Exotic transition in the three-dimensional spin-liquid candidate \( \text{Tb}_2\text{Ti}_2\text{O}_7 \)

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The insulator pyrochlore \( \text{Tb}_2\text{Ti}_2\text{O}_7 \) is a three-dimensional spin liquid candidate: the strength of the magnetic interaction would normally induce order at \( \approx 20 \) K, but according to published muon-spin relaxation and neutron diffraction measurements, it is still in a correlated paramagnetic state down to a temperature of 0.05 K. Our detailed experimental investigation shows that an exotic transition takes place at \( T_t \approx 0.15(2) \) K. It is characterized by an anomaly in the muon precession frequency shift but not in the specific heat, which nevertheless reveals the signature of degrees of freedom at very low energy. It might be associated with a cooperative Jahn-Teller transition. The robustness of the experimental results is discussed.

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The family of insulating rare-earth cubic compounds for which the magnetic rare-earth sublattice is composed of a network of corner-sharing regular tetrahedra exhibits a rich variety of magnetic ground states.

For example, when the rare-earth magnetic ions are characterized by a very strong Ising magnetic anisotropy fixed along the local [111] axis and coupled by a net ferromagnetic interaction, the spin-ice ground state is formed.2 The spin-ice state is characterized by a huge magnetic degeneracy as revealed by the large residual entropy. Such a ground state has been found for the pyrochlores \( \text{Ho}_2\text{Ti}_2\text{O}_7, 3 \text{ Dy}_2\text{Ti}_2\text{O}_7, 4 \text{ Ho}_2\text{Sn}_2\text{O}_7, 5 \) and spinel \( \text{CdEr}_2\text{Se}_4. 6 \) It has been predicted that the magnetic excitations of these spin-ice systems can be described as effective magnetic monopoles.7 Signatures of these emergent particles have been reported.7-13 On the other hand, when the net interaction is still ferromagnetic, but the magnetic moments are small and the crystal-field anisotropy is of the \( XY \) type, as for \( \text{Yb}_2\text{Ti}_2\text{O}_7, \) a first order transition in the spin dynamics is observed with a low-temperature ground state characterized by short-range correlations.14 Other examples of magnetic ground states for pyrochlore rare-earth compounds have been recently discussed.1

Within the whole family of these systems two compounds stand alone: \( \text{Tb}_2\text{Ti}_2\text{O}_7 \) and \( \text{Tb}_2\text{Sn}_2\text{O}_7. \) The analysis of their specific heat leads to the conclusion that their crystal-field ground state is a singlet, i.e., the \( \text{Tb}^{3+} \) magnetic moments are exchange induced.15 This conclusion is supported by the results of inelastic neutron scattering which evidences the splitting of the ground state at low temperature.16 More recent measurements confirm it in the case of the stannate.17 This evidence has recently been disputed in Ref. 18 in the case of the titanate. We note that this study fails to find the inelastic neutron scattering line around 0.2 meV in zero field which yet was present in previous measurements.18,19 No indication about the characterization of the sample used in Ref. 18, e.g., by specific heat measurement at low temperature, is provided. Besides, the authors argue that the lifting of the degeneracy of the ground state doublet deduced from the entropy variation is due to the presence of magnetic correlations. Unfortunately, no attempt is made to check whether the observed splitting between the lowest two energy levels is consistent with the magnitude of the exchange energy between the \( \text{Tb}^{3+} \) ions in the pyrochlore structure.

In \( \text{Tb}_2\text{Ti}_2\text{O}_7 \) the magnetic susceptibility, muon-spin relaxation (\( \mu \text{SR} \)), and neutron diffraction measurements do not detect any signature of a magnetic ordering down to 0.05 K, despite strong superexchange interactions,20,21 i.e., it is a spin liquid candidate system or a fluidlike magnetic system.22,23 Magnetic order with a strong dynamical character occurs below \( T_c \approx 0.88 \) K in the stannate.24 This picture was first proposed in Ref. 25 and was subsequently confirmed.26-29

Here we report specific heat, \( \mu \text{SR} \), and quasielastic neutron scattering measurements performed on single crystals of \( \text{Tb}_2\text{Ti}_2\text{O}_7 \). As the compound is cooled down, a strongly correlated paramagnetic regime is first entered at \( T_c \approx 2 \) K, followed by an exotic transition at \( T_t \approx 0.15 \) K. Below this temperature new degrees of freedom are detected.

