Spin dynamics in NaFeAs and NaFe_{0.53}Cu_{0.47}As probed by resonant inelastic x-ray scattering

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The parent compounds of iron-based superconductors are magnetically ordered bad metals, with superconductivity appearing near a putative magnetic quantum critical point. The presence of both Hubbard repulsion and Hund's coupling leads to rich physics in these multi-orbital systems, and motivated descriptions of magnetism in terms of itinerant electrons or localized spins. The NaFe_{1-x}Cu_xAs series consists of magnetically ordered bad metal ($x = 0$), superconducting ($x \approx 0.02$) and magnetically ordered semiconducting/insulating ($x \approx 0.5$) phases, providing a platform to investigate the connection between superconductivity, magnetism and electronic correlations. Here we use x-ray absorption spectroscopy and resonant inelastic x-ray scattering to study the valence state of Fe and spin dynamics in two NaFe_{1-x}Cu_xAs compounds ($x = 0$ and 0.47). We find that magnetism in both compounds arises from Fe²⁺ atoms, and exhibits underdamped dispersive spin waves in their respective ordered states. The dispersion of spin excitations in NaFe_{0.53}Cu_{0.47}As is consistent with being quasi-one-dimensional. Compared to NaFeAs, the band top of spin waves in NaFe_{0.53}Cu_{0.47}As is slightly softened with significantly more spectral weight of the spin excitations. Our results indicate the spin dynamics in NaFe_{0.53}Cu_{0.47}As arise from localized magnetic moments and suggest the iron-based superconductors are proximate to a correlated insulating state with localized iron moments.

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I. INTRODUCTION

The parent compounds of cuprate superconductors are magnetically ordered Mott-insulators, where the spin-1/2 Cu²⁺ moments forming antiferromagnetic (AF) order are completely localized and can be well-described by a Heisenberg Hamiltonian [1–3]. Because high-temperature superconductivity in cuprates is derived from magnetically ordered parent compounds after eliminating static AF order, it is generally believed that electronic correlations and magnetism are important for the superconductivity of these materials [1,2]. Spin dynamics in the parent compounds of cuprate superconductors are described by spin waves due to interactions between localized moments [3]. Cuprate superconductors exhibit similar spin dynamics, especially in the underdoped regime and at high-energies, suggesting the inheritance of

short-range spin correlations from their parent compounds [4–7]. In contrast, the parent compounds of iron-based superconductors (FeSCs) are magnetically ordered bad metals with significant electronic correlations [8–11], suggesting that their spin dynamics may originate from either localized spins or itinerant electrons.

In contrast to the cuprates which can be effectively described using a single orbital, the FeSCs are multi-orbital systems (with five 3d orbitals), and the presence of both Hubbard repulsion U and Hund's coupling J_H leads to a rich theoretical phase diagram [10,11]. At half-filling (with a total of $n = 5$ electrons per Fe), both U and J_H promote a Mott insulating state. Away from half-filling (such as $n = 6$), while large U and J_H lead to strong electronic correlations, a bad-metal state becomes favorable and a Mott insulating state is realized only for an intermediate range of J_H [12,13].

Since parent compounds of the FeSCs (with $n = 6$) exhibit large values of resistivity, comparable to those of underdoped cuprates, they fall in the bad metal regime, and have been suggested to exhibit incipient Mott physics [14]. In such a scenario, the metallic transport is due to the coherent part of the single-electronic excitations, while magnetism results from localized moments formed by the incoherent part [11].

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FIG. 1. (a) Magnetic structure of NaFeAs. (b) Magnetic structure of NaFe_{0.5}Cu_{0.5}As. (c) Local atomic environment in NaFeAs, with atomic distances from Ref. [20] for $T = 295$ K. (d) Local atomic environment in NaFe_{0.5}Cu_{0.5}As, with atomic distances from Ref. [25] for $T = 250$ K. (e) Reciprocal space of NaFeAs and NaFe_{0.5}Cu_{0.5}As. In both cases two types of domains are present, with spin waves exhibiting intensities at either $\mathbf{Q} = (1, 0)$ or $\mathbf{Q} = (0, 1)$. Since the reciprocal space probed by RIXS is limited to the dashed circle near $\mathbf{Q} = (0, 0)$ for NaFeAs (2% larger in diameter for NaFe_{0.5}Cu_{0.5}As), intensities from twin domains overlap. The shaded ellipsoids are schematic intensity contours for spin waves with anisotropic spin velocities in NaFeAs and NaFe_{0.5}Cu_{0.5}As. (f) Schematic scattering geometry of our RIXS measurements.

From this perspective, as electronic correlations are enhanced, a magnetically ordered $n = 6$ insulating phase should appear. BaFe₂Se₃ and BaFe₂S₃ tuned via pressure may be a realization of such a scenario [15–18], with their ground states transformed from magnetically ordered insulators under ambient conditions to superconductivity under pressure (the strength of electronic correlations decreases with increasing pressure). Alternatively, the FeSCs may be anchored around a half-filled ($n = 5$) Mott insulating state, with the magnetic and nematic orders in the parent compounds ($n = 6$) being the competing states that suppress superconductivity [19].

