^1 . The expected period is $\Delta H=H^2/F(\pi_2^1)=32.8 \pm 0.4$ G (Ref. 19), the solid curve is a fit by a finite Fourier series (up to the 4th harmonics) with $\Delta H=33.3 \pm 0.005$ G. The peak values $\lambda \approx 0.4$ μ s⁻¹ lead to the estimate $\Delta B \approx 9$ G (see Fig. 4).

FIG. 4. Induction B as a function of the applied field H for the same field range as in Fig. 3. The two B branches indicate sections with Condon domains, with a splitting of $\Delta B \approx 8$ G. The nonideal shape of the plateaus is discussed in the text.

the maxima shifted upwards with increasing m_i^* .² As Figs. 1 and 3 show, for $H \leq 1.41$ T and $H \geq 2.6$ T one has the dominating oscillations τ_2^1 and π_2^1 , respectively. However, Eq. (1) is the *general* condition for a Condon instability, no matter whether this results from a single quantum oscillation or from a number of superposed modes. In the present case, as the increasing H reaches the range $1.41 < H < 2.6$ T, the already decreasing amplitude for τ_2^1 and the still growing one for π_2^1 become comparable and, at some B values, the *superposition* of the two modes $\chi(B) = \sum_{i=\tau_2^1, \pi_2^1} \chi_a^{(i)} \cos(2\pi F_i/B + \phi_i)$ satisfies $\chi > 1/4\pi$. The irregular $\lambda(H)$ sequence observed at $H = 2$ T is due to the incommensurate frequencies, implying no periodicity for the position or length of the domain sections.

The maximum $\lambda \approx 0.4 \mu s^{-1}$ in Fig. 3, if due to a doublet, gives the estimate $\Delta B \approx 2\lambda/\gamma_\mu \leq 9$ G, already resolvable for sufficiently narrow component lines. Although a splitting in frequency space was visible only for the top value at $H = 26067$ Oe, the systematic variation of the lineshape indicates indeed the presence of two components, with intensities “flowing” from the lower (diamagnetic) line to the higher (paramagnetic) one as H increases.

The doublet structure is quantitatively confirmed by a standard analysis of the observed time series of the μ^+ polarization $P(t)$, by use of the fit function¹¹

$$P(t; H) = \sum_{j=1,2} a_j(H) e^{-\lambda^{(j)}(H)t} \cos[\gamma_\mu B_j(H)t + \psi], \quad (3)$$

with parameters $a_j, \lambda^{(j)}, B_j, \psi$. For a uniform state one expects to find $B_1(H) = B_2(H)$, while in the presence of Condon domains two distinct fields B_1, B_2 should result, both staying constant along the domain section of the dHvA cycle, whereas $a_1(H), a_2(H)$ should vary linearly, with the sum $a_1 + a_2$ independent of H . The parameters were allowed to vary freely, except for the plausible restriction $\lambda^{(1)} = \lambda^{(2)}$ for the doublet components.

The result of the fit for $B(H)$ is seen in Fig. 4, showing sections with two branches of B separated by $\Delta B \approx 8$ G in each dHvA cycle. The approximately flat B_1, B_2 branches in the first and third cycles are characteristic to the domain state, though there are no “plateaus” in the middle domain

FIG. 5. Asymmetries ($\propto$ volume fractions) a_1 ($\circ$) and a_2 ($\triangle$) for the dia- and paramagnetic domains, respectively, in the first Condon domain section of Fig. 4, showing the predicted linear behavior. For clarity, part of the $B(H)$ curve is redrawn with the corresponding symbols for the two branches, the mark $\square$ stands for the uniform phase. The pairs of points for a_i with the same symbol are data from two different detectors mounted at opposite sides of the sample.

section. The reason for this is not clear. An incomplete domain formation in some cycles may occur because of the smallness of the gain in free energy (scaled by $4\pi\chi_a$) that drives the transformation,² or due to the narrowness of the domain section $\delta H = n\Delta B$ ($n \approx 0.95$ is the demagnetizing coefficient for this sample). Also, ΔB here is still near to the resolution limit, and the statistical uncertainties in the data may lead to large distortions in the fitted shape of the $B(H)$ branches.

The μ^+ asymmetries (amplitudes) $a_i(H)$ of the doublet components are plotted in Fig. 5 for the first domain section of Fig. 4. The linear variations of a_1 and a_2 (for the dia- and paramagnetic components, respectively) with decreasing H show the readjustment of the domain volumes predicted by the “Maxwell construction” for $\bar{B} = H$. For $H > 26070$ Oe the crystal is uniform and the asymmetry is constant.

FIG. 6. Damping rate λ vs temperature at different applied fields: $B = 1$ T ($\square$) and 1.4 T ($\triangle$) for mode τ_2^1 , and 2.6 T ($\circ$) for mode π_2^1 . Domains are absent above the critical temperature T_0 , below T_0 the field splitting $\Delta B \propto \lambda(T)$ increases with decreasing temperature.

With the increase of temperature the dHvA amplitude and thereby the splitting ΔB should, according to Eq. (2), monotonically decrease and ΔB disappears at $T=T_0$ determined by $4\pi\chi_a^{(i)}(T_0)=1$. Figure 6 shows this predicted behavior of $\lambda(T)\propto\Delta B(T)$ for the two modes, at fields corresponding to equal volumes of dia- and paramagnetic regions. For $T>T_0$ one has $\lambda\approx\lambda_0$, where λ_0 is characteristic for the *uniform* state of the sample and does not vary at this temperature range.

In conclusion, evidence for dia- and paramagnetic domains in white tin has been obtained. Even for the relatively low fields of 1–2.6 T, the topology of the Fermi surface provides *two* domain generating dHvA oscillations for $H||[100]$: mode τ_2^1 is dominant for $H\leq 1.4$ T and mode π_2^1 near $H=2.6$ T. In the intermediate field range domain formation is driven by the superposition of the two modes of

comparable amplitudes, resulting in no periodicity in the sequence of domain states. The field splitting $\Delta B=4\pi(M_p-M_d)\approx 8$ G due to the opposite domain magnetizations M_d, M_p could, for the π_2^1 mode, be resolved in the μ SR signal, with line intensities showing the predicted linear behavior. For the τ_2^1 oscillation ΔB is smaller, but the doublet structure, unresolved in this case, is manifest in itself in the periodically arising sharp peaks of the line broadening $\lambda(B)$. For both “domain active” modes, $\lambda(T)\propto\Delta B(T)$ decreases monotonically with increasing temperature.

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