The organization of this paper is as follows. In Sec. I we describe the growth of the single crystals and the experimental methods used in the present work. Section II presents our experimental data and their analysis. The next section (Sec. III) discusses the robustness of our results. Finally a summary of our result is given in Sec. IV. Three appendices complete the description of our work.

I. EXPERIMENTAL

Crystals of \( \text{Tb}_2\text{Ti}_2\text{O}_7 \) were prepared with different starting oxides and growth velocity under either argon or oxygen gas.30 The best quality crystals, i.e., the ones with the lowest residual entropy, were obtained starting from compacted polycrystalline \( \text{Tb}_2\text{Ti}_2\text{O}_7 \) rods prepared using \( \text{TiO}_2 \) and \( \text{ Tb}_2\text{O}_3 \) powders. The crystals were grown under oxygen atmosphere by the traveling solvent floating zone technique with a growth velocity of 7 mm/h, as done previously for \( \text{Gd}_2\text{Ti}_2\text{O}_7. 31 \) Specific heat data were recorded above 0.4 K with a Quantum Design physical property measurement system (PPMS) using a relaxation method. At lower temperatures and in an overlapping range up to 0.8 K, the measurements were performed in a \( ^3\text{He}^-^4\text{He} \) dilution refrigerator, also using a relaxation method with a homemade calorimeter. The spin dynamics was studied.
by positive muon-spin relaxation (µSR) and quasielastic neutron scattering at the MuSR and IN12 spectrometers of the ISIS facility (Rutherford Appleton Laboratory, Chilton, United Kingdom) and the Institut Laue Langevin (Grenoble, France), respectively. The µSR frequency shifts were measured at the low temperature facility (LTF) and general purpose surface-muon (GPS) instruments of the Swiss Muon Source at the Paul Scherrer Institute (Villigen, Switzerland).

II. EXPERIMENTAL RESULTS

The results for the static magnetic properties of Tb2Ti2O7 as probed by µSR and specific heat measurements are presented in Fig. 1. In this µSR measurement, under the action of an external field applied to the sample and perpendicular to the muon polarization, the spins of the implanted muon precess at a frequency \( v_\mu = \gamma_\mu B_\mu \), where \( B_\mu \) is the local field at the muon site and \( \gamma_\mu = 851.6 \text{ Mrad s}^{-1} \text{ T}^{-1} \) the muon gyromagnetic ratio. The frequency shift shown in Fig. 1(a) is defined as \( \Delta v/v_{\text{ext}} \), where \( \Delta v = v_\mu - v_{\text{ext}} \) and \( v_{\text{ext}} = \gamma_\mu B_{\text{ext}} \).

An anomaly is observed in this shift at a temperature of 0.15 (2) K that we define as \( T_c \). A minimum value for the electronic specific heat is observed at approximately the same temperature [see inset of Fig. 1(b)]. Looking at the results of longitudinal µSR measurements probing spin dynamics in Tb2Ti2O7 shown in Fig. 2(a) and to be commented on below, no signature of \( T_c \) is found, in agreement with published results.20,32

The marked extremum of \( \Delta v/v_{\text{ext}} \) at \( T_c \) makes the lack of an anomaly in longitudinal µSR and specific heat measurements very paradoxical indeed. One would expect to observe µSR oscillations at a magnetic phase transition, or at least a partial loss of the signal if the oscillations are too fast or too strongly damped to be detected. There is one material which represents an exception to this rule: the aforementioned compound Tb2Sn2O7.25 The local field at the muon site evolves in a time shorter than the muon-spin precession time. This means that magnetic modes fluctuating in the 10–100 s time range are present below \( T_c \), as confirmed by neutron scattering.29 For Tb2Ti2O7, the behavior of \( \Delta v/v_{\text{ext}} \) below \( T_c \) seems at first glance, consistent with the system entering a spin-glass ground state.34 However, the presence of a marked minimum in the specific heat and the persistent spin dynamics down to temperatures as low as 0.06 K, as evidenced by the significant value of the spin-lattice relaxation rate \( \lambda_Z \) [Fig. 2(a)], contradicts the assumption that the transition is spin-glass-like at \( T_c \).

