Sensitivity of young water fractions to hydro-climatic forcing and landscape properties across 22 Swiss catchments

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Received: 8 December 2017 – Discussion started: 18 December 2017
Revised: 14 June 2018 – Accepted: 25 June 2018 – Published: 19 July 2018

Abstract. The young water fraction $F_{yw}$, defined as the proportion of catchment outflow younger than approximately 2–3 months, can be estimated directly from the amplitudes of seasonal cycles of stable water isotopes in precipitation and streamflow. Thus, $F_{yw}$ may be a useful metric in catchment inter-comparison studies that investigate landscape and hydro-climatic controls on streamflow generation. Here, we explore how $F_{yw}$ varies with catchment characteristics and climatic forcing, using an extensive isotope data set from 22 small- to medium-sized (0.7–351 km$^2$) Swiss catchments. We find that flow-weighting the tracer concentrations in streamwater resulted in roughly 26 % larger young water fractions compared to the corresponding unweighted values, reflecting the fact that young water fractions tend to be larger when catchments are wet and discharge is correspondingly higher. However, flow-weighted and unweighted young water fractions are strongly correlated with each other among the catchments. They also correlate with terrain, soil, and land-use indices, as well as with mean precipitation and measures of hydrologic response. Within individual catchments, young water fractions increase with discharge, indicating an increase in the proportional contribution of faster flow paths at higher flows. We present a new method to quantify the discharge sensitivity of $F_{yw}$, which we estimate as the linear slope of the relationship between the young water fraction and flow. Among the 22 catchments, discharge sensitivities of $F_{yw}$ are highly variable and only weakly correlated with $F_{yw}$ itself, implying that these two measures reflect catchment behaviour differently. Based on strong correlations between the discharge sensitivity of $F_{yw}$ and several catchment characteristics, we suggest that low discharge sensitivities imply greater persistence in the proportions of fast and slow runoff flow paths as catchment wetness changes. In contrast, high discharge sensitivities imply the activation of different dominant flow paths during precipitation events, such as when subsurface water tables rise into more permeable layers and/or the river network expands further into the landscape.

1 Introduction

Naturally occurring variations in stable water isotopes ($\delta^{18}$O, $\delta^{2}$H) or chemically passive solutes (e.g. chloride) are commonly used in catchment studies to track the flow of water and to gain insight into catchment storage and mixing behaviour (Buttle, 1994; Kendall and McDonnell, 1998; Klaus and McDonnell, 2013). Many catchment studies use these tracers to estimate time-averaged transit time distributions, to characterize the heterogeneity of flow pathways, and to estimate mobile catchment storage (e.g. Benettin et al., 2015; Birkel et al., 2011; Hrachowitz et al., 2009; Staudinger et al., 2017). Transit time distributions are often inferred from conservative tracers using lumped-parameter models (McGuire and McDonnell, 2006). Because the mean transit time expresses the ratio between mobile catchment storage and the average flow rate, it is widely used in catchment inter-comparison studies (e.g. Hrachowitz et al., 2009; McGuire et al., 2005; Staudinger et al., 2017). However, estimates of mean transit time can be biased and unreliable, especially for spatially heterogeneous catchments (Kirchner, 2016b; Seeger and Weiler, 2014). Instead, the young water
fraction $F_{yw}$ – i.e. the average fraction of streamflow that is younger than a specified threshold age – has recently been proposed as a more reliable measure of water age in heterogeneous catchments (Kirchner, 2016a, b). Young water fractions with a threshold age of roughly 2–3 months can be estimated directly from the amplitude ratio of the seasonal cycles in stable water isotopes in precipitation and streamwater.

The amplitudes of the seasonal isotopic cycles in precipitation and streamwater can be estimated directly from the isotope measurements themselves, or by volume-weighting these measurements by the corresponding precipitation or discharge rates. Precipitation isotope should generally be volume-weighted to prevent small precipitation events, potentially with anomalous isotope values, from substantially influencing the calculated seasonal precipitation isotope cycle. Streamwater isotope values can also be flow-weighted, using stream discharges as weights. Higher streamflows should typically correspond to larger young water fractions, for the simple reason that flow peaks typically follow intense rainfall and contain more recent precipitation than base flows (e.g. Kirchner, 2016b; von Freyberg et al., 2017). Hence, the flow-weighted average young water fraction (here denoted $F_{yw}^*$) is expected to be higher than the unweighted average young water fraction ($F_{yw}$). Both $F_{yw}$ and $F_{yw}^*$ are calculated over periods of a year or longer, and represent the average catchment behaviour over that time. In calculating the unweighted $F_{yw}$, each unit of time counts equally, and benchmark tests using a nonstationary lumped catchment model confirm that the calculated $F_{yw}$ should accurately reflect the time-averaged fraction of young water in discharge (Kirchner, 2016b). By contrast, in calculating the flow-weighted $F_{yw}^*$, each unit of flow counts equally, and benchmark tests confirm that the calculated $F_{yw}^*$ reflects the cumulative volume of young water, as a fraction of the cumulative volume of discharge, over the corresponding period (Kirchner, 2016b). Although $F_{yw}^*$ and $F_{yw}$ have previously been compared in benchmark tests, a systematic evaluation based on tracer data from natural catchments has not yet been carried out.

At sites where precipitation isotopes are not measured directly, catchment isotopic inputs can be estimated from nearby long-term monitoring stations using various spatial interpolation methods. These interpolation methods differ in their assumptions about temperature- and elevation-dependent isotope fractionation effects, and their treatment of seasonal snowpack storage. Based on a global database of $\delta^{18}$O in precipitation, Jasechko et al. (2016) calculated the seasonal cycle amplitudes and their standard errors for each station and interpolated them to generate a global grid of the seasonal cycle amplitudes. These interpolated coefficients were volume-weighted by the spatial pattern of precipitation over each catchment. An alternative approach (Allen et al., 2018; see Supplement) builds on the Jasechko et al. (2016) method with an additional step that accounts for the residuals of the observations from the fitted seasonal cycles. To generate a high-resolution precipitation isotope map for Switzerland, Seeger and Weiler (2014) interpolated $\delta^{18}$O in monthly precipitation from long-term monitoring stations in central Europe, using an elevation-gradient approach. They combined their interpolation method with an energy-balance-based snow model to estimate the liquid input to the soil surface at monthly temporal resolution. The latter two interpolation methods have been rigorously tested with real-world isotope measurements, and thus may be particularly useful for estimating young water fractions in catchments where no long-term precipitation isotope measurements exist.

Another analytical decision that affects the interpretation of $F_{yw}^*$ and $F_{yw}$ relates to whether snowpack storage is considered to be part of catchment storage, or not. If one measures precipitation to the snow surface as the catchment input, then snowpack accumulation and melt are implicitly included in catchment storage (e.g. Staudinger et al., 2017). In this case, comparisons of seasonal cycles in precipitation and streamflow should reflect the young water fraction resulting from the combination of snowpack and subsurface storage. Alternatively, if one uses precipitation and snowmelt arriving at the soil surface as the catchment input (for example, with melt pan lysimeters, or modelled snowpack outflows), then snowpack accumulation and melt are implicitly excluded from catchment storage. In this case, comparisons of seasonal cycles in streamflow and sub-snowpack catchment input should reflect the young water fraction resulting from subsurface storage alone. Because the total catchment storage in the first case (including snowpack storage) is larger than the subsurface storage alone, the resulting young water fractions are expected to be smaller. Previous studies that estimated young water fractions in snow-dominated watersheds (Jasechko et al., 2016; Song et al., 2017) did not differentiate between these two concepts of catchment storage and simply used incoming precipitation in the young water fraction calculations, thus implicitly considering snowpack storage as part of catchment storage (as in the first case outlined above). This approach is practical in view of the challenges of measuring or modelling snowmelt and its isotopic composition. However, it is still unclear whether, in cases where snowmelt can be modelled or measured, explicitly considering snowmelt as a catchment input would significantly alter young water fraction estimates.

