Magnetic ground state of the frustrated spin-$\frac{1}{2}$ chain compound $\beta$-TeVO$_4$ at high magnetic fields

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Frustrated spin-$\frac{1}{2}$ chains, despite the apparent simplicity, exhibit a remarkably rich phase diagram comprising vector-chiral (VC), spin-density-wave (SDW), and multipolar/spin-nematic phases as a function of the magnetic field. Here we report a study of $\beta$-TeVO$_4$, an archetype of such compounds, based on magnetization and neutron diffraction measurements up to 25 T. We find the transition from the helical VC ground state to the SDW state at $\sim$3 T for the magnetic field along the $a$ and $c$ crystal axes, and at $\sim$9 T for the field along the $b$ axis. The high-field (HF) state, existing above $\sim$18 T, i.e., above $\sim$1/2 of the saturated magnetization, is an incommensurate magnetically ordered state and not the spin-nematic state, as theoretically predicted for the isotropic frustrated spin-1/2 chain. The HF state is likely driven by sizable interchain interactions and symmetric intrachain anisotropies uncovered in previous studies. Consequently, the potential existence of the spin-nematic phase in $\beta$-TeVO$_4$ is limited to a narrow field range, i.e., a few tenths of a tesla below the saturation of the magnetization, as also found in other frustrated spin-$\frac{1}{2}$ chain compounds.

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I. INTRODUCTION

Frustrated spin-$\frac{1}{2}$ chains have been lately drawing considerable attention due to an intriguing magnetic quadrupolar [1–3], i.e., spin-nematic, phase that is predicted to occur in the applied magnetic field just before the magnetization gets saturated [4,5]. This remarkable state features no regular, i.e., dipolar magnetic order, but rather consists of ordered magnetic quadrupoles that are formed out of bound magnon pairs, which condense at the bonds between the neighboring spins [6–8]. As such, this novel state of matter is notoriously difficult to detect experimentally. The excitations of the spin-nematic order, however, break the bound magnon pairs and thus couple to the magnetic field [9,10]. The spin-nematic phase is, therefore, expected to be reflected either in a missing magnetization fraction [11] or in a particular kind of magnetic-excitation dispersion [9,10,12–14]. Unfortunately, the most studied frustrated spin-$\frac{1}{2}$ chain candidate LiCuVO$_4$ has a saturation field of $\sim$40 T [15], which severely hinders the applicable experimental techniques. The experimental reports of the spin-nematic phase are thus limited [11,15–17] and so far have not provided an indisputable proof of its existence in physical systems.

Here we focus on $\beta$-TeVO$_4$ [18,19], which has been recently recognized as a very good realization of a spin-$\frac{1}{2}$ frustrated ferromagnetic chain [20–23]. In this compound, the $V^{4+}$ ($S = 1/2$) magnetic ions are coupled by ferromagnetic nearest-neighbor $J_1 \approx -38$ K and antiferromagnetic next-nearest-neighbor $J_2 \approx -J_1$ exchange interactions mediated by oxygen and oxygen-tellurium-oxygen superexchange pathways, respectively (Fig. 1). The compound undergoes a long-range magnetic ordering below $T_M = 4.6$ K and the experimentally derived phase diagram [Fig. 2(a)] almost exactly matches the theoretically predicted diagram [20]. Namely, the helical ground state, denoted also vector-chiral (VC) state, is at $\sim$3 T succeeded by the spin-density-wave (SDW) state that exhibits additional stripe modulation up to $\sim$5 T and is at $\sim$18.7 T followed by another phase, whose properties are not yet determined. According to the theory, this phase could be a spin-nematic phase, persisting up to saturation of the magnetization at $\sim$21.5 T. The fact that the high-field (HF) phase develops already at moderately high fields of $\sim$18.7 T opens the possibility to explore this phase with neutron scattering experiments that could not have been done for other candidate compounds. These experiments should finally provide firm experimental evidence either in favor or against the existence of the spin-nematic order in $\beta$-TeVO$_4$.