The maximum strength of the applied field for the measurements of \( \Delta v/v_{\text{ext}} \) is appreciable with respect to the measured molecular field. Referring to the value found in the sibling compound Tb2Sn2O7, the applied field is about one fifth.15 This can explain the high sensitivity of \( \Delta v/v_{\text{ext}} \) to the field magnitude [Fig. 1(a)].

While no anomaly is present in the spin dynamics at \( T_c \), a change of regime in the dynamics occurs at a temperature an order of magnitude higher. This is clearly seen from the muon-spin relaxation and quasielastic neutron scattering experiments that we describe now.

Weak longitudinal field muon-spin relaxation spectra on crystals of Tb2Ti2O7 have been recorded. Contrary to previous results,20,32 the exponential line shape does not provide a good account of the data over the whole investigated temperature range; see Appendix B for a discussion. This is especially manifest at low temperature. An exponential-power relaxation function \( P_Z(t) = \exp[-(\lambda_Z t)^\beta] \) is found to properly fit the data. Figure 2(a) shows the temperature dependence of the muon-spin-lattice relaxation rate \( \lambda_Z \) and of the exponent \( \beta \). \( \lambda_Z(T) \) exhibits little thermal dependence outside the temperature interval between 1 and 5 K. On the contrary, it exhibits a marked increase on cooling between about 5 and 1 K; this is the signature of a slowing down of the spin dynamics.35 Roughly in the same interval, the exponent \( \beta \) increases from a high-temperature value of \( \approx 0.9 \) to \( \approx 1.2 \) below 1 K. In general terms, in the case of fast dynamics one expects the spectra to be exponential, i.e., \( \beta = 1 \), while this exponent is \( \beta = 2 \) for static or quasistatic fields. We interpret the increase of \( \beta \)
We complement our data with published results from Yasui et al. Exponential growth of the quasielastic neutron scattering linewidth measured for the wave vector $(0,0,2.1)$ in reduced units. In panel (b) we display the temperature dependence of the spin-lattice relaxation rate $\lambda_Z$ below which Tb$_2$Ti$_2$O$_7$ becomes a collective paramagnet, i.e., it is in a paramagnetic state characterized by strong correlations. While $\lambda_Z$ is independent of the temperature above $T_{cp} \simeq 2$ K, it decreases below this temperature. Interestingly, $T_{cp}$ is in the temperature range where $\lambda_Z(T)$ and $\beta(T)$ signal the change of regime in the spin dynamics. $T_{cp}$ can be interpreted as the crossover temperature below which Tb$_2$Ti$_2$O$_7$ becomes a collective paramagnet, i.e., it is in a paramagnetic state characterized by strong correlations.

In Fig. 3 we display the variation of the electronic entropy. It is deduced from the measured specific heat to which the nuclear and phonon contributions have been subtracted (see Appendix A).

The fact that the entropy variation is larger than $R \ln(2)$ confirms that the degeneracy of the trigonal crystal-field ground state is lifted at low temperature. Relative to the previous work of Chapuis et al., thanks to the extension of the specific heat measurement below 0.4 K, here we determine that there is a weak residual entropy at 0.06 K, the lowest measured temperature (inset of Fig. 3). A plateau in the electronic entropy $S_{elec}$ per mole of terbium in Tb$_2$Ti$_2$O$_7$. The entropy variation has been computed from $C_{elec}(T)$ and has been shifted to match the prediction of the model described below in the temperature range 15–20 K. The prediction shown as a dashed line is for a crystal-field scheme with energy levels lying at 0, 2, 19.5, 21.9, 123, and 171 K in units of temperature. The value of the first excited level has been determined for the entropy to be consistent to the experimental data. The splitting between the levels at 19.5 and 21.9 K was computed to be consistent with the splitting between the ground and first excited states. The last two values for the energy levels (123 and 171 K) result from the predictions for recently determined crystal-field parameters. Note that all these energy levels match very well the transitions which have been observed by inelastic neutron scattering. The subsequent levels are above 400 K and do not affect the entropy in the displayed temperature range. The inset shows the low-temperature part of the experimental data.