Because the young water fraction can be estimated from sparse and irregular tracer data, it has been suggested as a useful metric for catchment inter-comparison studies (Kirchner, 2016a). To date, however, most catchment inter-comparison studies have investigated controls on mean transit times instead. Mean transit times have been variably found to be correlated with (for example) flow path lengths and gradients (McGuire et al., 2005), drainage density (Soulsby et al., 2010), the areal fraction of hydrologically responsive soils (Tetzlaff et al., 2009), bedrock permeability (Hale and McDonnell, 2016), or combinations of multiple factors (Hrachowitz et al., 2009; Seeger and Weiler, 2014). So far,
only a few catchment inter-comparison studies have used young water fractions (Song et al., 2017; Stockinger et al., 2016; Jasechko et al., 2016). A global analysis of 254 watersheds, revealed large spatial variability in young streamflow, which correlated inversely with average topographic gradients and water table depths (Jasechko et al., 2016). Jasechko et al. (2016) hypothesized that steeper landscapes are associated with more pervasive rock fracturing, deeper infiltration, and reduced shallow lateral flow, all of which would reduce the young water fraction in steep terrain. However, the correlation between topographic steepness and young water fractions was highly scattered, indicating that other factors are also involved. Jasechko et al.’s (2016) study sites were mostly larger than 1000 km² (25th percentile 1753 km², median 10 800 km²) and thus were probably affected by a complex interplay of landscape characteristics, climatic variability, and human impacts. Identifying landscape and climatic drivers that potentially control catchment storage behaviour may be easier in small- to medium-sized catchments with near-natural streamflow regimes (Holko et al., 2015).

In the present study, we use seasonal cycles in δ¹⁸O to estimate young water fractions for 22 sites in Switzerland with catchment areas between 0.7 and 351 km². In a first step, we evaluate how choices of methodology affect the young water fraction estimates, with emphasis on (i) the spatial interpolation method for precipitation isotopes, (ii) the conceptual representation of snow storage, and (iii) flow-weighting the streamwater isotope data. Because the 22 study catchments cover a wide range of landscape and hydro-climatic characteristics, in the second part of this study, we test for correlations between the young water fraction and a wide range of landscape and hydro-climatic indices. Finally, we present a method for estimating the linear dependence of the young water fraction on the streamflow regime and propose that the slope of this relationship may be a diagnostic indicator of streamflow generation processes.

2 Theoretical background: young water fractions from seasonal cycles of stable water isotopes in precipitation and streamwater

The isotopic composition of precipitation follows a seasonal cycle (Feng et al., 2009). The damping and phase shift of this seasonal cycle as it is transmitted through catchments (Fig. 1) can be used to infer timescales of catchment storage and transport (e.g. DeWalle et al., 1997; Soulsby et al., 2006). Sine-wave fitting can quantify the amplitude ratio \( A_S / A_P \) and phase shift \( \varphi_S - \varphi_P \) between the seasonal isotope cycles in precipitation and streamflow (the indices P and S refer to precipitation and streamwater, respectively). The seasonal isotope cycles in precipitation and streamwater can be described by:

\[
c_P(t) = A_P \sin(2 \pi f t - \varphi_P) + k_P
\]

and

\[
c_S(t) = A_S \sin(2 \pi f t - \varphi_S) + k_S.
\]

In Eqs. (1) and (2), \( A \) is the amplitude (‰), \( \varphi \) is the phase of the seasonal cycle (in radians, with \( 2 \pi \) rad equalling 1 year), \( t \) is the time (decimal years), \( f \) is the frequency (yr⁻¹), and \( k \) (‰) is a constant describing the vertical offset of the isotope signal.

If one assumes that the transit times of water through the catchment follow a particular transit time distribution, the mean transit time can be calculated as a function of the amplitude ratio \( A_S / A_P \). However, mean transit times inferred from seasonal tracer cycles in runoff from heterogeneous catchments are potentially subject to severe aggregation bias (Kirchner, 2016a). Alternatively, the amplitude ratio \( A_S / A_P \) can be used to estimate the fraction of water younger than a specified threshold age. Compared to the mean transit time, this “young water fraction” \( F_{yw} \) is markedly less vulnerable to aggregation bias, and less sensitive to the assumed shape of the catchment transit time distribution (Kirchner, 2016a, b). For a wide range of transit time distributions, the young water threshold age is approximately 2.3 ± 0.8 months (Kirchner, 2016a).

We can estimate the amplitudes \( A_S \) and \( A_P \) of the seasonal isotope cycles in Eqs. (1) and (2) by using multiple linear regression to obtain the coefficients \( a \) and \( b \) in

\[
c_P(t) = a_P \cos(2 \pi f t + b_P \sin(2 \pi f t) + k_P
\]

and

\[
c_S(t) = a_S \cos(2 \pi f t) + b_S \sin(2 \pi f t) + k_S.
\]

The amplitudes \( A_S \) and \( A_P \) are then determined by

\[ A_P = \sqrt{a_P^2 + b_P^2} \]

and

\[ A_S = \sqrt{a_S^2 + b_S^2}. \]

Following Kirchner (2016a), we calculate young water fractions as the amplitude ratio \( A_S / A_P \). We estimate the coefficients \( a_S \), \( b_S \), \( a_P \), and \( b_P \) by fitting Eqs. (3) and (4) using iteratively re-weighted least squares (IRLS), a robust estimation method that minimizes the influence of any potential outliers (an R script with our IRLS code is provided in the Supplement). In estimating \( a_P \) and \( b_P \), we volume-weight Eq. (3) to avoid giving undue leverage to low-precipitation periods. To calculate the unweighted young water fraction \( F_{yw} \), we estimate \( a_S \) and \( b_S \) from Eq. (4) using unweighted IRLS. For the flow-weighted young water fraction \( F_{yw}^f \), we estimate \( a_S \) and \( b_S \) from Eq. (4) using discharge-weighted IRLS (see the R script provided in the Supplement). Uncertainties in the calculated unweighted and flow-weighted young water fractions are expressed as standard errors (SEs) and are estimated using Gaussian error propagation.
Figure 1. Hydrologic and isotopic seasonality of precipitation and streamflow for the Erlenbach and Dischmabach catchments. Precipitation isotopes were interpolated with the method of Seeger and Weiler (2014). Sinusoidal cycles were fitted to the isotope data using iteratively re-weighted least squares regression. The seasonal cycles of the streamwater isotopes exhibit damping and phase shifts relative to the precipitation isotopic cycles. Stronger damping of the seasonal isotope cycle, implying a smaller fraction of young water in streamflow, can be observed in the Dischmabach catchment.

3 Data set

The 22 study catchments cover areas between 0.7 and 351 km$^2$ and have mean elevations between 472 and 2369 m a.s.l. (Table 1). Most of the sites are located in the Swiss Plateau and in the northern Alps, where the geology is characterized by sedimentary rocks (limestones, sandstones, marls, marly shales, conglomerates, breccias) and unconsolidated sediments (clay, silts, sands). In the southern Alps, two high-elevation catchments (Dischmabach and Riale di Calneggia) are predominantly underlain by metamorphic rock (mica schist, gneiss), and Ova da Cluozza is the only study catchment underlain by dolomite (Fig. 2a and b).

Land use at lower elevations (400–800 m) is predominantly agriculture, while grassland and forests can be found at elevations up to around 1400 m. Much of the area above 1700 m is characterized by grasses, shrubs, and sparse vegetation. At two high-elevation sites, Dischmabach and Ova da Cluozza, up to ∼2% of the drainage area is covered by glaciers. At all sites, the human influence on river discharge is small, resulting in near-natural streamflow regimes.

Switzerland is characterized by a humid to temperate continental climate, with the Alps creating climatically distinct subregions. The wettest regions can be found in the northern pre-Alps and Alps, as well as in the canton of Ticino south of the Alps. The driest regions are located in inner Alpine valleys in the cantons of Valais and Grisons (Fig. 2c). Average annual precipitation rates for the 22 catchments range from 887 to 1853 mm based on observations from 2000 to 2015 (Table 1). To differentiate between the hydro-climatic regimes of the catchments, we grouped them into three classes (snow-dominated, rainfall-dominated, and hybrid) proposed by Staudinger et al. (2017).
Table 1. General properties of the 22 study catchments and streamwater isotope time series.

