Cation Distributions and Magnetic Properties of Ferrispinel MgFeMnO4

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ABSTRACT: The crystal structure and magnetic properties of the cubic spinel MgFeMnO4 were studied by using a series of in-house techniques along with large-scale neutron diffraction and muon spin rotation spectroscopy in the temperature range between 1.5 and 500 K. The detailed crystal structure is successfully refined by using a cubic spinel structure described by the space group Fd3m. Cations within tetrahedral A and octahedral B sites of the spinel were found to be in a disordered state. The extracted fractional site occupancies confirm the presence of antisite defects, which are of importance for the electrochemical performance of MgFeMnO4 and related battery materials. Neutron diffraction and muon spin spectroscopy reveal a ferrimagnetic order below Tc = 394.2 K, having a collinear spin arrangement with antiparallel spins at the A and B sites, respectively. Our findings provide new and improved understanding of the fundamental properties of the ferrispinel materials and of their potential applications within future spintronics and battery devices.

INTRODUCTION

The well-established spinel magnesium oxide family (MgM3O4, where M is a transition metal atom) has been the subject of interest within a broad scope of research as well as applications, for example, catalysts, humidity sensors, or microwave devices.1–4 Recently, increased attention has been drawn to a series of Mg materials, following the development of high-energy-density rechargeable magnesium batteries.5–8 However, spinel magnesium oxides also have many interesting fundamental materials properties, including diverse magnetic spin orders. This class of materials displays paramagnetism, ferrimagnetism, superparamagnetism, and spin-glass behavior. Such magnetic properties also play an essential role in the application within, for example, magnetic resonance imaging, data storage, and drug delivery systems.9,10 Spineloids have the general formula ABO4, and most of them are reported to have a cubic crystal structure with space group Fd3m. The structure consists of tetrahedrally coordinated A site cations at Wyckoff position 8a (1/8, 1/8, 1/8) and octahedrally coordinated B site cations at 16d (1/2, 1/2, 1/2). Oxygen (O) atoms lie on the body diagonals of the cube at 32e (u, u, u), where u is approximately 1/4. In the case of magnesium oxides, divalent magnesium and trivalent transition metal atoms tend to occupy the A and B sites, respectively. However, the cation distribution between the A and B sites, which is known to strongly influence the physical properties of these materials,9,10 is a controversial issue.

The parent compounds, MgMn2O4 and MgFe2O4, crystallize in different space groups and display very different magnetic properties. This was the main motivation for studying the solid solution (MgFeMnO4) of these two compounds. MgFe2O4 crystallizes in the typical cubic spinel structure, with a slight Mg/Fe disorder between the A and B sites.11,12 The magnetic ground state of MgFe2O4 has been reported to be a ferrimagnet below Tc = 363–493 K (here Tc is strongly dependent on the cation distribution.).13,14 On the other hand, MgMn2O4 is known to form a distorted tetragonal phase (space group: I41/mmd) due to the Jahn–Teller effect of Mn3+.15–17 Typically, this compound shows a perfect cation ordering with the lattice sites being occupied as A = Mg2+ and B = Mn3+. In addition, an antiferromagnetic spin order occurs below TN = 50 K.9 Recently, Mg(Mn1−xFex)2O4 has been synthesized and characterized by electrochemical measurements. Han et al.18 reported that more than 20% of Fe substitution could stabilize the cubic spinel structure of Mg(Mn1−xFex)2O4 demonstrating that the charge compensation during the charge/discharge processes mainly occurs on
Mn\(^{2+}/\text{Mn}^{4+}\). However, the electrochemical performance of MgMn\(^2\)O\(_4\) is not efficient because of the structural transition during the charge/discharge process between the tetragonal and the cubic phases. Thus, the substituted cubic system Mg(Mn\(_{1-x}\)Fe\(_x\))\(^2\)O\(_4\) is better suited as a magnesium battery cathode material. The detailed crystal structure and the magnetic characterization of Mg(Mn\(_{1-x}\)Fe\(_x\))\(^2\)O\(_4\) are missing so far to the best of our knowledge.

In this article, we present the detailed crystal structure and magnetic properties of the cubic spinel MgFeMnO\(_4\) (i.e., \(x = 0.5\)). The cationic arrangement of the compound was studied by the combination of X-rays and neutron diffraction methods. Contrary to the X-ray diffraction, the differences in the neutron scattering amplitudes (i.e., contrast) of the constituent atoms have allowed an accurate determination of the cation distribution in MgFeMnO\(_4\). These crystallographic studies unveiled that MgFeMnO\(_4\) indeed forms a cubic spinel structure with Mg/Fe/Mn disorder. Furthermore, macroscopic magnetization measurements show that the magnetic transition temperature is above room temperature (RT). A ferrimagnetic spin ordering is revealed below \(T_c = 392\) K by the combination of neutron powder diffraction (NPD) and muon spin rotation/relaxation (\(\mu^+\text{SR}\)) measurements. These results provide a deeper understanding of the fundamental properties of MgFeMnO\(_4\) along with potential improvement of related battery devices.