As an archetypal parent compound of FeSCs, NaFeAs exhibits a tetragonal-to-orthorhombic transition below $T_S \approx 55$ K and stripe-type collinear magnetic order [Fig. 1(a)]

below $T_N \approx 45$ K [20–22]. The magnetic and structural phase transitions in NaFeAs are quickly suppressed upon Cu-doping, giving way to superconductivity near $x \approx 0.02$ [23]. With further increase of Cu concentration, NaFe_{1-x}Cu_xAs starts to exhibit semiconducting/insulating electrical transport, accompanied by the appearance of short-range magnetic order and charge-gapped patches [24,25]. Upon approaching $x = 0.5$, Fe and Cu order into stripes and long-range magnetic order with $T_N \approx 200$ K reemerges [Fig. 1(b)], accompanied by a charge gap that persists above T_N [25–28]. The ordering between Fe and Cu atoms in the $x = 0.5$ compound is a structural analog of the stripe-type magnetic order in NaFeAs, resulting in quasi-one-dimensional (quasi-1D) Fe chains separated by nonmagnetic Cu chains. Such a superstructure has been suggested to be essential for the insulating properties [29] and the electronic structure [30] of the $x = 0.5$ compound. The magnetic structure of NaFe_{0.5}Cu_{0.5}As can be obtained from that of NaFeAs simply by replacing half of Fe atoms by nonmagnetic Cu atoms and rotating the orientations of magnetic moments by 90°, although with a much larger ordered moment ($\geq 1.1 \mu_B/\text{Fe}$ [25]) relative to that of NaFeAs ($\sim 0.1 \mu_B/\text{Fe}$ [20–22]). Locally, while the Fe-As distance is slightly larger in NaFe_{0.5}Cu_{0.5}As compared to NaFeAs, the heights of As atoms away from the transition metal planes are similar in the two compounds [Figs. 1(c) and 1(d)]. While simple valence counting suggests Fe to be in a 3+ state with $n = 5$ [25], the similar local environments of Fe ions in NaFeAs and NaFe_{0.5}Cu_{0.5}As suggests Fe in the latter to be in a 2+ state with $n = 6$.

Near $x \approx 0.5$, the insulating/semiconducting electrical transport in NaFe_{1-x}Cu_xAs exhibits a low-temperature resistivity $\sim 1 \Omega \cdot \text{cm}$. Such a resistivity value is comparable to that found in Fe_{1+\delta-x}Cu_xTe ($0.1\text{--}1 \Omega \cdot \text{cm}$ when $x \approx 0.5$) [31–34], but contrasts with the much smaller resistivity values ($\sim 1 \text{ m}\Omega \cdot \text{cm}$) in the Sr(Fe_{1-x}Cu_x)₂As₂ [35] and Ba(Fe_{1-x}Cu_x)₂As₂ [36] series. Such a difference may result from stronger electronic correlations in NaFeAs and FeTe [9,37], which persist upon $\sim 50\%$ Cu-doping and cause these systems to exhibit larger resistivity values. Another possibility is that while the structure of Sr(Fe_{1-x}Cu_x)₂As₂ and Ba(Fe_{1-x}Cu_x)₂As₂ allows the formation of c -axis collapsed phases with As-As covalent bonds [38,39], such a phase is unlikely in NaFe_{1-x}Cu_xAs and Fe_{1+\delta-x}Cu_xTe given the much larger As-As or Te-Te distances. From a theoretical perspective, insulating/semiconducting NaFe_{1-x}Cu_xAs with $x \approx 0.5$ may be a Mott insulator [25], in which an electronic gap opens due to strong electron-electron interactions; alternatively, a Slater insulator scenario, in which an electronic gap results from the symmetry lowering associated with magnetic order, has also been suggested [27]. In the latter scenario, persistent insulating/semiconducting behavior above T_N is suggested to result from spin fluctuations that persist well above T_N in a quasi-1D system, which lead to an electronic gap similar to static magnetic order.

Spin dynamics in the FeSCs not only contain information on their magnetic interactions, but also provide clues regarding the size of the fluctuating magnetic moment (seen within timescale of the experimental probe), which in turn reflects the system's degree of itinerancy/localization [40–42]. While spin dynamics in FeSCs and related compounds are typically

investigated using inelastic neutron scattering (INS) [42–44], resonant inelastic x-ray scattering (RIXS) has emerged as a useful complementary probe [45–55]. Since NaFeAs and NaFe_{0.5}Cu_{0.5}As exhibit significant similarities in their crystal and magnetic structures, a comparison of the spin dynamics in the two systems may provide insights for understanding the magnetism in the FeSCs.

In this work, we use x-ray absorption spectroscopy (XAS) and RIXS to study magnetically ordered NaFe_{1-x}Cu_xAs with $x = 0$ and 0.47 [Figs. 1(a) and 1(b)]. Our XAS measurements reveal that Fe atoms maintain a +2 valence in both compounds, despite Cu being in a +1 state in the latter. Underdamped dispersive spin waves were uncovered in both compounds, consistent with their magnetically ordered ground states. Measurements along the (q, q) direction is unaffected by twinning and allows the intrinsic spin wave dispersion to be extracted through RIXS measurements. Compared to spin waves in NaFeAs, the spin waves in NaFe_{0.53}Cu_{0.47}As are softer in energy but more intense in intensity, indicating a larger total (ordered and fluctuating) moment and stronger electronic correlations associated with its Fe²⁺ state. Our results suggest the magnetism in NaFe_{0.5}Cu_{0.5}As arises from localized spins, and are consistent with the FeSCs being close to a $n = 6$ correlated insulating state.