<table>
<thead>
<tr>
<th>Catchment name</th>
<th>Gauging station</th>
<th>Longitude (WGS84)</th>
<th>Latitude (WGS84)</th>
<th>Area (km²)</th>
<th>Mean elevation (range) (m)</th>
<th>Average annual precipitation* (mm)</th>
<th>Hydro-climatic regime</th>
<th>Sampling period for δ¹⁸O in streamwater (number of samples)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aabach</td>
<td>Mönchaldorf</td>
<td>8.7206</td>
<td>47.3110</td>
<td>49.0</td>
<td>635 (519–1092)</td>
<td>1358</td>
<td>Rainfall-dominated</td>
<td>Sep 2010–Feb 2013 (62)</td>
</tr>
<tr>
<td>Allenbach</td>
<td>Adelboden</td>
<td>7.5521</td>
<td>46.4860</td>
<td>28.8</td>
<td>1852 (1293–2742)</td>
<td>1338</td>
<td>Snow-dominated</td>
<td>Sep 2010–May 2015 (87)</td>
</tr>
<tr>
<td>Alp</td>
<td>Einsiedeln</td>
<td>8.7393</td>
<td>47.1508</td>
<td>46.5</td>
<td>1154 (845–1894)</td>
<td>1776</td>
<td>Hybrid</td>
<td>May 2010–2011/2015 (131)</td>
</tr>
<tr>
<td>Biber</td>
<td>Biberbrugg</td>
<td>8.7209</td>
<td>47.1534</td>
<td>31.6</td>
<td>999 (827–1495)</td>
<td>1658</td>
<td>Rainfall-dominated</td>
<td>May 2010–Nov 2015 (140)</td>
</tr>
<tr>
<td>Emme</td>
<td>Eggwil, Heidbüel</td>
<td>7.8047</td>
<td>46.8711</td>
<td>127.0</td>
<td>1285 (743–2216)</td>
<td>1372</td>
<td>Hybrid</td>
<td>Jun 2010–Nov 2013 (71)</td>
</tr>
<tr>
<td>Ergolz</td>
<td>Liestal</td>
<td>7.7342</td>
<td>47.4882</td>
<td>261.2</td>
<td>584 (305–1165)</td>
<td>1081</td>
<td>Rainfall-dominated</td>
<td>Jun 2010–Nov 2015 (140)</td>
</tr>
<tr>
<td>Erlenbach</td>
<td>Erlenbach</td>
<td>8.8089</td>
<td>47.0452</td>
<td>0.7</td>
<td>1359 (1117–1650)</td>
<td>1853</td>
<td>Hybrid</td>
<td>Jul 2010–May 2015 (140)</td>
</tr>
<tr>
<td>Guebne</td>
<td>Belp, Mülimatt</td>
<td>7.5155</td>
<td>46.7888</td>
<td>55.4</td>
<td>1037 (556–2152)</td>
<td>1236</td>
<td>Hybrid</td>
<td>Jul 2010–Dec 2012 (64)</td>
</tr>
<tr>
<td>Illis</td>
<td>Lägna</td>
<td>7.7975</td>
<td>46.3793</td>
<td>187.9</td>
<td>1037 (681–2087)</td>
<td>1443</td>
<td>Hybrid</td>
<td>Jul 2010–May 2015 (128)</td>
</tr>
<tr>
<td>Langeten</td>
<td>Hüttwil, Häberenbad</td>
<td>7.8287</td>
<td>47.1225</td>
<td>60.3</td>
<td>760 (598–1100)</td>
<td>1297</td>
<td>Rainfall-dominated</td>
<td>Jul 2010–May 2015 (103)</td>
</tr>
<tr>
<td>Lümpenbach</td>
<td>Lümpenbach</td>
<td>8.7052</td>
<td>46.4067</td>
<td>0.9</td>
<td>1336 (1092–1508)</td>
<td>1803</td>
<td>Hybrid</td>
<td>Oct 2010–Nov 2015 (132)</td>
</tr>
<tr>
<td>Mentue</td>
<td>Yvonand, La Mauguettaz</td>
<td>6.7242</td>
<td>46.7768</td>
<td>105.0</td>
<td>679 (447–926)</td>
<td>1097</td>
<td>Rainfall-dominated</td>
<td>Jul 2010–Feb 2013 (63)</td>
</tr>
<tr>
<td>Murg</td>
<td>Waengi</td>
<td>8.9529</td>
<td>47.4963</td>
<td>76.8</td>
<td>648 (467–1036)</td>
<td>1314</td>
<td>Rainfall-dominated</td>
<td>Jul 2010–Nov 2014 (95)</td>
</tr>
<tr>
<td>Reitholzach</td>
<td>Mosnang, Reitholz</td>
<td>9.0123</td>
<td>46.3793</td>
<td>3.2</td>
<td>794 (671–938)</td>
<td>1415</td>
<td>Rainfall-dominated</td>
<td>Jul 2010–Feb 2013 (68)</td>
</tr>
<tr>
<td>Sense</td>
<td>Thoerenhaus, Sensemat</td>
<td>7.3514</td>
<td>46.8883</td>
<td>351.2</td>
<td>1068 (554–2184)</td>
<td>1258</td>
<td>Hybrid</td>
<td>Oct 2010–Mar 2013 (47)</td>
</tr>
<tr>
<td>Sitter</td>
<td>Appenzell</td>
<td>9.4104</td>
<td>47.3319</td>
<td>88.2</td>
<td>1301 (768–2500)</td>
<td>1771</td>
<td>Hybrid</td>
<td>Nov 2010–May 2015 (97)</td>
</tr>
<tr>
<td>Vogelbach</td>
<td>Vogelbach</td>
<td>8.7161</td>
<td>47.0761</td>
<td>1.6</td>
<td>1335 (1038–1540)</td>
<td>1800</td>
<td>Hybrid</td>
<td>Jun 2010–Nov 2015 (139)</td>
</tr>
</tbody>
</table>

* Based on interpolated data from PREVAH and the time period January 2000–December 2015.
distributed more-or-less evenly throughout the year, although peak inputs to the soil surface (melt and precipitation) are shifted towards spring and summer in all snow-dominated sites and some hybrid sites.

3.1 Hydro-climatic data

Daily discharge data for 18 of the 22 sites were provided by the Swiss Federal Office for the Environment. Discharge measurements for the Aabach catchment were made available by the Office for Water, Energy and Air (WWEA) of the canton of Zurich. Discharge data for the Erlenbach, Vogelbach, and Lümpenenbach catchments were provided by the Swiss Federal Institute for Forest, Snow and Landscape Research (WSL), Birmensdorf, Switzerland.

Meteorological data for each site and each 100 m elevation band were interpolated from measurements taken by the national meteorological service of Switzerland (MeteoSwiss), using the PREVAH (Precipitation-Runoff-EVapotranspiration HRU) model (Viviroli et al., 2009). Mean precipitation for each 100 m elevation band was aggregated to obtain area-weighted catchment average values.

3.2 Catchment properties

The average hydro-climatic properties at the sites were described by various indices, such as mean monthly values of discharge $Q$ and precipitation $P$, as well as mean daily precipitation intensity $P_{\text{intensity}}$. To quantify the variability of the flow regimes, we determined the average coefficient of variation of daily discharge ($CV_Q$) and the quick-flow index (QFI). The QFI is the average ratio between $(Q - Q_{bf})$ and $Q$, where $Q$ is daily discharge and $Q_{bf}$ is daily baseflow; $Q_{bf}$ was calculated with the “BaseflowSeparation” function in the EcoHydRology package (version 0.4.12) in R using a recursive digital filter parameter of 0.925, as recommended by Nathan and McMahon (1990). All of these hydro-climatic indices were calculated for each site and for the duration of the site-specific streamwater isotope sampling campaigns, which varied between approximately 1 and 5 years (Table 1).