## Experimental Methods

### Materials Synthesis

Stoichiometric amounts of Mn\(_2\)O\(_3\) (Kishida Chemicals, 99% purity), Fe\(_2\)O\(_3\) (Kishida Chemicals, 98% purity), and MgO (99.9%, Wako pure chemical) powders were weighted in a molar ratio of 1:1:1. The powders were mixed by using a planetary ball mill to attain a homogeneous mixture. The powder was pelletized and calcined at 800 °C for 5 h in air. Quantification of the chemical composition of the as-prepared MgFeMnO\(_4\) was assessed by using inductively coupled plasma absorption electron spectroscopy (ICP-AES) on a Shimadzu ICPS-8100 instrument.

### X-ray and Neutron Powder Diffraction

X-ray powder diffraction (XRPD) measurements of the as-synthesized powders were performed in Bragg–Brentano mode by using a diffractometer (Bruker D2 ADVANCE) at a 2θ range of 5°–90° using a step size of 0.01°. The wavelength was set at Cu K\(_{\alpha}\), and measurements were performed at room temperature. Neutron powder diffraction (NPD) was performed on the D2B instrument (ILL, Grenoble) using the selected neutron wavelength \(\lambda = 1.595\) Å. Data were collected at two temperatures \(T = 300\) and 500 K. The measurement at 500 K was performed by using a dedicated furnace. Symmetry analysis and Rietveld refinements for both X-ray and neutron diffraction patterns were performed with tools from the FULLPROF software suite\(^{15}\) and the Bilbao Crystallographic Server.\(^{19}\)

### Electron Microscopy

The morphology of the materials was analyzed by a field-emission scanning electron microscope (JSM-6510LA). High-resolution transmission electron microscopy (HRTEM) images of pristine MgFeMnO\(_4\) were obtained on a TITAN80-300F at an accelerated voltage of 200 kV. Simulations of the HRTEM images were performed with the JEMS 31(PECD) software.

### Magnetization Measurements

Bulk magnetic (DC) susceptibility measurements as a function of temperature were performed with a Quantum Design superconducting quantum interference device magnetometer (MPMS) upon warming in a temperature range from 5 to 400 K. Data were collected in both zero-field-cooled (ZFC) and field-cooled (FC) protocols using an external magnetic field \(H = 100\) Oe. Magnetization data as a function of field were collected up to \(\pm 10.0\) kOe after zero field cooling. For the data analysis, the coercive field \(H_c\) is defined as \(H_c = (H_{+} + H_{-})/2(|H_{+} - H_{-}|)/2\), where the coercivity at the positive \((H_{+})\) and negative \((H_{-})\) fields has been determined by linear interpolation of the data points close to zero magnetization. In addition, the exchange bias field \((H_{\text{EB}})\) was extracted according to the following relation: \(H_{\text{EB}} = (|H_{+} - H_{-}|)/2\).
Mössbauer Spectroscopy. $^{57}$Fe Mössbauer experiments were performed at 298 K by using a conventional Mössbauer spectrometer. About 100 mg of sample was mixed with boron nitride and pressed into pellets (having a diameter of 10 mm) for Mössbauer transmission experiments. $\alpha$-Fe was used for velocity calibration. The Mössbauer spectrum was fitted by using standard data analysis software (Origin Pro, version 2020b) by adding multiple Lorentzian peak functions. Also pseudo-Voigt functions were tested, yielding very similar results (see the Supporting Information, Figure S2 and Table S2). Finally, data were fitted by using the specialized MossWinn program.\textsuperscript{20,21}

Muon Spin Rotation and Relaxation ($\mu$SR) Measurements. $\mu$SR experiments were performed by using the general purpose surface (GPS)-muon instrument\textsuperscript{22} at the Swiss Muon Source (SyS) of PSI in Switzerland. This spectrometer has a time resolution of 160 ps, which corresponds to an upper theoretical cutoff frequency of 6250 MHz. More realistically and experimentally proven the GPS spectrometer can resolve muon spin rotation frequencies up to 1842 MHz.\textsuperscript{22} Considering the gyromagnetic ratio of the muon $\gamma_\mu = 135.5$ MHz/T, this means that the highest detectable internal field at the muon stopping site is approximately $1842/135.5 \approx 13.6$ T. The temperature range for the current experiments, 20–300 K, was obtained by using a liquid-He flow-type horizontal cryostat. The powder sample ($m \approx 0.5$ g) was placed in an envelope made of very thin ($<$50 µm) Al-coated Mylar tape covering a surface area of 1 x 1 cm$^2$. To minimize the background signal, the envelope was attached to a fork-type Cu sample holder by a single layer of the Mylar tape. The sample holder was attached to a sample stick and inserted into the cryostat. The measurements above room temperature (RT) were performed by using a closed-cycle refrigerator (CCR). For such measurement the powder sample was pressed into a pellet that was attached onto a Cu-plate sample holder by Al-coated Mylar tape and secured by a thin Cu wire. For both setups, $\mu$SR time spectra were collected by using the zero-field ($ZF$) and weak transverse-field ($wTF = 50$ Oe) protocols. One of the main advantages of the $\mu$SR technique is that magnetic spin order can be studied in a true ZF environment. Further details regarding the experimental techniques and setups are provided in ref 23. The musrfit\textsuperscript{24} software package was used to fit and analyze the $\mu$SR data.