FIG. 3. (Color online) Temperature dependence of the entropy of electronic origin $S_{elec}$ per mole of terbium in Tb$_2$Ti$_2$O$_7$. The entropy variation has been computed from $C_{elec}(T)$ and has been shifted to match the prediction of the model described below in the temperature range 15–20 K. The prediction shown as a dashed line is for a crystal-field scheme with energy levels lying at 0, 2, 19.5, 21.9, 123, and 171 K in units of temperature. The value of the first excited level has been determined for the entropy to be consistent to the experimental data. The splitting between the levels at 19.5 and 21.9 K was computed to be consistent with the splitting between the ground and first excited states. The last two values for the energy levels (123 and 171 K) result from the predictions for recently determined crystal-field parameters. Note that all these energy levels match very well the transitions which have been observed by inelastic neutron scattering. The subsequent levels are above 400 K and do not affect the entropy in the displayed temperature range. The inset shows the low-temperature part of the experimental data.

III. ROBUSTNESS OF OUR RESULTS

The robustness of our results has been tested. Basically, the spin dynamics as displayed in Fig. 2(b) of the main text is sample independent: two samples of completely different origin give fully consistent results. Our longitudinal field $\mu$SR data measured on two different crystals are also consistent.

On the other hand, some magnetic properties are partly sample dependent. The temperature of the kink in the frequency shift for a sample with a larger residual entropy is changed from 0.15 K down to about 0.10 K. Interestingly, a branching between zero-field and field-cooling in alternating current susceptibility data was reported in the past at $\approx 0.10$ K by Luo et al. Beside the crystals mentioned so far, we have grown another one with a growth velocity of 3 mm/h. Its...
specific heat displays peak at about 0.37 K. This result is consistent with the observation of Hamaguchi et al. for a crystal of an unspecified growth velocity.\textsuperscript{37} A polycrystalline sample with such a specific heat peak has been recently studied by inelastic neutron scattering.\textsuperscript{38} The spin dynamics as probed by this experiment seems to suggest that it changes in nature at the peak temperature.

**IV. SUMMARY**

In summary, while \(\text{Tb}_2\text{Ti}_2\text{O}_7\) enters a correlated paramagnetic regime at \(T_{\alpha} \approx 2\) K, characterized by a pronounced slowing of the magnetic fluctuations, we have observed an exotic transition at \(T_{\alpha} = 0.15\) (2) K which is not spin-glass-like. It manifests itself through an anomaly in the \(\mu\)SR frequency shift (magnetic measurement) and the presence of unconventional excitations detected by specific heat below \(T_{\alpha}\). The magnetic transition at \(T_{\alpha}\) is of quantum nature, since \(\text{Tb}_2\text{Ti}_2\text{O}_7\) is an exchange-induced magnet with a small splitting of the first two crystal-field energy levels.\textsuperscript{15} This transition could be associated with a cooperative Jahn-Teller transition, which has been suggested to exist at \(\approx 0.1\) K. The inference arose from the observation of the temperature dependence of the elastic modulus.\textsuperscript{39} The observation of a broadening of Bragg reflections below \(\approx 20\) K in recent x-ray scattering experiments was interpreted as a precursor of the Jahn-Teller transition.\textsuperscript{40} However, this precursor effect seems sample dependent.\textsuperscript{41} Spin dynamics is still observed below \(T_{\alpha}\). The magnetic ground state is built up of crystal-field states of the first two crystal-field energy levels.\textsuperscript{15} This transition is the Zeeman and quadrupole interactions, written as \(H_{\text{CEF}} = -\mu_0g_\alpha\mu_B I_\alpha\) and \(H_Q = h\omega_Q[(3(I_z)^2 - (I_z)^2) + \eta(I_y)^2 - (I_y)^2)],\) with \(h\omega_Q = \frac{e^3Q}{4\hbar}\), respectively. In this last formula, \(V_{\alpha}\) is the principal component of the electric field gradient tensor acting on the nucleus, \(\eta\) is the asymmetry parameter, and \(Q = 1.432\) barn is the quadrupole moment of \(^{159}\text{Tb}\). It is here implicitly assumed that the principal axis \(z\) of the electric field gradient is parallel to the local trigonal symmetry axis at the Tb crystalline site coincides with the orientation of the magnetic field acting on the nucleus. This should be a fair approximation if we refer to the results obtained for \(\text{Sm}_2\text{Sn}_2\text{O}_7\).\textsuperscript{24,25} We now proceed to the estimate of \(V_{\alpha}\) using a conventional method.\textsuperscript{43-46} Since \(\text{Tb}_2\text{Ti}_2\text{O}_7\) is an insulator, \(V_{\alpha}\) is the sum of only two terms, i.e., \(V_{\alpha} = V_{\alpha}^{\text{CEF}} + V_{\alpha}^{\text{latt}}\), where the first and the second terms model the \(4f\)-electron and lattice contributions, respectively.