The seasonal variability of monthly precipitation for the years 2000–2015 was expressed through the amplitude and the phase shift of a fitted sinusoidal function (Berghuijs et al., 2014):

$$P(t) = \overline{P}[1 + A_{\text{precip}} \sin(2\pi (t - \psi_{\text{precip}})/\tau)].$$

(6)

where $P$ is the precipitation volume (mm month$^{-1}$), $\overline{P}$ is the average of $P$ (mm month$^{-1}$), $A_{\text{precip}}$ is the seasonal amplitude of precipitation ($\sim$), $t$ is the time (months), $\tau$ is the duration of a full seasonal cycle (12 months), and $\psi_{\text{precip}}$ is the phase (months). The phase describes the offset from the beginning of the seasonal cycle, which is defined here as 1 January. The parameters $A_{\text{precip}}$ and $\psi_{\text{precip}}$ were obtained by non-linear fitting to the monthly precipitation data using Newton’s method. Strong precipitation seasonality would be expressed in a high $A_{\text{precip}}$ value.

The hydro-climatic indices are to some extent redundant with one another. unsurprisingly, mean monthly discharge ($\overline{Q}$) and mean monthly precipitation ($\overline{P}$) were significantly correlated with each other across the 22 sites. Furthermore, $\overline{Q}$ was significantly correlated with the seasonality of precipitation ($A_{\text{precip}}$), and the QFI was significantly correlated with the coefficient of variation of daily discharge ($CV_Q$) (Table 4).

To quantify the geomorphological characteristics of the study catchments, we used terrain indices (median flow path length $L$, median flow gradient $G$, the ratio $L/G$, and me-
dian topographic wetness index – TWI) which were calculated previously by Seeger and Weiler (2014) for all 22 study sites using a digital elevation model with 25 m spatial resolution. The indices $L/G$ and TWI were previously applied in numerous catchment inter-comparison studies, e.g. Hrachowitz et al. (2009), McGuire et al. (2005), and Tetzlaff et al. (2009). In addition, we calculated the drainage density DD (the total channel length divided by the catchment area) based on the official river network from the topographical landscape model of Switzerland (swissTLM3D, ©2017 swisstopo; resolution 8 m or better).

Hydrologic soil properties and vegetation cover information were extracted from geospatial data provided by the Swiss Federal Office for Agriculture (BLW, 2012) and the Swiss Federal Statistical Office (BFS, 2004), respectively. The data product “land suitability” uses six soil properties – soil depth, large particle fraction, water storage capacity, nutrient storage capacity, permeability, and soil wetness index – to generate a map of 144 different soil classes. Each soil property is ranked from 0 (very low) to 5 or 6 (very high). For our analysis, we calculated the areal fractions of aggregated soil properties that are usually associated with fast runoff processes, i.e. low water storage capacity (ranks 1–3), low permeability (rank 1–3), and high soil wetness index (i.e. saturated soils, ranks 4–5). From the data product “forest diversity” we extracted the fraction of forested area for each catchment.

The hydrogeological properties of the study sites were obtained from the official geotechnical map of Switzerland (1 : 200 000, ©2017 swisstopo). We extracted the areal fractions of low, intermediate, and high groundwater productivity. Representative groundwater table depths could not be determined for all sites due to their complex small-scale topographic and geologic heterogeneity. The hydrologic soil properties, as well as the hydrogeological properties of the individual sites, are provided in the Supplement (Table S1).

Correlations between the catchments’ young water fractions, hydro-climatic conditions, and landscape properties were assessed with the Spearman rank correlation coefficient $\rho$ (Spearman, 1987). Following conventional practice, we consider correlations with $p < 0.05$ to be statistically significant.

### 3.3 Streamwater isotope data

Streamwater grab samples were collected approximately fortnightly at 21 sites between mid-2010 and mid-2011 or later (see Table 1 for exact dates). Oxygen isotope ratios ($\delta^{18}O$) were measured with a Picarro isotope analyser (Picarro Inc., Santa Clara, CA, USA) at the University of Freiburg, Germany, and are reported here as $\delta$ values relative to the VSMOW standard. For the Rietholzbach catchment, fortnightly streamwater $\delta^{18}O$ data were provided by the Institute for Atmospheric and Climate Science at ETH Zurich.

### 3.4 Precipitation isotope data

Values of $\delta^{18}O$ in precipitation were not measured directly at the 22 study catchments. Instead, $\delta^{18}O$ values from monthly cumulative precipitation samples were interpolated from long-term observations at nearby monitoring stations (the Swiss network for Observations of Isotopes in the Water Cycle – NAQUA-ISOT, the Global Network of Isotopes in Precipitation – GNIP, and the Austrian Network of Isotopes in Precipitation – ANIP). We used two different interpolation approaches that we summarize below: method 1 after Seeger and Weiler (2014) and method 2 similar to that of Allen et al. (2018). More detailed descriptions of both interpolation methods 1 and 2 can be found in Seeger and Weiler (2014) and in the Supplement, respectively.

In method 1, we adjusted a kriging interpolation of the available precipitation isotope values from 26 long-term monitoring stations for local differences in elevation. For this, we used the monthly average elevation gradient of $\delta^{18}O$ in precipitation, estimated from three isotope monitoring stations in central Switzerland (Meiringen, Guttannen, and Grimsel, Fig. S1 in the Supplement) that cover a similar elevation range as the 22 study catchments. Method 1 can be extended using an energy-balance-based model to explicitly simulate the storage of winter precipitation in the snowpack. The energy-balance-based model uses PREVAH simulations of air temperature, wind speed, incoming shortwave radiation, and precipitation amount to predict the meltwater amounts and their average isotopic compositions for each 100 m elevation band (without considering isotopic fractionation of the snowpack and snowmelt).

In method 2, we fitted isotope data from 19 long-term monitoring stations to sine curves using least squares. We then constructed a multiple linear regression model to explain the best-fit sine parameters as functions of latitude, longitude, and elevation. These spatially varying sine parameters were used to construct interpolated seasonal cycle maps for all of Switzerland. These seasonal cycles were then adjusted using kriged interpolations of the monthly residuals of station measurements from their fitted seasonal patterns, to account for non-sinusoidal isotope dynamics. For both interpolation methods 1 and 2, monthly isotope values were mass-weighted based on the monthly elevation-dependent precipitation volumes obtained from the PREVAH model (Viviroli et al., 2009).

### 4 Methodological evaluation of the young water fraction framework

#### 4.1 Comparing two methods for spatial interpolation of $\delta^{18}O$ in precipitation

Here, we apply two different methods 1 and 2 (Sect. 3.4) for interpolating monthly precipitation isotopes from nearby
Figure 3. (a) Comparison of flow-weighted seasonal amplitudes of precipitation $\delta^{18}$O cycles ($A_P$) obtained with two different interpolation methods, method 1 (Seeger and Weiler, 2014) and method 2 (based on Allen et al., 2018; Supplement). Differences in $A_P$ between the two interpolation methods were significant for the catchments highlighted with their abbreviated names. The abbreviations for the study sites stand for Allenbach (ALL), Alp (ALP), Biber (BIB), Dischmabach (DIS), Mentue (MEN), Ova da Cluozza (OVA), Riale di Calneggia (RIA), and Sense (SEN). (b) Comparison of young water fractions derived from the two interpolation methods. High-elevation, snow-dominated catchments are marked in light blue colour. Error bars show ±1 SE.

long-term monitoring stations and compare the resulting seasonal cycles of precipitation isotopes and their effects on the calculated young water fractions. In this comparison, method 1 is used without the snow module because method 2 does not allow for explicit simulation of snow accumulation and melt.