RESULTS

Fundamental Characterization. XRPD was first performed to check the quality of the sample at room temperature. It is known that the stoichiometry of magnesium spinel oxides is sensitive to the heat treatments performed during the synthesis process.\textsuperscript{25} The composition ratio of MgFeMnO$_4$ was carefully examined also by using ICP-AES (Table S1). The synthesized MgFeMnO$_4$ was confirmed to have the stoichiometric composition within the experimental accuracy. The concentration of Mg was found to be only slightly lower than that of Fe and Mn, probably related to the evaporation of Mg during the heat treatment process. The detailed analysis of the XRPD data is described in the next section, together with the neutron diffraction results.

The temperature dependencies of the DC magnetic susceptibility, $\chi(T)$, for MgFeMnO$_4$ by using both ZFC and FC protocols (measured upon warming) are shown in Figure 1a,b. As seen, the ZFC and FC magnetizations bifurcate at $T \approx 370$ K and show a broad peak in the ZFC curve with a maximum at $T_{\text{max}} \approx 330$ K. Such behavior supports the existence of antiferromagnetic and/or ferrimagnetic spin clusters.\textsuperscript{26,27} When the sample is measured during the FC process, more ferro- or ferrimagnetic clusters are aligned along the field direction, which causes a large separation between FC and ZFC.\textsuperscript{26} FC susceptibility reaches its maximum around $T \approx 20$ K and then saturates, which indicates a ferrimagnetic behavior.

The correlation between the magnetization and the strength of the external applied magnetic field strength ($M$ vs $H$ plots) at different temperatures is shown in Figure 1c,d. Hysteresis loops were observed at both $T = 298$ K and $T = 5$ K. $M$ increases steeply for low fields, then rises relatively slowly, and does not fully saturate up until $H = 10$ kOe. The hysteresis curves of MgFeMnO$_4$ show a soft ferromagnetic behavior at both temperatures. The coercivity ($H_C$) and remanence ($M_r$) values at the two different temperatures are summarized in Table 1. The coercivity is the magnitude of the field that must be applied in the negative direction to bring the magnetization of the sample back to zero. These magnetic properties at RT are very similar to the features of the ferrimagnetic parent compound MgFe$_2$O$_4$. In contrast, the other parent compound MgMn$_2$O$_4$ displayed an antiferromagnetic spin order.

Figure 2 shows the Mössbauer spectrum of MgFeMnO$_4$ recorded at RT. The sextet splitting of the Mössbauer spectrum indicates that MgFeMnO$_4$ is in a magnetically ordered state\textsuperscript{28} at RT. This is consistent with the fact that the current Mössbauer data are clearly acquired in the spin-ordered phase of MgFeMnO$_4$, as seen from, for example, the magnetization measurements in Figure 1. By using multiple Lorentzian peak functions, we can fit the data well using six components. The resulting peak positions and full width at half-maximum (FWHM) along with the respective peak splits, $\Delta_p$\textsuperscript{-p}, are detailed in Table S2. First of all, it is clear that the peak shapes are broadened. This could be due to several reasons including multiple Fe sites in the lattice (see below for structure determination) along with several additional effects, for example, the particle size, superparamagnetism, spin glass, or spin cluster systems. Here, the particle size of the present sample was determined to be approximately 50–200 nm, as extracted from SEM measurements (images are shown in

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<th>Table 1. Results from the Magnetization vs Magnetic Field Measurements (See Figure 1c,d)$^{29}$</th>
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<td>magnetic parameters</td>
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<tr>
<td>magnetization [$M_r$] (µB)</td>
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<td>retentivity [$M_r$] (µB)</td>
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<td>squareness [$r$]</td>
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<td>exchange bias field [$H_E$] (Oe)</td>
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$^{29}$The table lists the saturation magnetization ($M_s$), coercivity ($H_C$), retentivity ($M_r$), squareness ratio/remanence ratio ($r$), and the exchange bias field ($H_E$) of MgFeMnO$_4$ at $T = 5$ K and $T = 298$ K.
Figure S1). It should be noted that nanoparticles often yield a superparamagnetic contribution. Additional broadening may also stem from a wide magnetic hyperfine distribution as also observed in MgFe2O4.14