II. METHODS

A. Experimental details

Single crystals of NaFe_{1-x}Cu_xAs ($x = 0$ and 0.47) were grown using the self-flux method [23,25]. We probe the spin dynamics in the $x = 0.47$ sample to approximate the ideal NaFe_{0.5}Cu_{0.5}As system. RIXS measurements were carried out using the ADDRESS beamline at the Swiss Light Source, Paul Scherrer Institute [56,57]. The instrument energy resolution was calibrated using carbon tape and can be well-described by a pseudo-Voigt form, with a width (FWHM) of ≈ 86 meV. Since NaFeAs and its doped variants are highly air-sensitive, all sample preparations and transfers were carried out under either Ar or N₂ flow. Atomically flat pristine surfaces were then post-cleaved inside the chamber under ultra-high vacuum. Momentum transfers are labeled in reciprocal lattice units, using the orthorhombic unit cell [Figs. 1(a) and 1(b)] with $a \approx b \approx 5.59$ Å, $c \approx 6.97$ Å for $x = 0$ and $a \approx b \approx 5.70$ Å, $c \approx 6.88$ Å for $x = 0.47$. Samples were aligned in either (H, H, L) or $(H, 0, L)$ scattering planes. We used a fixed scattering angle of 130° , with grazing incident beam predominantly in the ab -plane of the sample and linearly polarized in the scattering plane (π polarized). The fixed scattering angle results in a fixed total momentum transfer $\mathbf{Q}$, while the in-plane ($\mathbf{Q}_{ab}$) and out-of-plane ($\mathbf{Q}_c$) components can be varied by rotating the sample with respect to the incident beam [Fig. 1(f)]. The accessible range of $\mathbf{Q}_{ab}$ is limited by kinematic constraints [Fig. 1(e)], and the layered nature of NaFe_{1-x}Cu_xAs samples suggest their spin dynamics have minimal dependence on $\mathbf{Q}_c$ (for example, a dispersion of only a few meV along $\mathbf{Q}_c$ is seen for NaFeAs [58]). RIXS spectra were collected at the Fe L_3 -edge ($E_i = 707.9$ eV). All measurements were carried out at $T = 17$ K, well in-

side the magnetically ordered state of both NaFeAs ($T_N \approx 45$ K [20,21]) and NaFe_{0.53}Cu_{0.47}As ($T_N \approx 200$ K [25]). The detector used has a pixel density of ≈ 30.8 meV/pixel (with a subpixeling of 4 we have ≈ 7.7 meV/subpixel), providing a significantly finer sampling of the RIXS spectra compared to previous work on NaFe_{1-x}Co_xAs [49] with ≈ 50 meV/pixel.

Structural twinning common to the FeSCs with low-temperature orthorhombic lattice structures is expected in both measured samples. In the magnetically ordered state of NaFeAs, there are magnetic domains that have antiferromagnetic spin stripes running along the $(q, 0)$ or the $(0, q)$ direction, corresponding to domains that order magnetically at the $(1, 0)$ and $(0, 1)$ positions, respectively. Similarly, in NaFe_{0.53}Cu_{0.47}As, there are domains with Fe chains that run along the $(q, 0)$ or $(0, q)$ direction, also resulting in magnetic order at the $(1, 0)$ and $(0, 1)$ positions, respectively. While the magnetic ordering vectors associated with the two types of domains are separate in momentum space, spin excitations stemming from $(0, 0)$ inevitably overlap [Fig. 1(e)]. Therefore, due to twinning, our data measured along the $(q, 0)$ direction contain contributions from both the $(H, 0)$ and $(0, K)$ directions of a single-domain sample. We note that because each measurement at a particular momentum position is obtained by binning multiple scans taken at randomly selected sample positions, even if structural domain sizes are larger than our beam spot, it remains reasonable to assume that the two domain types contribute similarly to our data. On the other hand, twinning does not affect measurements along the (q, q) direction [Fig. 1(e)].

B. Data analysis

To avoid beam damage, each measurement is repeated multiple times by translating the sample so that no single position is irradiated for more than 5 minutes. The repeated scans are combined and then normalized to their integrated intensity in the energy loss range $[0.4, 10]$ eV, which is dominated by the fluorescence signal, with intensity proportional to the amount of Fe atoms probed in the measurement. Within the energy loss range $[-1, 1]$ eV, we modeled the RIXS spectra (I_{total} as a function of energy loss E) with a linear background (I_{bkg}), an elastic peak [$c\delta(E)$], a fluorescence signal (I_{fluo}), and spin excitations (I_{spin}):

$$I_{\text{total}}(E) = I_{\text{bkg}}(E) + c\delta(E) + I_{\text{fluo}}(E) + I_{\text{spin}}(E). \quad (1)$$

The background I_{bkg} is modeled as a linear function. The fluorescence is modeled as a second-order polynomial:

$$I_{\text{fluo}}(E) = (p_1 E + p_2 E^2)H(E), \quad (2)$$

with $H(E)$ being the Heaviside step function. For consistency, we used the same model to describe the fluorescence for both $x = 0$ and $x = 0.47$ samples, even though the ground state of NaFe_{1-x}Cu_xAs with $x \approx 0.5$ exhibits an electronic gap ~ 100 meV [26,27]. We have carried out additional analysis to show that our conclusions are robust when I_{fluo} is modified to

$$I_{\text{fluo}}(E) = [p_1(E - \Delta) + p_2(E - \Delta)^2]H(E - \Delta), \quad (3)$$

with $\Delta = 0.1$ or 0.2 eV (see Appendix).