Figure 3a shows that the seasonal precipitation isotope cycle amplitudes ($A_P$) obtained with both methods are similar for most catchments; the differences range from $-1.34 \pm 0.21 \%e$ (±SE, Mentue) to $1.35 \pm 0.29 \%e$ (Dischmabach). Method 2 results in larger $A_P$ values for five sites (Alp, Biber, Mentue, Sense, and Riale di Caneggia), compared to the results of method 1 (Fig. 3a). However, smaller $A_P$ values are obtained with method 2 for three high-elevation sites: Allenbach, Dischmabach, and Ova da Cluozza. Overall, $A_P$ spanned a range of 1.77 ‰ with method 2, compared to a larger range of 3.47 ‰ with method 1. Nevertheless, for most sites the differences in $A_P$ between the two methods are small compared to the absolute values of $A_P$, and thus the choice of the interpolation method only marginally affects the estimated young water fractions $F_{yw}$. For all sites, the absolute differences between the values of $F_{yw}$ calculated with the two interpolation methods are below 0.06 and statistically insignificant (i.e. smaller than twice their pooled uncertainties, Fig. 3b).

A systematic test of both interpolation methods using on-site, long-term precipitation isotope measurements would go beyond the scope of this study. However, method 1 was tested with isotope measurements from six stations (Seeger and Weiler, 2014), and we evaluated the performance of method 2 as described in the Supplement. Results from the two methods are likely to differ because they make different assumptions about the changes in precipitation isotopic composition with elevation. For our objectives, however, it is helpful that these two different approaches yield different $A_P$ in several cases, because it allows us to show that this level of variability in $A_P$ has only minor effects on the calculated young water fractions. Our comparison thus demonstrates that both approaches for spatially interpolating $\delta^{18}$O in precipitation yield consistent young water fraction estimates for the 22 study catchments.

4.2 The effect of snow storage on the seasonal cycle amplitudes and phases of precipitation isotopes

At high-elevation sites with seasonally cold climates, precipitation (and its isotopic signature) will be stored temporarily in the snowpack in winter, and will be released during the melt season. Thus, significant volumes of isotopically depleted snow meltwater may reach the river system during spring and early summer, when the isotope signal of incoming precipitation is more enriched. As a result, the seasonal isotopic variation in water reaching the soil surface (rainwater and snowmelt) is likely to be smaller than the seasonal variation in precipitation alone.

In order to investigate the effect of snow storage on the amplitudes and phases of precipitation isotope cycles, we applied method 1 with the snow module, so that the input to the soil surface, and its isotope signal, can be described by a mixture of rainwater and snowmelt (the “delayed input” scenario in Fig. 4). Alternatively, method 1 can also be applied without the snow module, i.e. by ignoring snowpack as a separate storage, such that the catchment input is taken directly from the incoming precipitation and its isotopic composition (the “direct input” scenario in Fig. 4). Figure 4a shows, as an example, the time series of input water flux and $\delta^{18}$O (not volume-weighted) at the Dischmabach catchment for both scenarios. The delayed release of depleted winter precipitation from the snowpack (“delayed input” scenario) results in a smaller seasonal amplitude of the input tracer signal. However, when this input tracer signal is volume-weighted,
the fitted seasonal amplitudes ($A_P$) are statistically indistinguishable between the “direct” and “delayed” input scenarios for 21 of the 22 sites (Fig. 4b). This result arises because the “delayed” input scenario gives very little weight to winter inputs in snow-dominated catchments (because snowmelt volumes during winter conditions are small), allowing the fitted cycles to deviate from the winter isotope values. The difference in $A_P$ for both scenarios is statistically significant only at the Schaechen catchment, which contains the highest-elevation snowpacks in our data set (elevation up to 3260 m a.s.l., Table S1). As a consequence, snowmelt at the Schaechen site is isotopically more depleted compared to the other, lower-elevation sites. For the hybrid and rain-dominated sites, the $A_P$ values are almost indistinguishable between the two scenarios, either because snowmelt occurs early in the season when rainwater and snowmelt have similar isotopic signatures (i.e. hybrid catchments), or because the contribution of snowmelt is small compared to that of rainfall (rain-dominated catchments). As a consequence, the young water fractions $F_{yw}$ are virtually identical between the “direct input” and “delayed input” scenarios (Fig. 4c).

As can be seen in Fig. 4a, the delayed meltwater input shifts the seasonal isotope pattern toward later in the season. Thus the “delayed input” scenario results in later cycle phases ($\varphi_P$) compared to the “direct input” scenario (Fig. 4d), with statistically significant differences for the five high-elevation, snow-dominated sites and for four hybrid catchments (Erlenbach, Lümpenbach, Vogelbach, and Sitter). However, the “delayed input” scenario had a statistically significant effect on the phase shift between input and output.
output ($\varphi_S - \varphi_F$) only at Dischmabach (where it altered the phase shift by 0.06 years) and Riale di Calneggia (where it altered the phase shift by 0.07 years; Fig. 4e). In the analysis presented below, we use interpolated precipitation isotope values obtained with method 1 that explicitly account for snowpack accumulation and melt (i.e. the “delayed input” scenario) in order to be consistent with previous studies where this data set has been used (Seeger and Weiler, 2014; Staudinger et al., 2017).

4.3 Comparing unweighted and flow-weighted young water fractions

We use the isotope and discharge data sets of the 22 catchments to estimate young water fractions from the ratios of the seasonal cycle amplitudes $A_S$ and $A_F$, with and without discharge-weighting ($F_{yw}^* \text{ and } F_{yw}$, respectively). Figure 5a shows that flow-weighting the streamwater isotope values results in a roughly 25% increase in the fitted seasonal streamwater isotope cycle amplitudes $A_S$, relative to the unweighted $A_S$ values for the same sites. Statistically significant differences between unweighted and flow-weighted values of $A_S$ were found for Dischmabach, Emme, Mentue, Rietholzbach, and Sense, as well as Alp, Erlenbach, Lümpenbach, Vogelbach, and Biber (which are all located nearby one another and share similar catchment characteristics).

Perhaps unsurprisingly, the effect of flow-weighting on $A_S$ is largest in catchments with highly variable flow regimes, i.e. at sites with relatively large coefficients of variation of daily discharge ($CV_Q$) and QFI (Table 2). In such catchments, robust estimation of the flow-weighted $F_{yw}^*$ may require a smart sampling strategy that captures a representative range of hydrologic conditions.

The flow-weighted $F_{yw}^*$ values range from 0.07 ± 0.01 to 0.49 ± 0.03 (±SE), whereas the unweighted $F_{yw}$ values range from 0.06 ± 0.01 to 0.37 ± 0.03. Thus, flow-weighting the streamwater isotope values yields young water fractions ($F_{yw}^*$) that are around 26% larger than those calculated from unweighted streamwater isotope values ($F_{yw}$: Fig. 5b, Table 3), because high flows generally contain more young water than base flows. The average values of $F_{yw}^*$ and $F_{yw}$ are 0.22 ± 0.02 and 0.17 ± 0.02, respectively, meaning that approximately one-fifth of total discharge was younger than roughly 2.3 ± 0.8 months (assuming that the catchment transit times can be described by gamma distributions with shape factors $\alpha$ ranging from 0.3 to 2; Kirchner, 2016a). Our $F_{yw}$ results are within the range of young water fractions reported for rivers in mountainous regions in North America and central Europe by Jasechko et al. (2016).

5 Relationships between young water fractions, hydro-climatic conditions, and landscape characteristics

By examining how the catchments’ young water fractions correlate with their landscape and hydro-climatic characteristics, we aim to identify dominant controls on their hydrological behaviour. Below, we present our results for flow-weighted young water fractions ($F_{yw}^*$); however, the unweighted young water fractions ($F_{yw}$) yield very similar results, as both values are significantly correlated with each other ($\rho = 0.9$, $p < 0.001$; Table 4).

Table 4 and Fig. 6 show that young water fractions exhibit statistically significant positive correlations with five hydro-climatic indices: mean monthly discharge ($\bar{Q}$), mean monthly precipitation ($\bar{P}$), mean daily precipitation intensity ($\bar{P}_{intensity}$), coefficient of variation of daily discharge ($CV_Q$), and QFI. These correlations suggest that
Table 2. Hydro-climatic and topographic indices, as well as soil properties of the 22 study catchments.