An isomer shift $\delta = 0.31$ mm/s was extracted from our data by using the MossWin fitting software.20 Such a value of $\delta$ supports that an iron valence Fe3$^+$ rather than Fe2$^+$ is present in MgFeMnO4.26,29,30 In addition, a mixed valence case containing both Fe$^2+$ and Fe$^3+$ would cause an asymmetric peak shape (Figure 2a), which is not (clearly) visible. Moreover, the quadrupole splitting (QS) was not discernible in MgFeMnO4.31 Thus, the spin state of Fe cannot be determined from our Mössbauer data. It is noteworthy that Fe is normally stable in the high-spin (HS) state; on the other hand, low-spin and intermediate-spin states can be induced by applying high pressure.29 The parent compound, MgFe2O4, is indeed reported to have high-spin Fe3+.32 In similarity to MgFeMnO4, the QS for MgFe2O4 was not resolved in the magnetically ordered state but could be observed in the paramagnetic phase above the magnetic transition temperature. Even though we did not have the possibility to measure MgFeMnO4 in its paramagnetic state, it is very reasonable to surmise that Fe$^3+$ also in MgFeMnO4 would adopt the high-spin state at ambient pressure. The magnetism of spinel ferrites is known to be strongly related to the cation distribution between the $A$ and $B$ sites. For instance, Osmond et al. claimed that the disorder of the magnetic cation in both $A$ and $B$ sites induces ferrimagnetic interactions.33 However, as De Grave et al. mentioned in ref 14, it is impossible to determine the Fe$^3+$ cation distribution among $A$ and $B$ sites of a spinel lattice from using only zero-field Mössbauer spectroscopy. To investigate the details of the cation distribution, a careful crystal structure analysis was performed by combining both X-ray and neutron powder diffraction measurements.

**Crystal Structure Determination.** The crystal structure of MgFeMnO4 was investigated by using both XRPD and NPD techniques. The neutron scattering technique was absolutely necessary because of its higher sensitivity to oxygen as well as greater Mn/Fe contrast, in comparison to XRPD. The structural analysis of MgFeMnO4 started from the reported space group, unit cell, and atomic coordinates of cubic spinel MgFe2O4.24,34 The XRPD and NPD patterns of MgFeMnO4 are indexed perfectly by using a cubic crystal structure (space group Fd3m, No. 227) with $a \sim 8.43$ Å. The space group and cell parameters are also confirmed by electron diffraction recorded at RT (see Figure S1c,d). To avoid the influence of magnetic Bragg peaks, the NPD pattern recorded at $T = 500$ K (i.e., above magnetic transition temperature) was used to initially determine the crystal structure. The crystallographic parameters obtained from the refinement performed on the NPD data ($T = 300$ K and $T = 500$ K) and the corresponding interatomic distances are presented in Table 2. Figure 3 shows the resulting XRPD and NPD patterns along with the calculated patterns. The crystal structure obtained from the calculated patterns is displayed in Figure 4. The values of the lattice parameter of the cubic structure, determined in this study, are 8.4290 Å at $T = 500$ K and 8.4116 Å at $T = 300$ K. The values are comparable to the reported cell parameter of MgFe2O4 studied by synchrotron X-ray diffraction (at 500 K: $a = 8.437$ Å; at 300 K: $a = 8.4208$ Å).35

No signs of impurity phase peaks were observed in either XRPD or NPD patterns, indicating that the synthesized sample is a single high-quality phase. The structure is a typical spinel structure, and the three cations (Mg, Fe, and Mn) are

| Table 2. Structural Parameters of MgFeMnO4 at $T = 500$ K and $T = 300$ K from Rietveld Refinement of Neutron Powder Diffraction (NPD) Data$^a$
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<tr>
<td>$T = 500$ K</td>
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<tr>
<td>Structural parameters</td>
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<tr>
<td>$a$ (Å)</td>
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<td>8.4116 (1)</td>
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<tr>
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<td>8.4208 (1)</td>
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<td>8.4116 (1)</td>
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<tr>
<td>$A-B$ (Å)</td>
<td>3.494 (1)</td>
<td>3.487 (1)</td>
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$^a$The space group is $Fd3m$ and cations occupy Wyckoff positions $8a$ [tetrahedral sites (A)] and $16d$ [octahedral sites (B)]. The fractional coordinates of (A) and (B) positions are (1/8, 1/8, 1/8) and (1/2, 1/2, 1/2), respectively. Oxygen atoms occupy Wyckoff position $32e$ with fractional coordinates ($x$, $x$, $x$). The isotropic thermal factors ($B_{iso}$) as well as fractional occupancies ($O_{(A)/(B)}$) are given for the different sites. Finally, the goodness of fit is also detailed.
Magnetic Structure Determination. For the magnetic spin analysis, each model was refined to convergence, and the best result was selected based on agreement factors and stability of the refinement. The occupancy of cations on tetrahedral and octahedral sites obtained from the earlier refinements were kept fixed, and all other parameters were varied freely. Figure 3c shows a neutron diffraction pattern containing both nuclear and magnetic contributions. The solid line is the resulting refinement based on two-phase analysis, showing a satisfactory agreement between the observed and calculated profiles. Because there is no magnetic Bragg peak observed at the position of (200) (indexed and highlighted in red in Figure 3c), the spin orientation can be concluded to have only one magnetic component (i.e., as described in Figure 5). The resulting magnetic structure at $T = 300\text{ K}$ having ordered magnetic moments of $A = 1.57$ (S) and $B = 1.22$ (4) $\mu_B$. The spins of the $A$ and $B$ sites are found to align in a collinear but antiparallel fashion, hereby suggesting that the magnetic structure is ferrimagnetic. The resulting spin arrangement of MgFeMnO$_4$ is shown schematically in Figure 5.