The spin excitations are described by a general damped harmonic oscillator function [59]:

$$I_{\text{spin}}(E) = \frac{A}{\pi} \frac{1}{1 - e^{-\beta E}} \frac{2\gamma E E_0}{(E^2 - E_0^2)^2 + (\gamma E)^2}, \quad (4)$$

which in the limit of no damping ($\gamma \rightarrow 0$) and low temperature ($\beta E \gg 1$) is $I_{\text{spin}} = A\delta(E - E_0)$. In addition, the position of zero energy loss ($E = 0$) is also set as a free parameter in our model. The measured RIXS spectra were then fit to our model of I_{total} , after convolving with the instrument energy resolution. We then extracted the values and uncertainties (1 s.d.) of the best fit parameters. It should be noted that fit values of E_0 and the zero energy position are correlated, so that the uncertainties obtained from fitting may be underestimated. This is especially the case for small in-plane momentum transfers, for which the spin excitations and the elastic line strongly overlap, causing the fit values of E_0 to be overestimated and the associated fit uncertainties of E_0 to be underestimated.

C. U(1) slave-spin mean-field theory

To understand the nature of the insulating behavior, we studied the multiorbital Hubbard model for $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$ using the U(1) slave-spin theory [60]. Since Cu ions exhibit +1 valence and are nonmagnetic [25], the local (ionization) potential difference between the Fe and Cu ions is large and will suppress the hopping integral between Fe and Cu sites. This allows us to treat Cu ions in $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$ as vacancies, with Fe atoms ordering into the quasi-1D chains as shown in Fig. 1(b). For the hopping parameters between Fe ions, we use those for NaFeAs [61]. In the calculation, the electron density is fixed to $n = 6$ per Fe ion, to be consistent with the observed +2 valence of Fe. The details of this method is presented in Ref. [60]. To study the metal-to-insulator transition of the model, we calculated the quasiparticle spectral weight, Z_α , in each Fe $3d$ orbital α . The ground state of the system is a Mott insulator if $Z_\alpha = 0$ in all orbitals, and is a metal if $Z_\alpha > 0$ for all orbitals. We have also found an orbital-selective Mott phase (OSMP), corresponding to $Z = 0$ in the d_{xy} orbital, and $Z_\alpha > 0$ for other orbitals. The resulting phase diagram is shown in Fig. 7.

III. RESULTS

A. X-ray absorption spectroscopy

XAS near the Fe L_3 edge measured in total fluorescence yield (TFY) are compared for $\text{NaFe}_{1-x}\text{Cu}_x\text{As}$ ($x = 0$ and 0.47) in Fig. 2(a), after normalizing the spectra so that the maximum and minimum intensities respectively correspond to 1 and 0. Both spectra are dominated by an absorption peak at $E = 707.9$ eV, without an additional peak at $E \approx 710$ eV [62]. This suggests that Fe ions are in the Fe^{2+} state for both compounds, with minimal contributions from the Fe^{3+} state. This conclusion is surprising for the $x = 0.47$ compound, as Cu ions are in the Cu^{1+} state (see Supplementary Information of Ref. [25]) and valence counting suggests Fe ions to be in the Fe^{3+} state, when As ions are assumed to be in the As^{-3} state. Since As-As covalent bonding found in c -axis collapsed iron pnictides [39] is unlikely for the NaFeAs structure, this

FIG. 2. (a) X-ray absorption spectroscopy measurements for $\text{NaFe}_{1-x}\text{Cu}_x\text{As}$ for $x = 0$ and $x = 0.47$. The measured spectra have been normalized so that the intensity maximum (minimum) corresponds to 1 (0). (b) Typical RIXS spectra compared for $x = 0$ [$\mathbf{Q}_{ab} = (0.50, 0)$] and $x = 0.47$ [$\mathbf{Q}_{ab} = (0.51, 0)$] samples. All RIXS spectra are normalized by integrated intensity within the energy loss range [0.4, 10] eV.

suggests that nominally the As ions may be in an unusual $\text{As}^{-2.5}$ state. At present, it is difficult to probe directly the valence state of As. The absorption peak at $E = 707.9$ eV is slightly sharper for the $x = 0.47$ sample compared to $x = 0$, which is a result of its more localized nature.