<table>
<thead>
<tr>
<th>Catchment name</th>
<th>Quick-flow index QFI (–)</th>
<th>Coefficient of variation of ( Q ) (%)</th>
<th>Average discharge ( Q ) (mm month(^{-1}))</th>
<th>Average precipitation ( P ) (mm month(^{-1}))</th>
<th>Precipitation amplitude ( A_{\text{precip}} ) (mm month(^{-1}))</th>
<th>Median flow path length ( L ) (m)</th>
<th>Median flow path gradient ( G ) (m m(^{-1}))</th>
<th>( L / G ) (m)</th>
<th>Drainage density, DD (km km(^{-2}))</th>
<th>Mean topographic gradient (%)</th>
<th>Median topographic wetness index TWI (–)</th>
<th>Fraction forested area (%)</th>
<th>Fraction low-permeable soils (%)</th>
<th>Fraction saturated soils (%)</th>
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young water fractions tend to be highest in humid catchments where prompt runoff response is facilitated by fast flow paths and/or high-intensity precipitation events. $F_{yw}$ was also significantly correlated with high values of drainage density (DD) and low values of flow path length ($L$) (Table 4). There was also a significant negative correlation with the ratio of the flow path length to gradient ($L/G$), but as there is nearly zero correlation with $G$ itself, the correlation with $L/G$ apparently arises through $L$ alone. Drainage density is inversely proportional to median flow path length, so the strong positive correlation of $F_{yw}$ with DD and negative correlation with $L$ can be viewed as two sides of the same coin. All else equal, high values of DD, and thus small values of $L$, facilitate faster runoff, which is directly linked to $F_{yw}$. Some studies have identified catchment area as a major control on mean transit times (e.g. DeWalle et al., 1997; Soulsby et al., 2000), however, the inverse correlation of $F_{yw}$ with catchment area only becomes significant ($\rho = -0.49$, $p < 0.05$) when the five high-elevation, snow-dominated sites are omitted from the analysis (Fig. 6). The young water fractions of the remaining 17 sites were also strongly correlated with mean catchment elevation ($\rho = 0.65$, $p < 0.005$, Fig. 6), which in turn is a major control on other hydro-climatic indices ($Q$, $P$, and topographic indices (DD, $G$, $L$, $L/G$, and TWI)).

Figure 6. Scatter plots showing how young water fractions correlate with climatic and landscape indices. High-elevation, snowmelt-dominated sites are marked in light blue. Error bars show ±1 SE. Spearman rank correlation coefficients ($\rho$) and corresponding $p$ values are provided in the individual figures.
Across the 22 catchments, $F_{yw}$ is positively correlated with the areal fraction of saturated soils ($\rho = 0.58$, $p < 0.01$) and low-permeability soils ($\rho = 0.52$, $p < 0.05$). These relationships remain significant when the snow-dominated sites are omitted from the analysis. A strong positive relationship with $F_{yw}$ can be expected because saturated soils and low-permeability soils are often associated with overland flow and/or fast subsurface flow mechanisms triggered by exceedance of soil water storage thresholds (saturation excess; Dunne and Black, 1970) or precipitation intensity (infiltration excess; Horton, 1933). Particularly high fractions of saturated soils occur at three neighbouring catchments (Erlenbach, Lümpenbach and Vogelbach) that are characterized by shallow gleysols (Feyen et al., 1996; Fischer et al., 2015). Together with the nearby Biber catchment, these four sites exhibit the largest young water fractions in our data set. No correlation was evident between $F_{yw}$ and the fraction of soils with low water storage capacity, likely due to the strong influence of six sites where this fraction was zero.

$F_{yw}$ is not significantly correlated with the areal fractions mapped as having high, intermediate, or low groundwater productivity, here used as a proxy for the catchments’ hydrogeologic properties. This result is perhaps unsurprising; most groundwater is probably older than the threshold age that defines young water, so the young water fraction will not be sensitive to how much older the groundwater is. Instead, the fraction of young water should primarily reflect mechanisms that control flow processes and routing near the land surface (shallow groundwater, soil water, overland flow) rather than groundwater flow in deep aquifers where flow velocities can be several orders of magnitude slower.

Across our study catchments, the young water fraction is strongly correlated with the areal fraction of forest ($\rho = 0.58$, $p < 0.01$; Tables 1 and 4). Excluding the snow-dominated sites from the analysis slightly weakens this relationship although it remains statistically significant ($\rho = 0.51$, $p < 0.05$). One would normally expect tree roots to increase soil permeability, resulting in greater infiltration and groundwater recharge (Brantley et al., 2017). However, on steep forested slopes, abundant lateral preferential flow pathways (e.g. macropores) may facilitate rapid transport of water (Whipkey, 1965). Thus, the correlation we observe may be artefactual, since across our sites, forest cover is also correlated with higher drainage densities and shorter mean
Table 4. Spearman rank correlation coefficients relating the flow-weighted \( F_{yw} \) and unweighted \( F_{uw} \) young water fractions, and the discharge sensitivity of \( F_{yw} \), to selected hydro-climatic indices and landscape properties of the 22 Swiss catchments. The corresponding \( p \) values are indicated by regular font in grey fields (\( p < 0.05 \)), bold font in grey fields (\( p < 0.01 \)), as well as italic and underlined font in grey fields (\( p < 0.001 \); fields without grey shading indicate \( p > 0.05 \).
Figure 7. Variation in unweighted young water fractions with flow regime (log-transformed) for the nine Swiss catchments that have sufficiently long time series of streamwater isotope measurements. Error bars show ±1 SE. The young water fraction increases with discharge differently at different sites, suggesting different degrees of activation of fast flow paths at high flows.

flow paths, as well as higher fractions of saturated and low-permeability soils, all of which can plausibly increase the young water fraction. More generally, among our 22 study sites, hydro-climatic characteristics are correlated with landscape properties, making it challenging to clearly identify individual controls on the young water fraction. Broadly, however, we can conclude that high young water fractions are generally associated with hydro-climatic factors (e.g. humid climate and high precipitation intensity) and landscape characteristics (e.g. low soil permeability and high drainage density) that facilitate fast streamflow responses.

5.1 Discharge sensitivity of the young water fraction as a diagnostic indicator of runoff generation processes

The catchment inter-comparison analysis presented in Sect. 5 suggests that wetter catchments, and those with shorter and faster flow paths, have larger young water fractions. In individual catchments, one would also expect young water fractions (and thus seasonal isotope cycles) to be variable in time, i.e. to be larger during periods of stronger precipitation forcing and wetter antecedent conditions, as shallower, faster flow paths become more dominant, and as the stream network extends farther into the landscape, shortening the average path length of subsurface flow (Godsey and Kirchner, 2014). In this section, we examine how young water fractions respond to changes in catchment wetness, as reflected in stream discharge.

5.2 Young water fractions of distinct flow regimes

Our expectation that the young water fraction should be higher under wetter conditions (and thus during higher stream discharges) is borne out by the observation that flow-weighted young water fractions are systematically higher than unweighted young water fractions (Sect. 4.3). We can visualize the relationship between $F_{yw}$ and stream discharge (as a proxy for catchment wetness) by separating the streamwater isotope time series into different discharge ranges and calculating the seasonal isotope cycles and $F_{yw}$ values individually for each of these flow regimes. These flow regimes comprise the 1st to 4th quartiles, as well as the upper 20 and 10% of daily discharges at the day of sampling. For instance, from the 140 streamwater isotope samples at the Erlenbach site, each quartile of $Q$ comprised 35 samples, while the upper 20 and 10%, of daily discharges comprised 28 and 14 samples, respectively. In Fig. 7, we plot $F_{yw}$ in relation to the median discharge values of the six flow regimes at nine of our study sites. These sites have the longest isotope time series in our data set, allowing us to estimate robust seasonal cycle coefficients $A_S$ for each individual flow regime. At our sites with shorter time series, sub-sampling individual flow regimes would result in highly uncertain $A_S$ estimates.