**Muon Spin Relaxation ($\mu$SR).** We also performed positive muon spin rotation/relaxation ($\mu$SR) measurements of MgFeMnO$_4$ under weak transverse field ($w_{\text{TF}} = 50\text{ Oe}$) (Figure 6) and zero field (ZF) (Figure 7) at temperatures between 2 and 470 K. The $w_{\text{TF}}-\mu$SR spectrum was fitted by using a combination of a slowly (exponentially) relaxing oscillatory (cosine) signal due to the externally applied magnetic field $w_{\text{TF}} = 50\text{ Oe}$ and a nonoscillating but exponentially relaxing ("mag") signal:

$$A_0 P_{\text{TF}}(t) = A_{\text{TF}} \cos(2\pi w_{\text{TF}} t + \phi_{\text{TF}}) \exp(-\lambda_{\text{TF}} t) + A_{\text{mag}} \exp(-\lambda_{\text{mag}} t)$$

(1)

Here $P_{\text{TF}}(t)$ is the muon spin polarization function, $A_0$ is the initial asymmetry, $A_{\text{TF}}$ and $A_{\text{mag}}$ are the asymmetries of the related polarization components, and $2\pi w_{\text{TF}}$ is the angular frequency of the Larmor precession (of the rotating muon spins) under the applied transverse field. In addition, $\lambda_{\text{TF}}$ and $\lambda_{\text{mag}}$ are the exponential relaxation rates for the two components, and $\phi_{\text{TF}}$ is the initial phase of the precessing signal. In particular, $A_{\text{TF}}$ is the fraction of muons sensing the applied $w_{\text{TF}} = 50\text{ Oe}$, while $A_{\text{mag}}$ is the fraction of muons coupled to the internal field. Note that the experimental setup was changed at 300 K from low-temperature cryostat to high-temperature CCR. The time spectra at 300 K were collected by using both setups to record an overlapping data point. There is no precessing signal ($A_{\text{TF}} = 0$) at 300 K when using the cryostat, but $A_{\text{TF}} = 0.06$ is observed when the setup was...
Figure 6. (a) $\mu$SR time spectra of MgFeMnO$_4$ at $T = 2$ K (in cryostat) and (b) temperature dependence $\mu$SR time spectra (at 300, 380, 400, 420, and 470 K in CCR) under a weak-transverse field, wTF = 50 Oe. The corresponding fits using eq 2 are shown as solid lines. For clarity, $A_0$ is the initial asymmetry and $P_{TF}(t)$ is the muon spin polarization function. (c) Temperature dependence of the normalized wTF asymmetry $A_{TF}$ of MgFeMnO$_4$ obtained from fits to the wTF $\mu$SR time spectra using eq 2. In addition, the sigmoid fit (red solid line) yields the magnetic transition temperature, $T_C = 394.2$ K. (d) wTF relaxation rate ($\lambda_{TF}$) displaying a clear peak in the vicinity of the magnetic phase transition.

Figure 7. (a) ZF-$\mu$SR time spectra of MgFeMnO$_4$ at $T = 2$ K shown for the complete time domain. A shaded blue rectangle is shown in (b) where a zoomed-in view of the shorter time domain emphasizes the absence of any clear oscillations along with a missing asymmetry fraction. (c) Temperature-dependent ZF-$\mu$SR spectra for MgFeMnO$_4$ in the long time domain up to 8 $\mu$s. A shaded blue rectangle is shown in (d) with a zoomed-in view of the early time domain up to 0.2 $\mu$s. For (c, d) each spectrum is offset along the y-axis by 0.1 for clarity of display. Solid lines are the best fits to the data using eq 2.
changed to the CCR. The additional asymmetry stems from muons hitting the Cu sample holder, that is, a courtesy of the higher background signal of the CCR setup. The wTF signal shown in Figure 6b was measured by using CCR.

Because the applied field is weak relative to the internal field (when the sample is magnetically ordered), the fraction of normalized asymmetry ($N_{\text{ATF}} = A_{\text{TF}}/\max[A_{\text{TF}}]$) with background subtracted then corresponds to the paramagnetic (PM) fraction of the sample. Therefore, the temperature dependence of $A_{\text{TF}}(T)$ can be considered as the evolution of the magnetic state in the sample. By plotting $N_{\text{ATF}}$ vs $T$ (see Figure 6c), we can fit the trend of the asymmetry with a sigmoid function. From such fit, the transition temperature $T_C = 394.2$ (12) K is defined as the middle point of the fitting curve, where $N_{\text{ATF}} = 0.5$. Such a value of $T_C$ is in excellent agreement with our other experimental results mentioned previously. From the wTF spectra collected below $T_C$, it is clear that the entire volume of the sample enters into a long-range magnetic order (since $A_{\text{TF}} = 0$ at low temperatures as shown in Figure 6a). This is a clear indication that the investigated sample is homogeneous and of high quality. The unique possibility to accurately determine the magnetically ordered volume fraction of a sample is a powerful capability of the $\mu$SR technique. Finally, the temperature dependence of the wTF relaxation rate ($\lambda_{\text{TF}}$) is shown in Figure 6d, displaying a clear peak in the vicinity of the magnetic phase transition. Here the strong increase in $\lambda_{\text{TF}}$ indicates the expected and drastic change in the spin dynamics associated with the spin order.