For the first contribution we can write

\[
V_{\alpha}^{\text{CEF}} = -\frac{e^2}{4\pi\varepsilon_0} \theta_2(1 - R_Q) (r^{-3})_{4f} E. \tag{A1}
\]

All the parameters of this equation refer to the \(\text{Tb}^{3+}\) ion. The atomic parameters are the second-order Stevens factor \(\theta_2 = -1/99.47\), the Sternheimer coefficient \(R_Q = 0.12, 48\) and the expectation value of the cube of the inverse distance from the \(^{159}\text{Tb}\) nucleus to the \(4f\) shell. \(V_{\alpha}^{\text{latt}}\) is the expectation value of the quadrupole operator \(3J_z^2 - J(J + 1)\) acting on the \(\text{Tb}^{3+}\) crystal-electric-field (CEF) state: it depends on the ion environment. It is a fair approximation to retain only the lowest two CEF electronic states, since at the temperatures of interest here the population of the other ones is negligible.

We recall that the third CEF state lies at about 20 K in temperature units above the ground state. The first two states \(|\phi_1,\pm\rangle\) are a linear combination of the states \(|\pm\rangle\), namely,

\[
|\phi_1,\pm\rangle = -\sin(\alpha_1/2)|\pm\rangle + \cos(\alpha_1/2)|-\rangle, \quad \text{with} \quad |\pm\rangle = -0.958|\pm0.129| \pm 1\rangle - 0.121|\mp2\rangle + 0.226|\mp5\rangle, \tag{A15}
\]

\(\alpha_1 = \pi/2,\) and \(\alpha_2 = \alpha_1 + \pi.\) We compute \(E = 6.1,\) a value which is actually independent of the mixing angles \(\alpha_2.\) This leads to \(V_{\alpha}^{\text{latt}} = 4.7 \times 10^{31}\) V m\(^{-2}\).

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FIG. 4. Schematic view of the $^{159}$Tb nuclear levels. In the presence of the Zeeman interaction only, the four levels are equidistant. When the quadrupole interaction is included, the two levels in the middle are shifted upward. For the sake of clarity the shift is enlarged in the figure. The actual normalized values for the four levels are 0, 1/3, 2/3, 1 and 0, 0.346, 0.679, 1 for the pure Zeeman case and when the quadrupole interaction is added, respectively.