In this work we combine neutron diffraction experiments on $\beta$-TeVO$_4$ in applied magnetic fields up to 25 T with an in-depth high-field magnetization study. The data reveal that the HF phase exhibits long-range incommensurate magnetic order and is thus not the spin-nematic phase that is theoretically predicted for the isotropic frustrated spin-$\frac{1}{2}$ chain. We argue that this is most likely due to sizable interchain exchange interactions and strong symmetric anisotropy of the intrachain interactions, which induce the stripe modulation in the narrow region of the SDW phase [20] and probably also...
help stabilizing the incommensurate magnetic order at high magnetic fields.

II. EXPERIMENT

The single-crystal samples were grown from TeO$_2$ and VO$_2$ powders by chemical vapor transport reaction, using a two-zone furnace and TeCl$_4$ as a transport agent [20,22,23]. Magnetization measurements in pulsed magnetic fields up to 25 T were performed on a 1.6 $\times$ 0.7 $\times$ 0.8 mm$^3$ single crystal at the High Magnetic Field Laboratory, Institute for Materials Research, Sendai, Japan. This sample was cut from a larger sample oriented by neutron diffraction. Neutron diffraction measurements were performed on a 2 $\times$ 3 $\times$ 4 mm$^3$ single crystal. Measurements in magnetic field up to 15 T applied along the $b$ axis were performed on the triple-axis-spectrometer TASP at the Paul Scherrer Institute (PSI), Villigen, Switzerland. An analyzer was used to reduce the background, while the standard ILL orange cryostat was used for cooling. Measurements in magnetic field applied up to 25 T in the $ac$ plane were performed on the HFM/EXED instrument at the Helmholtz Zentrum Berlin, Berlin, Germany, which is the only existing instrument/facility that allows for neutron scattering experiments in static magnetic fields up to 26 T [24,25]. Due to the complex construction of the HFM/EXED hybrid magnet, the magnetic field can be applied only horizontally with the magnet opening of $\sim$30$^\circ$. Hence, when probing the (0.2 0 $-0.42$) magnetic reflection the magnetic field cannot be applied exactly along the $a$ axis, but rather rotated towards the $c$ axis by $\sim$30$^\circ$. To cover the broad region of the reciprocal space ($h, 0, l$), where 0 $\leq h \leq 1$ and $-1 \leq l \leq 0$, the sample was rotated around the $b$ axis from the $a$ towards the $c$ axis in steps of $\sim$10$^\circ$. The maps of the reciprocal space shown in Fig. 6 are thus obtained by combining data sets measured at different field orientations within the $ac$ plane. We note that the HFM/EXED instrument does not have beam collimators and employs a conical cryostat, which puts a substantial amount of the material in the neutron beam, leading to a significant background that is also angle dependent.

III. RESULTS

A. Magnetization measurements

Magnetization measurements were performed in pulsed magnetic field at 1.7 K to identify low-temperature field-induced magnetic transitions. The data obtained for magnetic field ($B$) applied along all three crystallographic axes ($a$, $b$, and $c$) are shown in Fig. 3 and summarized in Fig. 2. The magnetization curves exhibit three anomalies, indicating magnetic transitions from the VC ground state to the SDW state, from the SDW to the HF state, and finally into the fully saturated state. The response for $B || a$ and $B || c$ is rather similar, i.e., the anomalies for $B || a$ ($B || c$) are found at 2.8 (2.5), 18.7 (18.1), and 21.5 (21.0) T. On the other hand, for $B || b$ the low-field anomaly is shifted to significantly higher field, i.e., it occurs at 9.7 T, whereas the other two are found at only slightly higher fields than for the other two directions, i.e., at 19.4 and 22.2 T. This is not surprising when considering the strong magnetic anisotropy highlighted in preceding studies [20,22,23,26,27].
B. Neutron diffraction

In order to explore the magnetic phase diagram in more detail, we performed neutron diffraction measurements in the presence of the applied magnetic field.