Figure 7a shows ZF-$\mu$SR time spectra recorded at the lowest experimental temperature, $T = 2$ K. It is apparent that no oscillation signal is present even in the shortest time range (see the inset of Figure 7a). However, we clearly observe that the initial asymmetry at time zero is only $A_0 \approx 0.1$ instead of the expected $\sim 0.24$ (determined by the experimental setup). This so-called “missing fraction” is directly related to the ferrimagnetic order and will be further discussed below. In fact, no oscillatory signal was observed in the entire experimental temperature range ($T = 2$–470 K, see also Figure 7b,c). Consequently, the ZF spectra were fitted by three exponentially relaxing nonoscillatory components. Here one of such signals is due to the paramagnetic background (BG) signal coming from the Cu holder in the high-temperature wTF CCR measurements (i.e., such component was only used for the data recorded above 300 K, where $A_{\text{BG}}$ was fixed to 0.0284). The resulting ZF fit function is described by

\[
A_0 P_{\text{ZF}}(t) = A_{\text{fast}} \exp(-\lambda_{\text{fast}}t) + A \exp(-\lambda_{\text{tail}}t)
+ A_{\text{BG}} \exp(-\lambda_{\text{BG}}t)
\]

where $A_0$ is the initial asymmetry, $A_{\text{fast}}$, $A_{\text{tail}}$, and $A_{\text{BG}}$ are the asymmetries associated with each signal, and $\lambda_{\text{fast}}$, $\lambda_{\text{tail}}$, and $\lambda_{\text{BG}}$ are the exponential relaxation rates of each signal. It is clearly shown in Figure 7 that both short ($t < 0.2 \mu s$) and long ($t \approx 8 \mu s$) time spectra were well fitted by using eq 2. At $T = 2$ K ($A_{\text{BG}} = 0$), $A_{\text{tail}}$ is about 0.08, which is coherent with the expected $1/3$ (i.e., 0.24–0.0284/3) powder average tail component (local field oriented parallel to the muon spin). This further supports the wTF results showing that the volume fraction of the magnetic phase is effectively 100% below $T_C$. $A_{\text{tail}}$ on the other hand, corresponds to internal field components that are perpendicular to the initial muon spin. This fraction should correspond to about 2/3 of the local fields in an ideal powder that is magnetically ordered. In other words, an asymmetry $2/3A_0 = 0.16$ is expected if the depolarization is within the time resolution of the experimental setup. In this case we clearly have a missing fraction since we only find that $\lambda_{\text{BG}} \approx 0.03$ at $T = 2$ K.

The fitting parameters of the ZF-$\mu$SR time spectra above 300 K are summarized in Figure 8. It is noted that the paramagnetic (BG) signal from the high-temperature setup comes from the Cu sample holder. A previous $\mu$SR study of the Cu metal shows a small relaxation rate ($\lambda_{\text{BG}} \approx 0.025$) observed at 300 K, and it decreases further by increasing the temperature. Because $A_{\text{BG}}$ is also small, it is difficult to discern such minor relaxation contribution for our present data. Thus, we fixed $\lambda_{\text{BG}} = 0$, which is a good approximation for our purposes.

In the temperature dependence of $\lambda_{\text{tail}}$, a maximum is observed at $T_{\text{max}} = 400$ K. Such a maximum occurs close to the inflection point of $A_{\text{tail}}$ and is directly related to a critical slowing down of magnetic moments accompanied by the magnetic order (cf. the coherent behavior of $\lambda_{\text{TF}}$ above in Figure 6d). Such a magnetic ordering temperature is in good agreement with the one determined by the wTF-$\mu$SR data, that is, $T_C = 394.2$ K. Below $T_C$, the internal magnetic fields are strong enough to create a large field distribution at the muon site, that is, to produce a fast depolarization of the muon beam (faster than the time resolution of the current experimental setup).

This is why we see such a large “missing fraction” as mentioned above. The resulting internal fields at the muon stopping sites are so strong that the muon spin precession is simply too fast, and the oscillation occurs below $t \approx 0.1 \mu s$, that is, faster than the time resolution of the GPS spectrometer. Such situation is often observed in $\mu$SR spectra recorded in ZF for materials with very large magnetic moments, for
instance, ferro-/ferrimagnetic materials.\textsuperscript{38--40} Because the magnetic moments of each magnetic site in MgFeMnO$_4$ are maximum $\sim$1.6 $\mu_B$, such a scenario is very reasonable. Hence, this is also in perfect agreement with the current NPD results that reveal a collinear ferrimagnetic ordering.