The visual patterns shown in Fig. 7 are similar for catchments located close to each other, such as for Alp and Biber, or for Lümpenenbach, Vogelbach, and Erlenbach. However, young water fractions vary substantially among the sites in Fig. 7, with $F_{yw}$ in the lowest flow regime ranging from 0.03 at Dischmabach to 0.29 at Erlenbach and $F_{yw}$ in the highest flow regime ranging from 0.13 at Ilfis to 0.60 at Biber. Figure 7 suggests that the relationship between discharge and $F_{yw}$ may be a diagnostic fingerprint linked to hydrological properties that control the storage and release of young water. However, the nine catchments shown in Fig. 7 are too small of a sample to draw any robust conclusions concerning
how this fingerprint may vary with catchments’ landscape characteristics and hydro-climatic conditions.

5.3 Estimating the discharge sensitivity of $F_{yw}$ and linking it to catchments’ landscape and hydro-climatic characteristics

As a first-order estimate of the sensitivity of $F_{yw}$ to discharge across all 22 study catchments, we calculated the linear slope of the relationship between $Q$ and $F_{yw}$, using a method that does not require breaking the streamwater isotope time series into separate flow regimes (and thus has more modest data requirements than plots like Fig. 7). Instead of fitting a linear slope to the few data points shown in Fig. 7, we estimated the linear slope of the $Q$–$F_{yw}$ relationship directly from the tracer time series $c_S(t)$ and $c_P(t)$. For each site, we assume that the seasonal amplitude of precipitation isotopes ($A_P$) is independent of $Q$, leaving the seasonal amplitude of streamwater isotopes $A_S$ as the only flow-rate-dependent variable. If $A_S$ varies with discharge but $A_P$ does not, then the young water fraction $F_{yw}$ varies with $Q$ as follows:

$$F_{yw}(Q) = A_S(Q)/A_P.$$  

If we approximate $A_S$ as a linear function of $Q$,

$$A_S(Q) = n_S + m_S Q,$$

we can estimate the linear slope ($m_S$) and the intercept ($n_S$) through nonlinear fitting (analytic Gauss–Newton algorithm) by replacing $A_S$ in Eq. (2) with $A_S(Q)$ from Eq. (6), yielding the following:

$$c_S(t) = (n_S + m_S Q) \cdot \sin(2\pi f t - \phi_S) + k_S.$$  

In Eq. (8), $\phi_S$ is the phase of the seasonal streamwater isotope cycle (rad), $t$ is the time (decimal year), $f$ is the frequency (yr$^{-1}$), and $k_S$ (‰) is a constant describing the vertical offset of the streamwater isotope signal. For the sake of simplicity, Eq. (8) assumes that the amplitude of the seasonal cycle varies with $Q$ but the phase $\phi_S$ does not. Numerical experiments (e.g. Fig. 8 in Kirchner, 2016b) suggest that the change in streamwater isotope cycle phase $\phi_S$ between high and low flows should have only a minor influence on the estimate of the parameters in Eq. (8), because the change in $\phi_S$ can only be large when the cycle is strongly damped (i.e. during low-flow conditions), and the phase of such a strongly damped cycle will have little effect on the fit to the data.

Combining Eqs. (6) and (7) yields

$$F_{yw}(Q) = \frac{n_S + m_S Q}{A_P} = \frac{n_S}{A_P} + \frac{m_S Q}{A_P}$$

and thus, the linear slope of the dependence of $F_{yw}$ on $Q$ can be approximated as $m_S/A_P$, which has units of $Q^{-1}$. The uncertainty in this slope was estimated through Gaussian error propagation. Please note that Eq. (9) quantifies discharge sensitivity based on the linear slope of the relationship between $F_{yw}$ and $Q$, whereas Fig. 7 shows how $F_{yw}$ varies with log($Q$) for different fractions of the discharge distribution. By replacing $Q$ with log($Q$) in Eqs. (6)–(9), one could easily determine the linear slope of the relationship between $F_{yw}$ and log($Q$) instead.

For convenience, we term this linear slope of the $Q$–$F_{yw}$ relationship the “discharge sensitivity” of $F_{yw}$. Our use of this term should not be interpreted to mean that $F_{yw}$ depends, in a mechanistic sense, on discharge per se. Instead, we use the term to indicate the statistical sensitivity of $F_{yw}$ to discharge, where discharge is a proxy indicator of catchment wetness conditions and hydro-climatic forcing. Catchments with high discharge sensitivity of $F_{yw}$ (steep linear slope in Eq. 9) are ones in which the young water fraction varies greatly between low and high flows, suggesting that faster flow paths are more predominant in larger events. Conversely, catchments with low discharge sensitivity (shallower linear slopes in Eq. 9) are ones in which young water fractions are broadly similar between low and high flows, sug-
suggesting that the same predominant flow paths are activated in similar proportions in both large and small runoff events.

On average, we find that every 1 mm day\(^{-1}\) increase in discharge is associated with an increase of 0.0202 ± 0.0046 in \(F_{yw}\). From this analysis, we excluded the Aach catchment because only two streamwater samples were collected during high-flow conditions, resulting in an unrealistic and highly uncertain value for \(m_S\). At the remaining 21 sites, the discharge sensitivities of \(F_{yw}\) range between zero (within error) at Ilfis and Sitter, and 0.0732 ± 0.0360 day mm\(^{-1}\) at Mentue. A similar analysis was carried out by Wilusz et al. (2017) for two neighbouring catchments in Plynlimon, Wales. For those two sites, Wilusz et al. (2017) combined a rainfall–runoff model with a rank storage selection (rSAS) transit time model and estimated an increase in \(F_{yw}\) of 0.031 to 0.040, respectively, with every 1 mm day\(^{-1}\) increase in average annual precipitation. Multiplying their “precipitation sensitivities of \(F_{yw}\)” by the site-specific runoff ratios (0.78 and 0.90) yields average discharge sensitivities of \(F_{yw}\) of 0.0242 and 0.0360 day mm\(^{-1}\), respectively, which are within the range of values we obtained for our 22 Swiss study sites.

Even though the methods, tracers, and timescales Wilusz et al. used to estimate \(F_{yw}\) differed from ours, the similarity in the discharge sensitivities between their sites and ours suggests that this may be a robust and reproducible metric that could be useful in future catchment studies.

For our study catchments, there was no systematic relationship between the young water fraction (either \(F_{yw}\) or \(F_{yw}^b\)) and the discharge sensitivity, indicating that they are different and largely independent measures of catchment behaviour (Figs. 8 and 9). The discharge sensitivity of \(F_{yw}\) is, however, strongly correlated to a range of landscape and hydro-climatic conditions, including \(\overline{P}\) (\(\rho = -0.64\), see also Fig. 9b), \(\overline{Q}_{\text{intensity}}\) (\(\rho = -0.56\)), \(\overline{Q}\) (\(\rho = -0.61\)), \(DD\) (\(\rho = -0.59\)), \(L/G\) (\(\rho = 0.75\)), \(L\) (\(\rho = 0.46\)), \(G\) (\(\rho = -0.46\)), \(TWI\) (\(\rho = 0.52\)), \(A_{\text{precip}}\) (\(\rho = -0.44\)), and mean catchment elevation (\(\rho = 0.64\)). All of these correlations remain statistically significant (and many become stronger) when the snow-dominated sites are excluded from the analysis.

In contrast, calculating linear slopes between \(F_{yw}\) and \(\log(Q)\), instead of \(Q\), yields no significant correlations with any of the variables in Tables 2 or S1. It should be noted that calculations based on \(\log(Q)\) will be more strongly influenced by small discharges, whereas calculations based on \(Q\) will be more strongly influenced by the upper tail of the \(Q\) distribution. Thus, since our primary focus is storm runoff generation, we interpret the discharge sensitivities of \(F_{yw}\) based on \(Q\) instead of \(\log(Q)\).