B. Resonant inelastic x-ray scattering

Since Fe ions are in the Fe^{2+} ($3d^6$) state for both NaFeAs and $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$, in the RIXS process the electronic configuration of the Fe ions are excited from $2P_{3/2}^4 3d^6$ to $2P_{3/2}^3 3d^7$, and then relax back to $2P_{3/2}^4 3d^6$, allowing for the creation of spin excitations with $\Delta S = 1$. Figure 2(b) compares representative RIXS spectra for the $x = 0$ [$\mathbf{Q}_{ab} = (0.50, 0)$] and 0.47 [$\mathbf{Q}_{ab} = (0.51, 0)$] samples over a broad energy transfer range. As can be seen, broad fluorescence peaks are seen for both samples. The presence of clear differences indicates a significant modification of the electronic structure upon heavy Cu-substitution in NaFeAs [25–27,29]. For energies less than 0.5 eV, an additional inelastic peak can be resolved, which can be attributed to spin excitations. The intensity of this feature is more prominent in the $x = 0.47$ sample, with the RIXS spectra normalized to integrated intensity in the energy loss range [0.4, 10] eV. This suggests that the spectral weight of spin excitations per Fe atom is substantially larger in the $x = 0.47$ compound. The elastic peak is also more prominent in the $x = 0.47$ sample, which is likely caused by stronger Laue monotonic scattering [63] due to increased disorder.

To focus on the spin dynamics, we analyzed our RIXS data within an energy window of $[-1, 1]$ eV, with representative scans and the corresponding fits summarized in Fig. 3. The green solid lines represent the results of fits to the fluorescence on top of a linear background ($I_{\text{bkg}} + I_{\text{fluor}}$), and the shaded areas are either damped harmonic oscillators that capture the spin excitations (I_{spin}) or elastic peaks. As can be seen, all scans are well-described by our model of I_{total} , allowing the intensity of the spin excitations I_{spin} to be separated. Figure 8 in Appendix shows a comparison between data and fit I_{spin}

FIG. 3. RIXS spectra for $\text{NaFe}_{1-x}\text{Cu}_x\text{As}$ with $x = 0$ and 0.47 . Each column of plots corresponds to measurements done for either $x = 0$ or 0.47 , and for $\mathbf{Q}_{ab}$ along either $(q, 0)$ or (q, q) . $\mathbf{Q}_{ab}$ is labeled inside each panel. In each panel, the measured data points (blue symbols), total fit intensity I_{total} (red line), $I_{\text{bkg}} + I_{\text{flu}}$ (green line), I_{spin} (light blue shaded area), and the elastic peak (light gray shaded area) are presented.

after the fit background, elastic peak, and fluorescence have been subtracted.

Since our data are normalized using the fluorescence peak, it is meaningful to compare quantitatively the intensity of spin excitations as a function of $\mathbf{Q}_{ab}$ and doping x . Color-coded and interpolated intensities of spin excitations for the $x = 0$ and 0.47 samples are compared in Fig. 4. Overall, the spin excitations appear more intense in the $x = 0.47$ sample [note the different color scales in panels (a) and (b) compared to (c) and (d)]. A quantitative comparison of the spin excitation intensities is presented in Fig. 5(c), through the fit parameter A ($I_{\text{spin}} = A\delta(E - E_0)$ as $\gamma \rightarrow 0$). As can be seen, spin excitations are clearly more intense in $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ compared to NaFeAs , with the difference being more prominent near the zone center. The observation of more intense spin excitations in $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ is consistent with its larger ordered magnetic moment [25]. Intensities of spin excitations increase with the increase of momentum transfer, which is a result of RIXS probing the Brillouin zone centered around $(0,0)$. This is distinct from INS measurements, which probe the Brillouin zones near $\mathbf{Q}_{\text{AF}} = (1, 0)$ or $(0, 1)$, where intensities of spin excitations typically decrease when moving away from $\mathbf{Q}_{\text{AF}}$ [42]. Moreover, Fig. 4 suggests that spin excitations in both NaFeAs and $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ are dispersive, confirmed by energies of E_0 extracted from our fits (red symbols).

To further quantitatively compare the spin excitations in the two studied samples, fit results of E_0 and $\gamma/2$ are summarized in Figs. 5(a) and 5(b), as a function of the in-plane momentum transfer $\mathbf{Q}_{ab}$. As can be seen in Fig. 5(a), spin excitations in NaFeAs are systematically more energetic compared to those in $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$. While the dispersions are almost isotropic for NaFeAs along the (q, q) and $(q, 0)$ directions, in

FIG. 4. Color-coded and interpolated intensities of spin excitations for NaFeAs along (a) (q, q) and (b) $(q, 0)$, and for $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ along (c) (q, q) and (d) $(q, 0)$. Red symbols are E_0 extracted from our fitting. The intensities of spin excitations are obtained from our data, after subtracting fits to I_{flu} , I_{bkg} and the elastic peak (as done for data in Fig. 8).

FIG. 5. Fit results of (a) E_0 , (b) $\gamma/2$, and (c) A , compared for NaFeAs and NaFe_{0.53}Cu_{0.47}As.