For the lattice contribution to $V_{zz}$ we have

$$V_{zz}^{\text{latt}} = -rac{4(1 - \gamma_\infty)}{e \theta_2 (r^2)_{1/4} (1 - \sigma_2)} B_2^0,$$

(A2)

The new parameters are the Sternheimer coefficient $\gamma_\infty = -60$, the expectation value of the square distance from the $^{159}$Tb nucleus to the $4f$ electrons, $(r^2)_{1/4} = 0.822$ in atomic units, the screening coefficient of the crystal field $\sigma_2 = 0.6$, and the crystal-field parameter $B_2^0 = -4.93 \times 10^{-23}$ J. Numerically we get $V_{zz}^{\text{latt}} = -8.1 \times 10^{21}$ V m$^{-2}$. Altogether we compute $V_{zz} = -3.3 \times 10^{21}$ V m$^{-2}$. Compared to other compounds the absolute value is quite small. When such a small magnitude, it is legitimate to consider the quadrupolar electric interaction as a perturbation of the Zeeman interaction. In the presence of the sole Zeeman interaction, the Zeeman nuclear eigenstates $|\pm 3/2\rangle$ and $|\pm 1/2\rangle$ are equidistant in energy, as displayed in the left side of Fig. 4. To first order perturbation, the repartition is changed by the quadrupole interaction to the one shown in the right side. Note that the energy shift of the levels is independent of $\eta$.

In the pyrochlore compounds, titanium is nonmagnetic and the contribution of the two non-spinless titanium nuclei can be readily estimated from the nuclear splittings measured with a $^{47}$Ti nuclear quadrupole resonance experiment on Dy$_2$Ti$_2$O$_7$: transitions are found by this technique at 4.37 MHz and the double of this value. It is indeed a good approximation to consider the electric field gradient acting on the Ti nuclei in Dy$_2$Ti$_2$O$_7$ and Tb$_2$Ti$_2$O$_7$ to be very close to each other. Then it is easily shown that the overall contribution of the Ti nuclei to the total nuclear specific heat down to 0.06 K is absolutely negligible compared to the Tb one.

The nuclear contribution to the specific heat of Tb$_2$Ti$_2$O$_7$ shown in Fig. 1(b) of the main text has been computed with an overall splitting of the $^{159}$Tb levels of $3h\omega_{Zee} = 0.0191$ (4) meV. In principle our experimental data do not provide a definite value for $3h\omega_{Zee}$ but as a matter of fact, the bounds for $3h\omega_{Zee}$ are quite tight. The higher bound is the value used for the plot. Indeed, if a higher value for $3h\omega_{Zee}$ was used, the electronic specific heat in the 0.1 – 0.2 K range, which is obtained from subtracting the nuclear estimate to the experimental data, would be negative. The lower bound is 0.0172 (4) meV, since any smaller value for $3h\omega_{Zee}$ would result in a negative electronic entropy when $T \to 0$ (see Fig. 3 of the main text).

Interestingly, if the lower bound is retained for $3h\omega_{Zee}$, the electronic specific heat still exhibits a minimum value around $T_c$, i.e., the shape of the temperature variation of $C_{\text{elec}}$ shown in the inset of Fig. 1(b) of the main text is conserved. Basically, in this case only a vertical shift of the data is observed with a minimum value for $C_{\text{elec}}$, which is around 0.4 J/(K mol Tb) at $T_c$ instead of about 0 in Fig. 1(b) of the main text.

Since $\omega_{Zee}$ can be written in terms of the hyperfine field $B_{\text{hyp}}$ as $\omega_{Zee} = \gamma_{\text{hyp}} B_{\text{hyp}}$, where $\gamma_{\text{hyp}} = 64.31$ Mrad s$^{-1}$ T$^{-1}$ is the nucleus gyromagnetic ratio, we find $B_{\text{hyp}} = 142$ T from $3h\omega_{Zee} = 0.018$ (1) meV, a mean value of the two bounds. It would be interesting to compare this value with the one deduced from the ground state magnetic moment using the published hyperfine constant of 40 (4) T/\(\mu_B\). The main physical purpose would be to determine whether the hyperfine field is reduced because of the dynamical nature of the electronic ground state. However, this would require a value for the moment which is still unknown.

