The influence of tree and branch fracture, overturning and debris entrainment on snow avalanche flow

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ABSTRACT. A simple center-of-mass avalanche model that accounts for avalanche flow in forests is presented. The model applies the principle of conservation of energy to calculate the deceleration of avalanches caused by tree fracture, overturning and debris entrainment. The model relates the physical properties of forests (tree spacing, tree age, tree type, soil conditions) to avalanche flow. Modified dry-Coulomb and velocity-dependent friction parameters commonly used in avalanche runout calculations are derived. Example calculations demonstrate how the model can be applied to back-calculate observed avalanche events. The model quantitatively explains why large avalanches can destroy forests without significant deceleration. Furthermore, it shows why tree fracture consumes little of the avalanche’s energy. Finally, the model reveals how protective forests in avalanche tracks can be maintained over time to provide the best protective capacity against snow avalanches.

1. MOTIVATION

Snow avalanches can destroy large tracts of mountain forests. This was clearly evident during the extreme avalanche winters of 1951 and 1999, when large avalanches easily demolished tree stands of various ages (SLF, 1951, 2000). Quite often the fractured tree debris was entrained into the snow flow. Avalanche deposits were strewn with large tree trunks, lopped branches, wood fragments, root clusters and eroded soil (Fig. 1).

The importance of protective forests in preventing avalanches from starting has been studied by De Quervain (1979), Salm (1979) and Gubler and Rychetnik (1994). The purpose of these works was to establish the tree spacing required to stabilize the snowpack on forested slopes. The inclusion of forests in avalanche-dynamics calculations, however, has not been studied in detail. This is understandable, given that there are even now still many unanswered questions dealing with snow flow in open, i.e. unforested, terrain.

The Swiss Guidelines on avalanche-runout calculation specify that the velocity-dependent friction parameter used in model calculations can be increased on forested slopes (Salm and others, 1990). The dry Coulomb friction values remain unchanged. This procedure decreases the predicted terminal velocity of the avalanche significantly, yet decreases the predicted runout distances only slightly (Bartelt and others, 1999). This empirical approach is based on extensive model calibration (Buser and Frutiger, 1980). Since these model calculations have been calibrated using observed runout distances, the requisite of decreasing the velocity-dependent friction can clearly be questioned. Furthermore, in practice hazard maps are prepared by using model calculations that assume the forest no longer exists to slow the avalanche down. The safe assumption must always be made that a tree stand has been destroyed by a previous avalanche.

In summary, the problem of avalanche flow in forests is both highly complex and has little practical priority. Nonethe-

Fig. 1. Avalanche deposits at Evolène, Switzerland. Note the size of the fractured tree trunks and amount of wood debris. The runout distance of this avalanche was correctly predicted without considering the influence of the forest.
eters such as height, girth, branchiness and root-system strength. We will apply the principle of conservation of energy to a center-of-mass avalanche model to derive friction formulas for the mean deceleration of snow avalanches. This is a first step in developing friction laws for advanced numerical models. The principal problem that must be solved is to relate the mechanical properties of trees to the dynamics of snow avalanche flow.

An important distinction must be made from the beginning between avalanche flow force and flow energy. We assume that the avalanches are sufficiently large and fast-moving to enable the forces they apply to the trees to fracture or overturn them. We do not consider how the avalanche force is applied to the trees. In fact, the trees which are entrained in the flow will smash into other trees, applying the force of the avalanche in an arbitrary and completely in calculable manner. Many foresters believe that this “battering-ram” effect is the main cause of forest destruction. In the following, we will assume that this destructive force will always be enough to destroy the remaining trees. How the force is applied is immaterial to our analysis. We are not interested in the fracture stress or overturning moment which must be overcome, rather in the fracture energy. Small or slow-moving avalanches which, because they exert small forces, do not destroy the forest are of little interest. If the entrained trees block the path of the avalanche by becoming tangled in the standing trees, the avalanche at that moment simply does not have the force to destroy the forest. Of course the locked trunk trees will increase the internal flow resistance. But this will only occur when the avalanche is already close to stopping.

The above explanation is central to understanding why mountain forests offer little protection against snow avalanches once the avalanches have already started and reached a critical flow energy. It reveals the gist of our calculations and explains the massive forest destruction during the winters of 1951 and 1999: trees can resist large forces, but on breaking consume little of the avalanche’s flow energy. In the following we will try to prove this supposition. At what critical flow velocity the trees break or overturn must be the topic of another work.