NaFe_{0.53}Cu_{0.47}As the dispersion along $(q, 0)$ is clearly more energetic compared to (q, q) . $\gamma/2$, which parametrizes damping, is compared in Fig. 5(b). While similar damping rates are obtained for $|\mathbf{Q}_{ab}| \lesssim 0.3 \text{ \AA}^{-1}$, spin excitations in the $x = 0.47$ sample become clearly less damped compared to those in NaFeAs for $|\mathbf{Q}_{ab}| \gtrsim 0.3 \text{ \AA}^{-1}$. E_0 and $\gamma/2$ in Figs. 5(a) and 5(b) are plotted against the same vertical axis, which allows a direct comparison of the two quantities. This is important as spin excitations with a well-defined propagating energy can be assigned only when $\gamma/2 < E_0$ (underdamped), since when $\gamma/2 > E_0$ the spin excitations become overdamped and are nonpropagating [59]. As can be seen in Figs. 5(a) and 5(b), $\gamma/2 < E_0$ is satisfied for all measurements in both $x = 0$ and $x = 0.47$ samples (within fit uncertainties). Our results suggest that although significant damping is present in both samples, the spin excitations remain underdamped, and can be described as spin waves associated with their respective magnetically ordered ground states.

Given that Fe and Cu atoms order into chains in the ideal NaFe_{0.5}Cu_{0.5}As structure [Fig. 1(b)] [25], spin excitations in our $x = 0.47$ sample should be quasi-1D. The dispersion of spin waves in a 1D antiferromagnetically ordered spin chain, with two spins in the unit cell along the chain direction (the K -direction in reciprocal space), is described within classical linear spin wave theory by

$$E(\mathbf{Q}) = 2SJ \sin(K\pi), \quad (5)$$

with J being the nearest-neighbor exchange coupling and S being the size of the effective spin. For a quasi-1D system, long-range order is only possible when there are exchange interactions between the chains, which will add H and L dependencies to $E(\mathbf{Q})$. Nonetheless, it is reasonable to assume that J is the dominant interaction and spin waves probed in the energy scale of RIXS are mostly determined by J . Given that the (q, q) direction is unaffected by twinning, we fit its dispersion using the 1D model and obtained $SJ = 79.4(6) \text{ meV}$ [Fig. 6(a)]. This value of SJ is then used to obtain the dispersion along the Fe chain direction [the $(0, K)$ direction, solid line in Fig. 6(b)], in comparison with our measurements along the $(q, 0)$ direction [symbols in Fig. 6(b)]. As can be seen, the measured dispersion appears significantly lower in energy, which results from twinning. This is because the $(H, 0)$ direction is perpendicular to the Fe chains and exhibits spin excitations at considerably lower energies compared to the $(0, K)$ direction, and since our $(q, 0)$ measurements con-

tain contributions from both $(H, 0)$ and $(0, K)$ directions, the measured energies along $(q, 0)$ are lower compared to what's expected for $(0, K)$. We note that due to strong quantum fluctuations in 1D, while the dispersion of spin excitation is well-described by Eq. (5), the factor 2 is replaced by π for $S = 1/2$ [64] and ≈ 2.8 for $S = 1$ [65]. This means that the extracted values of J based on classical linear spin wave theory could be overestimated by $\approx 57\%$ for $S = 1/2$ and $\approx 40\%$ for $S = 1$. In contrast, a much smaller overestimation is expected in two dimensions ($\approx 18\%$ for $S = 1/2$ on a square lattice [3]).

While spinons dominate the excitation spectrum of an ideal $S = 1/2$ antiferromagnetic spin chain, spin waves dominate the magnetically ordered phase induced by inter-chain interactions [66]. The contribution from spinons also becomes less important for $S > 1/2$, and if spinons are present in NaFe_{0.53}Cu_{0.47}As, it would be challenging to distinguish them

FIG. 6. (a) Fit to a classical 1D spin chain model, for the dispersion of spin excitations in NaFe_{0.53}Cu_{0.47}As along (q, q) , resulting in $SJ \approx 80 \text{ meV}$. (b) Comparison of expected dispersion along $(0, K)$ (along the Fe chains) in NaFe_{0.53}Cu_{0.47}As ($SJ = 79.4 \text{ meV}$) with the measured dispersion along $(q, 0)$. Comparisons of the dispersion of spin excitations from our measurements with previous results on BaFe₂As₂ [46], NaFeAs [49], and FeSe [53], along (c) (q, q) and (d) $(q, 0)$.

from the fluorescence. For the points closest to the zone center $Q_{ab} = (0, 0)$ in Figs. 6(a) and 6(b), the data appear to deviate from Eq. (5). This may suggest the presence of a sizable zone-center spin gap, or it may result from an overestimate of E_0 when its intrinsic value is small (as discussed in Sec. II B.). INS measurements which probe spin excitations at the $(1,0)/(0,1)$ zone center would be able to distinguish these two scenarios.

We compare our RIXS results on $\text{NaFe}_{1-x}\text{Cu}_x\text{As}$ ($x = 0$ and 0.47) with previous results on BaFe_2As_2 [46], NaFeAs [49] and FeSe [53] in Figs. 6(c)–6(d). We find our results on NaFeAs to be consistent with previous measurements [49], within experimental uncertainties. Along the (q, q) direction, spin excitations in FeSe are the most energetic, followed by those in BaFe_2As_2 , NaFeAs and $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ [Fig. 6(c)]. Less contrast in the energy of spin excitations is observed along the $(q, 0)$ direction, with $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ being slightly less energetic than the other compounds [Fig. 6(d)].