1. Magnetic field along the b axis

First, we measured temperature dependencies of the second strongest magnetic reflection, i.e., the \((-0.2\ 0\ 0.42)\) reflection that also coincides with the magnetic wave vector, at several fixed magnetic fields applied along the b axis [Figs. 4(a)–4(d)]. The intensity data reveal a gradual reduction of the magnetic-ordering transition temperature \(T_{N1}\), which reduces from 4.60(2) K at 0 T to 4.10(2) K at 12 T [Fig. 4(a)]. Considering that in the vicinity of the magnetic transition the intensity of the magnetic reflection is proportional to the square of the magnetic order parameter, i.e., \(\propto (T_{N1} - T)^{2\beta}\), we find an increase of the critical exponent \(\beta\), from 0.22(2) at 0 T to 0.41(2) at 12 T. This suggests a crossover from two-dimensional XY (2D planar, \(\beta \approx 0.23\)) towards three-dimensional Heisenberg (3D isotropic, \(\beta \approx 0.36\)) universality class [28–30], implying that with increasing field the intra-chain correlations are enhanced and become more isotropic. In the absence of the magnetic field, the occurrence of the satellite magnetic reflection at \(T_{N2} = 3.35(5)\ K\) indicates the establishment of the spin-stripe modulation, while the anomaly at \(T_{N3} = 2.35(2)\ K\), where the satellite reflection merges with the main one, indicates the establishment of the VC phase. The two transitions are also associated with the changes of the magnetic wave vector. The latter first shifts linearly from \(T_{N1}\) to \(T_{N3}\) and then suddenly jumps and locks to the low temperature value. This implies that also for this field the system undergoes the transition into the VC phase. Finally, the temperature dependence measured at 12 T [Fig. 4(d)] shows no anomaly in the magnetic peak intensity nor in its position, indicating that for this field the system persists in the SDW state down to 1.7 K.

In the next step, we performed complementary field-dependence measurements at fixed temperatures [Figs. 4(e)–4(h)]. At 1.7 and 3.6 K the intensity of the \((-0.2\ 0\ 0.42)\) reflection exhibits no anomalies up to 15 T, implying that the projection of the magnetic order to the plane perpendicular to the magnetic wave vector does not change significantly at these temperatures [Fig. 4(e)]. The peak position measured at 1.7 K, however, exhibits a clear local maximum at 9.0(2) T that must be associated with the VC-to-SDW magnetic transition [Fig. 4(f)] (see also the magnetization measurements in Fig. 3). Yet, we found no such anomaly at 3.6 K [Fig. 4(h)], implying that at this temperature the system persists in the SDW phase in this field range. In contrast, the measurements at 2.6 K clearly show the existence of the satellite reflection, i.e., the indication of the spin-stripe modulation, which at 2.8(3) T merges with the main magnetic reflection [Figs. 4(e) and 4(g)]. The peak position exhibits a second anomaly at 8.0(5) T, which most likely indicates the transition from the VC to the SDW phase.