Our results suggest that catchments with low discharge sensitivity of \(F_{yw}\) are characterized by high elevations, dense river networks (high \(DD\), low \(L/G\)) and/or generally humid conditions (high \(\overline{P}\)). These catchment properties are generally associated with predominantly shallow runoff flow paths during both large and small precipitation events, such that the fraction of young water remains relatively high under widely varying flow regimes. In contrast, in catchments characterized by lower drainage density and less humid conditions, larger or higher-intensity storms are likely to strongly alter the proportions of different dominant flow paths, leading to bigger variations in \(F_{yw}\) (i.e. higher discharge sensitivity). For example, the dynamic extension of the stream network (e.g. Godsey and Kirchner, 2014; Jensen et al., 2017) and/or the increase in hydrologic connectivity between the stream network and the surrounding landscape (e.g. Detty and McGuire, 2010; Phillips et al., 2011; von Freyberg et al., 2015) should more strongly influence the relative proportion of young streamflow in catchments where drainage density is not already high. Likewise, the activation of shallow flow paths during larger storm events will have a bigger influence on \(F_{yw}\) in drier catchments than in wetter ones, where shallow flow paths are likely to be activated during both large and small events.

Interestingly, although \(F_{yw}\) and its discharge sensitivity are not significantly correlated with each other, they are often correlated with catchment characteristics in opposite ways (Table 4). For example, \(DD\), \(\overline{Q}\), \(\overline{P}_{\text{intensity}}\), \(QFI\), and \(CV_{\overline{Q}}\) exhibit positive correlations with \(F_{yw}\) but also exhibit negative correlations with the discharge sensitivity of \(F_{yw}\). In catchments with dense river networks and/or generally hu-

![Figure 9. (a) Flow-weighted young water fractions at the 22 Swiss study catchments; (b) discharge sensitivity of \(F_{yw}\) at the same sites (mean annual precipitation for the period 1991–2010 is shown for comparison).](image-url)
mid climates, fast runoff flow paths will dominate (and thus $F_{yw}$ and $F_{yw}^*$ will be high). These same conditions should also make fast runoff flow paths more persistent, with the result that the young water fraction will not be strongly dependent on catchment wetness conditions or hydro-climatic forcing (and thus discharge sensitivity will be low).

5.4 A conceptual model of the mechanistic relationship between young water fractions and discharge

Figure 10 presents a conceptual summary of the relationships between the young water fraction, its discharge sensitivity, and landscape and hydro-climatic characteristics that control streamflow generation. We suggest that the general trend of the $Q–F_{yw}$ relationship is positive because high-flow periods during precipitation events are likely to contain larger fractions of young water travelling by quick flow paths, while low-flow conditions are primarily sustained by older groundwater. In Fig. 10, the steepness of the linear slope expresses how extensively fast flow paths are activated during high flows. In theory, a linear slope of zero (i.e. $F_{yw}$ insensitive to discharge) would represent strictly linear rainfall–runoff behaviour with a constant mixing fraction of young and old water. In natural systems, however, the relative proportions of streamflow generation mechanisms are likely to vary between high and low flows, making $F_{yw}$ sensitive to discharge.

From our analyses in Sect. 6.1. and 6.2, we find that low discharge sensitivities of $F_{yw}$ can occur at sites with either high or low young water fractions (cases 1 and 3, respectively, in Fig. 10; e.g. Erlenbach and Ilfis, respectively, in Fig. 7). Case 1 might be found in humid catchments with frequent precipitation, low storage capacity, and dense river networks, where shallow runoff flow paths dominate both during and between events (e.g. triggered by saturation excess). Case 3 is more likely to occur in catchments with high infiltration capacity and large subsurface storage, where slow subsurface flow paths dominate both during events and between them, leading to consistently low young water fractions. A steep linear slope (case 2 in Fig. 10; e.g. Alp, Biber or Murg in Fig. 7) is likely to occur in catchments where the relative contributions of fast and slow flow paths vary dramatically in response to hydro-climatic forcing or antecedent wetness conditions, for example through drainage network expansion, or shifts in hydrological connectivity due to groundwater tables rising into more permeable layers.

The hydrological concepts presented in Fig. 10 are based on the young water fraction analysis for 21 Swiss catchments that share several landscape and hydro-climatic characteristics, such as similar vegetation cover, relatively humid climate, and (partly) mountainous terrain. Hence, we must be cautious about extending this conceptual model to regions characterized by (semi-)arid or arctic climates, very different vegetation cover or predominantly flat terrain. In addition, linking young water fractions to catchment wetness conditions and hydro-climatic forcing may be difficult in catchments with streamflow regimes that are discontinuous or strongly affected by lakes, water management (e.g. groundwater pumping, artificial groundwater recharge, irrigation, or water diversion) or land-use change (e.g. urban development, soil degradation, or forest clear cutting). Nevertheless, long-term tracer data sets from other catchments could be used to expand our analysis beyond the Swiss study sites and to test the transferability of the conceptual model presented in Fig. 10.
6 Summary and conclusions

The fraction of streamflow younger than roughly 2–3 months has recently been proposed as a robust measure of water age which can be estimated directly from the seasonal cycles of stable water isotopes in precipitation and streamflow (Kirchner, 2016a, b). Here, we have leveraged an extensive isotope data set from 22 small- to medium-sized Swiss catchments to explore how the young water fraction ($F_{yw}$) varies with catchment characteristics and climatic forcing.

Catchment inter-comparison studies require application of consistent procedures across sites, so we quantified how choices of methodology may affect estimates of $F_{yw}$. Across the 22 sites, $F_{yw}$ values were not particularly sensitive to the spatial interpolation methods used to estimate precipitation isotope signatures (Sect. 4.1), or sensitive to whether one accounts for snow accumulation and melt in estimating isotopic inputs to the catchment (Sect. 4.2). Flow-weighting the streamwater isotope measurements, however, yielded flow-weighted young water fractions ($F^*_{yw}$) that were roughly 26% larger than their unweighted counterparts ($F_{yw}$; Sect. 4.3, Fig. 5). This result is not surprising, because flow peaks typically follow intense rainfall and thus should contain more recent precipitation than base flows. Here we quantify, for the first time, how flow-weighting affects young water fractions, using real-world data.

The flow-weighted young water fractions of the 22 Swiss catchments ranged from 0.07 ± 0.01 to 0.49 ± 0.03 (±SE), whereas the unweighted $F_{yw}$ were slightly smaller, ranging from 0.06 ± 0.01 to 0.37 ± 0.03. The $F_{yw}$ values from our study sites span roughly the 10th to 80th percentiles of the $F_{yw}$ values estimated by Jasechko et al. (2016) for 254 rivers around the world. The median $F_{yw}$ among the 22 Swiss catchments was 0.16 (95% confidence interval 0.10–0.21), somewhat less than the global median of 0.21 (95% confidence interval 0.19–0.24; Jasechko et al., 2016), consistent with Jasechko et al.‘s (2016) observation that young water fractions tend to be smaller in steeper landscapes. Among the 22 Swiss catchments, $F_{yw}$ and $F^*_{yw}$ were positively correlated with catchment characteristics that control wetness conditions (e.g. mean monthly precipitation and mean precipitation intensity) and near-surface flow routing (e.g. drainage density and areal fractions of saturated soils; Sect. 5).

By calculating young water fractions for individual ranges of streamflow, we demonstrated that young water fractions generally increase with discharge ($Q$), and that this sensitivity of $F_{yw}$ to $Q$ varies from site to site (Sect. 6.1, Fig. 8). We developed a method to quantify the discharge sensitivity of $F_{yw}$ through calculating the linear slope of the $Q$–$F_{yw}$ relationship (Eqs. 6 to 9). The discharge sensitivity expresses how $F_{yw}$ responds to changes in river discharge, which is used here as a proxy for catchment wetness and hydro-climatic forcing. Across our study catchments, the young water fraction and its discharge sensitivity were not correlated with each other, suggesting that these metrics repre-