Starting from NaFeAs and doping Co to span the phase diagram encompassing the superconducting dome, it was shown that high-energy ($\gtrsim 20$ meV) spin excitations exhibit little variation with doping [49,67]. As similar observations were also made for $\text{BaFe}_{2-x}\text{Ni}_x\text{As}_2$ [68], such a behavior should be general for electron-doped FeSCs. Since Cu dopes electrons near the superconducting dome [69,70], we expect high-energy spin excitations in superconducting $\text{NaFe}_{1-x}\text{Cu}_x\text{As}$ to be similar to those in NaFeAs . This means that the softening we observe in $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ likely occurs when doping well beyond the superconducting dome.

IV. DISCUSSION AND CONCLUSION

As Cu was shown to have +1 valence and to be nonmagnetic in $\text{NaFe}_{1-x}\text{Cu}_x\text{As}$ when $x \approx 0.5$ (see Supplementry Information of Ref. [25]), valence counting suggests Fe ions to have a 3+ valence and correspond to a $n = 5$ state. The present findings instead indicate Fe ions having a 2+ valence and remains in a $n = 6$ state upon Cu-doping, similar to NaFeAs . This is consistent with the similar local atomic environment found in the two cases [Figs. 1(c) and 1(d)], and suggests that As ions have an unusual -2.5 valence. Therefore, even though As-As covalent bonding along the c axis as in BaCu_2As_2 [39] is not possible, a change of As nominal valence in $\text{NaFe}_{1-x}\text{Cu}_x\text{As}$ occurs upon Cu-substitution ($\text{As}^{3-} \rightarrow \text{As}^{2.5-}$), and is associated with a reduction of the c -axis lattice parameter ($c = 6.97 \text{ \AA} \rightarrow c = 6.88 \text{ \AA}$). It appears that the holes contributed through Cu doping reside on the As sites, rather than the Fe sites. This is analogous to the hole-doped cuprates, in which the doped holes reside on the O sites rather than the Cu sites. This charge transfer physics deserves further theoretical and experimental investigations.

The nearest-neighbor exchange coupling $SJ \approx 80$ meV obtained within classical linear spin wave theory for $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ can be compared against effective exchange couplings obtained for the parent compounds of FeSCs. A comparison between the magnetic structures of NaFeAs and $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$ [Figs. 1(a) and 1(b)] shows that the latter can be obtained by replacing half of the Fe ions in NaFeAs by nonmagnetic Cu ions (and an in-plane 90° rotation of spins), thus there is a correspondence between SJ_{1a}

in NaFeAs and SJ in $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$. SJ_{1a} for archetypal parent compounds of FeSCs are ≈ 40 meV for NaFeAs [44], ≈ 59 meV for BaFe_2As_2 [71], ≈ 50 meV for CaFe_2As_2 [72] and ≈ 31 – 39 meV for SrFe_2As_2 [73]. SJ in our $x = 0.47$ sample is clearly larger than SJ_{1a} in parent compounds of the FeSCs (the larger bandwidths of spin excitations in the latter include contributions from SJ_{1b} and SJ_2), within classical linear spin wave theory. The larger value of SJ in $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ could be the result of a larger exchange coupling J , a larger S or stronger quantum fluctuations (which leads to a larger overestimation of SJ within classical linear spin wave theory). To differentiate between these possibilities, it would be desirable to map out magnetic excitations over the Brillouin zone using inelastic neutron scattering, which allows S and J to be independently determined [42]. Once S is determined, the overestimation of J due to quantum fluctuations can also be corrected for.

Density functional theory (DFT) [25,29] and DFT+dynamical mean field theory (DMFT) calculations [27] suggest $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$ to be metallic in the paramagnetic state, while experimentally semiconducting/insulating transport persists above $T_N \approx 200$ K. This difference may result from strong electronic correlations not fully captured by DFT and DFT+DMFT calculations [25,29], which results in $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$ being a Mott insulator. Alternatively, it has been suggested that short-range spin correlations persist above T_N , and $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$ is a Slater insulator. Our finding of $SJ \approx 80$ meV suggests the dominant exchange interaction energy is substantially larger than $k_B T_N$, and implies the presence of spin fluctuations above T_N . Ideally, to differentiate whether $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$ is a Mott insulator or a Slater insulator, its transport properties for $k_B T \gg J$ should be studied; however, since $k_B J$ is comparable to the melting temperature of $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$, this is difficult to achieve experimentally.

To shed light on the nature of the insulating state of $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$, we calculated the theoretical phase diagram of $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$ using U(1) slave-spin mean field theory (with Fe ions in the $n = 6$ state), with results shown in Fig. 7. Consistent with previous studies of multiorbital models [12,13], we find that for $n = 6$ the Mott insulating state survives in a significantly smaller parameter space, compared to half-filling ($n = 5$). Using the band renormalization factor obtained from ARPES measurements for NaFeAs [74], we estimated the physical regime of U and J_H for NaFeAs [25]. Given the similar local environment and valence of Fe ions in NaFeAs and $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$, this regime of U and J_H is then extended to the latter compound. As can be seen, while the physical regime is entirely inside the Mott insulator state of $n = 5$, it is only partially inside the Mott insulating state of $n = 6$.