2. Magnetic field perpendicular to the b axis

Neutron diffraction measurements for \(B|a\) up to 6 T have been previously reported in Ref. [20]. We thus focus here on new experiments at even higher magnetic fields up to 25 T. Due to experimental limitations (see Sec. II), when probing the \((0.2\ 0\ -0.42)\) magnetic reflection the magnetic field was rotated from a towards c by \(\sim 30^\circ\). However, we do not expect this rotation to have any dramatic effect, since the magnetization measurements [Fig. 3(a)] imply that the magnetic responses for \(B|a\) and \(B|c\) are similar. In agreement with Ref. [20] we find that increasing the magnetic field from zero does not affect the peak position, while its intensity notably decreases. At 4.0(1) T, the intensity of the main magnetic reflection drops almost to zero and a weak satellite reflection emerges, which persists up to 5.0(2) T [Fig. 5(b)], indicating the range of the spin-stripe modulation. In parallel, the position of the main magnetic reflection shifts linearly from \((0.21\ 0\ -0.42)\) at 4 T to \((0.11\ 0\ -0.29)\) at 17.2(1) T, where it jumps to \((0.22\ 0\ -0.44)\), i.e., very close to the zero-field position, and gains back the low-field intensity (Fig. 5). Further increase of the field up to 21.4 T shifts the peak to \((0.19\ 0\ -0.4)\), which is almost exactly the zero-field position. Eventually, at 21.4 T, the incommensurate magnetic reflections suddenly disappear [Fig. 5(b)], indicating a sharp transition into the saturated phase. The new data thus clearly show that the HF state between 17.2 and 21.4 T in \(\beta\)-TeVO4 is a long-range-ordered state dominated by the incommensurate magnetic ordering. We note that the slight deviation of the transition fields compared to the magnetization measurements for \(B|a\) and \(B|c\) is probably due to the fact that eigenaxes of the susceptibility tensor within the ac plane are tilted by \(\sim 45^\circ\) away from the a and c axes [26].
FIG. 4. Neutron diffraction measurements of the (−0.2 0 0.42) magnetic reflection and its satellite (existing only in the spin-stripe modulated phase) for magnetic field applied along the b axis. The position of the magnetic reflection directly determines the magnetic wave vector. (a) The temperature dependencies of the intensity of the (−0.2 0 0.42) reflection and its satellite in different magnetic fields. Solid lines are fits of the critical behavior \( \propto (T_{\text{N}} - T)^\beta \), where \( \beta \) is the critical exponent. (b)–(d) The temperature dependence of the measured \( h \) and \( l \) components \( (k = 0) \) of the magnetic wave vector at 0, 4, and 12 T. Inset in (b) shows also the wave vector corresponding to the satellite reflection in the spin-stripe modulation. (e) The magnetic-field dependencies of the (−0.2 0 0.42) reflection intensity at different temperatures. (f)–(h) The magnetic field dependence of the \( h \) and \( l \) components \( (k = 0) \) of the magnetic wave vector measured at 1.7, 2.6, and 3.6 K. Inset in (g) shows also the wave vector corresponding to the satellite reflection in the spin-stripe modulation. Solid lines are guides to the eye, allowing for easier identification of the phase transitions indicated by the vertical arrows.

Finally, to check if there is any additional magnetic wave vector present in the VC (at 3 T), SDW (at 12 and 17 T, i.e., far above the stripe region) and HF (at 21 T) phases, we inspected the broad region of the reciprocal space \( (h, 0, l) \), where \( 0 \leq h \leq 1 \) and \( -1 \leq l \leq 0 \) (Fig. 6). We note that the direction of the magnetic field had to be varied within the ac plane to cover the complete reciprocal-space region (see Sec. II). Detailed inspection of the diffraction maps shows that besides the (1 0 0) and (0 0 −1) nuclear reflections, the only reflection that exists in this range (see arrows in Fig. 6) is the one for which we measured complete field dependence (Fig. 5). This indicates that similarly to the VC and SDW phases the HF phase also exhibits an incommensurate magnetic order determined by a single magnetic wave vector.

IV. DISCUSSION

The prime goal of our study is to understand the nature of the HF phase in \( \beta \)-TeVO\(_4\). First, we focus on the experimentally determined magnetic phase diagrams, which we derive
FIG. 5. Neutron diffraction measurements of the (0.2 0 -0.42) magnetic reflection at 1.7 K for magnetic fields applied in the ac plane, tilted by ∼30° from a towards c. (a) The integrated intensity of the magnetic reflection, while (b) shows the measured l and h components (k = 0) of the magnetic wave vector. The solid line indicates the theoretically predicted response for l (see text for details).