\section*{DISCUSSION}

Cation Distribution and Electrochemical Performance. Magnesium is generally known to be in a divalent state at tetrahedral lattice sites, whereas Fe and Mn are usually trivalent in the octahedral sites. The trivalent state of Fe is confirmed by Mössbauer spectroscopy (Figure 2). Assuming that Mg is stable in divalent state and all Fe are in trivalent state, then all Mn ions also have to be in trivalent state. To ultimately confirm the accurate valence state of the cations, further experiments, such as X-ray absorption near-edge spectroscopy (XANES), are required. In fact, XANES studies of the very closely related Mg(Mn$_{0.5}$Fe$_{0.5}$)$_2$O$_4$ compound at the Mn and Fe K-edge have indeed shown that both Mn and Fe are mainly in the trivalent state rather than the divalent state.\textsuperscript{6} Consequently, it is very reasonable to expect that MgFeMnO$_4$ also displays similar valence states. The trivalently charged Mn in octahedral site (HS d$^4$: $t_2g^3e_g$) is a Jahn–Teller-active cation, which is the origin of the distorted spinel MgMn$_2$O$_4$. However, the non-Jahn–Teller cations (Fe$^{3+}$ with HS d$^3$: $t_2g^3e_g$) suppresses such distortion. Another interesting point is that both tetrahedral and octahedral Mn sites can have an orbital degree of freedom ($t_2g + e_g$ are not completely filled) and, therefore, electrons can occupy both orbitals. Therefore, our current results concerning both Mn valence and site occupancy should also be of high interest for future applications, such as spintronics and ultimately quantum computing.\textsuperscript{41--43}

The electrochemical properties of the Mg(Mn$_{1-x}$Fe$_x$)$_2$O$_4$ series of compounds have been studied by Han et al.\textsuperscript{6} It was shown that the redox processes mainly occur between Mn$^{3+}$ and Mn$^{4+}$. However, it is necessary to substitute more than 20% of Mn with Fe to stabilize the cubic crystal structure, which yields the best charge/discharge performance. In our current study of MgFeMnO$_4$ (i.e., $x = 0.5$), we do not present results from electrochemical characterization. However, we naturally expect similar (intermediate) performance as $x = 0.4$ and $x = 0.6$, which is reported in ref 6. Such compositions showed much better electrochemical properties compared to the parent compounds, MgFe$_2$O$_4$ and MgMn$_2$O$_4$. Moreover, disorder between the tetrahedral and octahedral sites in spinel oxides is known to create “anti-site defects”, resulting in physical, chemical, optical, and electrochemical properties, which are favorable for battery devices as well as other applications.\textsuperscript{6,44} This effect relates to the interesting self-substitution occurring between tetrahedral and octahedral sites. The normal spinel structure consists of divalent ions occupying the tetrahedral site and trivalent ions placed in the octahedral site. If a distribution of cations between the two sites is present, a mixed valence state becomes possible: for instance, if a trivalent cation is placed in the tetrahedral A site. Then, to compensate for the trivalent valence, the compound became the electron producing donor state (n-type). On the other hand, if a divalent cation is substituted into the octahedral B site, it will instead form a hole producing acceptor state (p-type) to compensate for the divalent valence. Most of the produced holes/electrons will be electrochemically compensated. However, based on the cation occupancy determined by our diffraction studies, MgFeMnO$_4$ could in fact be a p-type semiconductor. Normally, antisite defects tend to degrade the ion-transport performance by effectively blocking the diffusion paths.\textsuperscript{45--47} However, because of this interesting self-substitution phenomenon, the resulting cathode performance can instead be improved through its propensity toward semiconducting properties.\textsuperscript{34,48} In this study, an accurate cation distribution of MgFeMnO$_4$ was determined by combining X-ray and neutron powder diffraction. From our results it is clear that such antisite defects are present in this series of materials.

Finally, Mg$^{2+}$ is only located at the tetrahedral A site in MgMn$_2$O$_4$.\textsuperscript{35--37} On the other hand, MgFe$_2$O$_4$ shows a certain degree of antisite defects (10--30% of Mg in the octahedral B site).\textsuperscript{36} In the current case of MgFeMnO$_4$, the mixture of manganese and iron in the spinel oxide clearly increases the amount of antisite defects. The same effect was observed in Mg(Mn$_{1-x}$Co$_x$)$_2$O$_4$.\textsuperscript{18} Moreover, in the case of Mg(Mn$_{1-x}$Co$_x$)$_2$O$_4$, Zhao et al. claimed that the antisite effect plays a critical role to improve the electrochemical performance.\textsuperscript{4} Our current results, together with the previously reported electrochemical performance studies,\textsuperscript{6} further support the critical role of the antisite defects for improved electrochemical behavior. Consequently, we believe that our current results will also be of high interest for the electrochemistry and battery application communities.