**APPENDIX B: EXPERIMENTAL DETAILS FOR MUON-SPIN RELAXATION EXPERIMENTS**

The spin dynamics as probed by the longitudinal $\mu$SR technique consists of measuring the spatial asymmetry $a_0 P_{Z}^{\exp}(t)$ in the muon decay positron distribution. The function $P_{Z}^{\exp}(t)$ which models the evolution of the muon polarization is well described by the sum of two components: $a_0 P_{Z}^{\exp}(t) = a_0 \exp[-(\lambda Z t)^\beta] + a_0 \exp[-(\lambda Z t)^\alpha]$. The exponential-power relaxation function provides an effective model for the relaxation arising from the muons implanted into the sample. It is characterized by the spin-lattice relaxation rate $\lambda Z$ and the exponent $\beta$ ($\beta > 0$). The constant term $a_0 \exp[-(\lambda Z t)^\alpha]$ accounts for the muons which have missed the sample. A longitudinal magnetic field of 13 mT was applied on the sample. This magnetic field strength was chosen, after a series of tests, to be sufficiently strong to quench the relaxation from the nuclear magnetic moments, i.e., the $^{159}$Tb nuclear magnetic moments, but small enough such that the relaxation from the Tb$^{3+}$ magnetic moment is not disturbed too much. Relative to Tb$_2$Sn$_2$O$_7$ for which a pronounced $\lambda Z$ maximum was observed at low field, only a slight maximum is observed (with a maximum increase of 0.2 $\mu$K$^{-1}$) and only for $T \leq 0.4$ K. The values of the $\mu$SR parameters $\beta$ and $\lambda Z$ were found identical within error bars for the three investigated orientations of the field relative to the crystal axes. They were [111], [110], and [100].

Previously measured longitudinal $\mu$SR spectra were analyzed with an exponential relaxation function down to the lowest measured temperature, in contrast to our results. In Fig. 5 we show that the relaxation deviates substantially at low temperature from the previously assumed exponential behavior. We believe that the deviations from the exponential form were missed in the past because of either insufficient statistics in the spectra, or the deviation from the exponential shape was simply not looked for. An exponent with a value above 1 indicates that the measured spin dynamics is not in the motional narrowing limit, i.e., a slowing down of the dynamics is observed.
taking into account different contributions: (i) the elastic part of the figure displays the difference between the data and the best fit for two different values of the exponent $\beta$. For the sake of clarity a difference is magnified by a factor of 3.

APPENDIX C: EXPERIMENTAL DETAILS FOR QUASIELASTIC NEUTRON EXPERIMENTS

Measurements were performed on the cold neutron triple axis spectrometer IN12 installed at the high-flux reactor of the ILL. IN12 was operated with a vertically focusing PG(002) monochromator, a horizontally focusing PG(002) analyzer, and a liquid-nitrogen-cooled Be filter in the scattered beam to remove higher-order neutrons. The final energy was fixed to 3.78 meV and the energy resolution at elastic energy transfer was 0.12 meV (full width at half maximum). Scans were performed in energy with a typical counting time of 90 seconds per point. The sample was mounted such that the $[\hbar\hbar\ell]$ plane was accessible to the measurements.

Our quasielastic neutron scattering data were analyzed taking into account different contributions: (i) the elastic incoherent scattering described by a Gaussian function which is also the resolution function, (ii) a background independent of the temperature and energy transfer, (iii) the inelastic scattering arising from the first crystal-field excited state at a thermal energy of $\sim 2$ K, which is described by the sum of two symmetric Lorentzian functions centered at approximately $\pm 0.2$ meV, and finally (iv) the quasielastic scattering component of electronic origin which is modeled by a Lorentzian function of half-width at half-maximum equal to $\Gamma$. In Fig. 6 we display a quasielastic neutron scattering spectrum recorded at 1.6 K at the scattering vector $(0, 0, 2.1)$ given in reduced units. The different components of the spectrum are explicitly shown.

In addition to our own spectra, we have reanalyzed spectra presented in Ref. 33, since the effect of the crystal-field level at the thermal energy of $\sim 2$ K was not taken into account in the published analysis. Our analysis provides a notably improved account of the experimental data compared to the original fit. The values obtained for $\Gamma$ are compatible with the values of Ref. 33: the additional scattering from the crystal-field levels does influence $\Gamma$ only within error bars.

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EXOTIC TRANSITION IN THE THREE-DIMENSIONAL...