Our theoretical results suggest that depending on the precise values of U and J_H , $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$ may either be in a Mott insulating state or a orbital-selective Mott insulating state, with the Slater mechanism relevant for the insulating transport behavior in the latter case. It should be emphasized that in both scenarios, strong electronic correlations are essential for the insulating behavior in $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$. Near the boundary that separates the two cases, we expect a crossover in Mott-type and Slater-type behavior, where

FIG. 7. Theoretical phase diagram of $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$. The shaded gray area is the expected physical regime that the system resides in. Depending on the values of Hubbard repulsion U and Hund's coupling J_H , the system may be a metal, an orbitally selective Mott phase (OSMP), or a Mott insulator (MI). For a fixed J_H/U , the system may experience an orbitally selective Mott transition ($U = U_{\text{OSMT}}$) and a Mott transition ($U = U_{\text{MT}}$), with the increase of U . The line of U_{OSMT} for $n = 5$ is similar to that of $n = 6$ [25].

distinctions between the two are blurred. $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$ is thus a rare example of a $n = 6$ multiorbital correlated insulator continuously connected to unconventional superconductivity, similar to BaFe_2S_3 and BaFe_2Se_3 [15,17,18]. In the latter compounds, the semiconducting/insulating behavior under ambient pressure was attributed to Mott physics

[16,75–77] or a Slater mechanism [78]. It is interesting to note the RIXS spectra of BaFe_2Se_3 are dominated by dd -excitations, which are typically strongly suppressed in the iron pnictides [47], this suggests a larger U in BaFe_2Se_3 compared to the iron pnictides. Similar crossover between Mott-type and Slater-type insulating behavior has been discussed for the iridates Sr_2IrO_4 [79–81] and $\text{Nd}_2\text{Ir}_2\text{O}_7$ [82].

As demonstrated using INS [83] and other techniques [84], it should be possible to detwin NaFeAs (or other parent compounds of FeSCs) by applying a small strain in RIXS experiments. For $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$, as twinning is due to Fe-Cu ordering already present at room temperature, it is unlikely strain will have a similar detwinning effect. Nonetheless, it is conceivable that Fe-Cu ordering may disappear at a higher temperature. Applying strain above such a temperature and cooling to room temperature could lead to a detwinned sample. It may be desirable to pursue such a strategy in heavily doped $\text{NaFe}_{1-x}\text{Cu}_x\text{As}$ to reveal the system's in-plane anisotropic physical properties using RIXS and other experimental probes.

In conclusion, we show that Fe ions in $\text{NaFe}_{1-x}\text{Cu}_x\text{As}$ remains in a $n = 6$ state for both $x = 0$ and 0.47 . RIXS measurements demonstrate the presence of underdamped dispersive spin excitations in both cases. Compared to NaFeAs , spin excitations in $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ are slightly softened in energy but significantly enhanced in intensity. In addition, the dispersion of spin excitations is consistent with arising from localized quasi-one-dimensional magnetic moments. Our results suggest that $\text{NaFe}_{0.5}\text{Cu}_{0.5}\text{As}$ likely resides in a crossover regime between Mott-type and Slater-type insulating behavior, and strong electronic correlations are essential for realizing its insulating state.

FIG. 8. Similar scans as in Fig. 3, but showing only I_{spin} (red lines and light blue shaded areas). Fit values of I_{bkg} , I_{fluo} , and the elastic peak have been subtracted from the measured data (blue symbols).

FIG. 9. Comparison of fit results for the fit parameters (a) E_0 , (b) $\gamma/2$, and (c) A , with the introduction of a gap Δ in I_{fluo} [Eq. (3)]. The fits are for data on $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ along (q, q) .

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APPENDIX A: COMPARISON BETWEEN DATA AND FIT SPIN EXCITATIONS

To allow a direct comparison between our data and fit spin excitations, fits to I_{fluo} , I_{bkg} and the elastic peak are subtracted from Fig. 3 and shown in Fig. 8. This allows the fit I_{spin} to be directly compared with experimental data. As can be seen, good fits to the model of I_{spin} have been achieved in all cases.

APPENDIX B: EFFECT OF A GAP IN THE FLUORESCENCE ON FIT RESULTS

Since $\text{NaFe}_{1-x}\text{Cu}_x\text{As}$ with $x \approx 0.5$ is a semiconductor with a lowest electronic gap ≈ 0.1 eV [27], we considered modeling its fluorescence using a gapped form [Eq. (3)], which reduces to Eq. (2) when the gap Δ becomes 0. All of our analysis in the main text were fit using Eq. (2) for I_{fluo} . In Fig. 9, we compare fit results of E_0 , $\gamma/2$ and A with $\Delta = 0, 0.1$, and 0.2 eV, for $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ along (q, q) . With the increase of Δ , the fit values of E_0 , $\gamma/2$ and A all increases, with the change being rather small for $\Delta = 0.1$ eV. Similar results are also obtained for data along $(q, 0)$.

This analysis suggests that the experimentally obtained charge gap ≈ 0.1 eV is unlikely to significantly affect our fit results. Moreover, our conclusion of enhanced magnetic fluctuations in $\text{NaFe}_{0.53}\text{Cu}_{0.47}\text{As}$ compared to NaFeAs remains robust with the increase of Δ .

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