Magnetic Structure. The present system is composed of two types of magnetic ions, that is, Mn (HS: d$^4$ for Mn$^{3+}$ and HS: d$^3$ for Mn$^{2+}$) and Fe (HS: d$^5$ for Fe$^{3+}$). The theoretical ordered magnetic moment values are 5.9 $\mu_B$ for Fe$^{3+}$ and 4.9 $\mu_B$ for Mn$^{3+}$. Consequently, the calculated values for each sublattice moments are $A = 3.86$ and $B = 3.70$ $\mu_B$, as obtained by applying the cation distributions from the Rietveld refinement of the presented diffraction data (see Table 2). Clearly, the experimental (NPD) values for both A and B site magnetic moments ($A = 1.57$ (5) and $B = 1.22$ (4) $\mu_B$) are well below theoretical expectations, losing 59.3% and 67.0% of the expected moment, respectively.

The exchange interaction within the cubic spinel family has already been extensively studied for related compounds by using both experimental and theoretical methods.\textsuperscript{26,49} Because of the unique geometry of the spinel structure, three types of magnetic interactions are expected. The strongest one is tetrahedral (A)–octahedral (B) antiferromagnetic interactions connected by the corner sharing (A–B distance at RT = 3.49 Å). The other two paths are expected to show relatively weak interplay: the edge-sharing B–B (2.97 Å) and the isolated A–A (3.64 Å) interactions. Even if all three interactions are expected to be antiferromagnetic, the edge-sharing B–B spins favors a parallel ground state. In our study, the refined magnetic structure of MgFeMnO$_4$ is in very good agreement with these expected exchange interactions. In MgFeMnO$_4$, the A and B sites are occupied by two different magnetic atoms, which have different size of the magnetic moment, namely, Mn$^{3+}$ and Fe$^{3+}$. This yields two types of A–B interactions: Fe–Fe or Mn–Mn antiferromagnetic and Fe–Mn ferrimagnetic. Because nonmagnetic Mg atoms are also distributed in both octahedral and tetrahedral sites, the magnetic ordering can be disturbed and instead form finite sized PM clusters. Because we observe clear magnetic Bragg peaks by NPD, we confirmed the existence of long-range magnetic ordering in this compound. However, the reduced magnetic moment on both A and B sites can be related to such PM clusters, which naturally do not contribute to the magnetic Bragg peaks.
These results con- **importance for improved electrochemical performance in octahedral** properties of MgFeMnO₄. Consequently, the current research provide new and improved understanding for the fundamental **di** range magnetic ordering as con- sites are occupied by nonmagnetic cation) only shows a short- **range magnetic ordering as con**- found that the entire sample enters the ferrimagnetic state below the magnetic transition temperature **T_C = 394.2 (12) K.** In the ferrimagnetic phase, no muon spin oscillations are observed in the ZF-**μ** SR time spectra, which is consistent with the ferrimagnetic spin ordering determined by neutron diffraction. Hence, the magnetic properties of MgFeMnO₄ are more similar to those of the ferrimagnetic MgFe₂O₄ than to those of the antiferromagnetic MgMn₂O₄. Our findings provide new and improved understanding for the fundamental properties of MgFeMnO₄. Consequently, the current research should also be of high importance for future potential applications within spintronics as well as battery devices.

**CONCLUSION**

Accurate studies of crystal structure of the magnesium spinel MgFeMnO₄ have been performed by combining electron, X-ray, and neutron diffraction techniques. The crystal structure has been confirmed to be a typical cubic spinel structure (SG: Fd̅3m with a = 8.429 Å at 500 K). Three cations (Mg, Fe, and Mn) are found to be distributed over both tetragonal A and octahedral B sites, and fractional occupations are presented. These results confirm the presence of antisite defects and their importance for improved electrochemical performance in MgFeMnO₄ and related compounds. In addition, the crystal structure is unaffected by the onset of the magnetic order, which is determined to be a collinear ferrimagnetic order by neutron powder diffraction. From **μ** SR measurements it is found that the entire sample enters the ferrimagnetic state below the magnetic transition temperature **T_C ≈ 394.2 (12) K.** In the ferrimagnetic phase, no muon spin oscillations are observed in the ZF-**μ** SR time spectra, which is consistent with the ferrimagnetic spin ordering determined by neutron diffraction. Hence, the magnetic properties of MgFeMnO₄ are more similar to those of the ferrimagnetic MgFe₂O₄ than to those of the antiferromagnetic MgMn₂O₄. Our findings provide new and improved understanding for the fundamental properties of MgFeMnO₄. Consequently, the current research should also be of high importance for future potential applications within spintronics as well as battery devices.

**ASSOCIATED CONTENT**

**Supporting Information**

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.inorgchem.0c02241.

Detailed cation weight ratios obtained from ICP-AES method, images of MgFeMnO₄ particles obtained by SEM and TEM, and the electron diffraction along the main zone axis [111] and simulated pattern indexed by the cubic structure; fitting result of Mössbauer measurement using both Lorentzian peak and pseudo-Voigt peak functions (ZIP)

**Accession Codes**

CCDC 2019621 and 2021028 contain the supplementary crystallographic data for this paper. These data can be obtained free of charge via www.ccdc.cam.ac.uk/data_request/cif, or by emailing data_request@ccdc.cam.ac.uk, or by contacting The Cambridge Crystallographic Data Centre, 12 Union Road, Cambridge CB2 1EZ, UK; fax: +44 1223 336033.

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Notes
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