for magnetic fields applied along all three crystallographic axes (Fig. 2). Our data are in good agreement with magnetization, heat capacity, and magnetostriction measurements presented in Ref. 22, except for the results for B||a, which in Ref. 22 have probably been measured with the field applied along the b axis. We stress that the diffraction experiments do not allow for an error in the orientation of the monoclinic crystal. Hence, we believe that responses for B||a and B||c are very similar, whereas for B||b the low-field transition is shifted to much higher fields. In contrast to the strong anisotropy at lower fields, the transition to the HF phase is significantly less orientation dependent (Fig. 3). This suggests that the HF phase reflects the intrinsic response of the isotropic J1-J2 spin- 1/2 chain model that predicts the quadrupolar/spin-nematic phase to develop in this magnetization region [5,20]. However, the presence of the magnetic reflections shows that “conventional” dipolar magnetic order still exists in this phase.

Another interesting result is the behavior of the magnetic wave vector. Clearly the latter is locked in the VC phase [Figs. 4(b) and 5(b)], whereas it shows significant field and temperature dependencies in the SDW phase. This is most obvious for B⊥b [Fig. 5(b)], where the magnetic wave vector changes almost linearly from (0.21 0 -0.42) at 4 T to (0.11 0 -0.29) at 17.2(1) T. The observed behavior is in reasonable agreement with the theoretically predicted dependence for the SDW phase in the isotropic J1-J2 spin- 1/2 chain model, for which l = (1 - M/Msat)/p, where M is the magnetization, Msat is its saturated value, and p = 2 stands for the quadrupolar spin correlations [5]. On the other hand, in the HF phase the magnetic wave vector changes back to almost exactly the zero-field value, signifying a clear deviation from the isotropic J1-J2 spin- 1/2 chain model. In addition, we find that h and l components of the magnetic wave vector shift simultaneously and change by almost exactly the same amount for B||b (Fig. 4) as well as for B⊥b [Fig. 5(b)]. This suggests that despite h being very close to -l/2, the modulation along the a axis must be affected by the competition between inter- and intrachain interactions. This complies with the density-functional-theory calculations [22], suggesting that there are several active ferromagnetic interchain interaction pathways along the a axis, which compete with the dominant intrachain interactions.

The incommensurate magnetic order in the HF phase is most likely triggered by perturbations of the isotropic J1-J2 spin- 1/2 chain model. In fact, in another frustrated spin-1/2 chain candidate, linarite [31], already small anisotropies were found to induce a fan-type spin order in applied magnetic field before the complete saturation of the magnetization was reached [32]. The HF state in β-TeVO4 might, therefore, exhibit a similar kind of a fan order that suppresses the realization of the spin-nematic phase, predicted by the simple isotropic model.

Finally, we bring to attention studies of the spin-nematic phase in LiCuVO4 [11,15,17], where the spin-nematic phase was suggested to exist in a very narrow range between ~0.95Msat and Msat. In this respect, the spin-nematic phase in β-TeVO4 might also develop in a few tenths of a tesla below the saturation, where neutron magnetic reflections may already vanish, while the magnetization is still not completely saturated. The best check for this hypothesis would be precise neutron-diffraction measurements of both magnetic and nuclear reflections, the former probing the signal corresponding to the magnetic order, while the latter probing the signal of the saturated ferromagnetic phase on top of the nuclear contribution. Alternatively, nuclear magnetic resonance measurements...
similar to those presented in Ref. [11] could be employed to address this intriguing question.

V. CONCLUSION

In conclusion, combining magnetization measurements in pulsed magnetic fields and neutron diffraction in static magnetic field up to 25 T, we are able to determine in detail the magnetic phase diagram of $\beta$-TeVO$_4$. We find a novel high-field phase that exhibits a long-range incommensurate magnetic order, which most likely suppresses spin-nematic phase due to the presence of interchain interactions and sizable magnetic anisotropies. Nevertheless, the field dependence of the magnetic wave vector in the SDW phase approximately follows the response predicted by the isotropic $J_1$-$J_2$ model, suggesting that the spin-nematic phase might still develop in a narrow region of a few tenths of a tesla before the full magnetic saturation is reached.

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