2. MATHEMATICAL DESCRIPTION OF A FOREST AND PRINCIPAL MODES OF FOREST FAILURE

We assume, based on our field observations, that a forest is damaged or destroyed according to one of the following four causes:

Tree fracture and entrainment

A flowing avalanche fractures and entrains the trees in the flow. The fracture energy, $\omega_f$, is assumed to be linearly proportional to the the trunk's cross-sectional area. Values of $\omega_f$ can be found in Sell (1987). We will assume that the tree trunks have a constant girth of radius $r_t$. The girth is constant over the entire tree height, $h_t$. The mass of the tree is $m_t$. For the moment, we will assume that the tree fractures at the base of the trunk and the entire tree is entrained. The center of mass of the trunk is denoted by $Z_t$. The number of trees entrained per unit time, $n_t$, is given by (1) the mean tree spacing in the direction of flow $d_t$ (2) the tree spacing along the width of the avalanche, $d_w$ (3) the avalanche’s speed $u$ and (4) the width, $w$, of the avalanche (see Fig. 2),

$$n_t = \frac{w d_w}{d_t d_w}.$$  

(1)

Tree overturning

An avalanche overturns trees. The breaking energy is approximated by assuming that the failure stress on the overturning slip surface is given by a Mohr–Coulomb failure criterion:

$$\tau_t = c + \sigma_t \tan \delta,$$  

(2)

where $\tau_t$ is the shear stress acting on the wedge failure surface and $\sigma_t$ is the overburden stress. The parameters $c$ and $\delta$ are the cohesion and internal flow friction of the mountain soil. The overturning wedge is a half-cylinder with radius $r_t$ and length $2r_t$. Overturning is thus defined by three parameters, the internal friction angle $\delta$ of the soil, the soil cohesion, $c$, and the failure radius of the root cluster, $r_t$. The overburden stress is clearly a function of tree mass.

Tree overturning with entrainment

Observations of avalanche deposits reveal that entire overturned trees are entrained in the flow and are carried long distances (Fig. 3). In this case, the influence of overturning and that of entrainment are added to find the total avalanche deceleration.

Trunk fracture and branch lopping

Powder-snow avalanches will often fracture the trunks of trees but will not entrain them in the avalanche flow. In this case, we consider the deceleration caused by fracture alone. Often the trunks will remain standing but are completely stripped of their branches. Tree lopping by powder-snow ava-
lances is a special case which requires the introduction of an additional tree parameter, the mean branch spacing, \( d_0 \). The number of branches fractured per tree per unit time is

\[
n_t = \frac{h_t w u}{d_0 d_b d_w}.
\]  

(3)

The branches have mean length, \( h_b \). We will assume that the fracture energy per cross-sectional area of the branches is the same as that of the trunk. This is probably not the case, but we have found no experimental data to allow a more realistic modeling.

In summary, the above failure modes involve three physical processes: fracture, overturning and entrainment. The avalanche decelerations produced by each of these processes are derived in the following sections.

### 3. ENERGY ANALYSIS

We determine the motion of an avalanche moving down a slope of constant angle \( \psi \) between two discrete times, \( t_0 \) and \( t_1 \). At time \( t_0 \) the avalanche is moving with velocity \( u_0 \) and has flow height \( h_0 \) and length \( l_0 \) (see Fig. 4). At time \( t_1 \) the avalanche has flow velocity \( u_1 \) and height \( h_1 \) and length \( l_1 \) (see Fig. 5). Between time \( t_0 \) and \( t_1 \) (time interval \( \Delta t \)) the avalanche changes velocity by \( \Delta u \):

\[
u_1 = u_0 + \Delta u.
\]  

(4)

The avalanche penetrates the distance \( u_0 \Delta t \) into the forest. Over the same time interval, the center of mass of the avalanche moves downwards from height \( Z_0 \) to \( Z_1 \). Application of the principle of conservation of energy at positions 0 and 1 leads to

\[
m_0 g Z_0 + m_0 \frac{u_0^2}{2} = m_1 g Z_1 + m_1 \frac{u_1^2}{2} + \hat{E} \Delta t,
\]  

(5)

where \( \hat{E} \) is the energy required per unit time to either fracture or overturn the trees. Values for \( \hat{E} \) are derived in sections 4 and 5. In the following, the energy equation will be solved to find \( \Delta u/\Delta t \), the avalanche deceleration. The center of mass of the avalanche at position 1 defined in relation to \( Z_0 \) is

\[
Z_1 = Z_0 - u_0 \Delta t \sin \psi + \frac{\Delta h}{2} \cos \psi + \frac{\Delta l}{2} \sin \psi.
\]  

(6)

For the special case when \( \hat{E} = 0 \) and when the avalanche does not change mass \( (m_1 = m_0) \) or shape \( (\Delta l = \Delta h = 0) \), the trivial solution is obtained,

\[
\frac{\Delta u}{\Delta t} = a_0 = g \sin \psi.
\]  

(7)

This result is found by substituting Equations (4) and (6) into Equation (5) and neglecting all second-order terms, i.e. assuming terms such as \( (\Delta t)^2 \) or \( (\Delta u/\Delta t) \) are zero.

### 4. TREE ENTRAINMENT

Because it entrains debris, the avalanche grows in mass and volume. The change in mass over the time interval \( \Delta t \) is

\[
\Delta m_e = n_t m_e \Delta t.
\]  

(8)

Subsequently, the mass of the avalanche at position 1 is

\[
m_1 = m_0 + \Delta m_e.
\]  

(9)

The mean flow density of the avalanche is denoted \( \rho_e \). The volume of the avalanche is

\[
V = wh_l,
\]  

(10)

and thus the volume change within the time interval \( \Delta t \) is

\[
\Delta V = w \Delta h + w \Delta l \Delta t.
\]  

(11)

Assuming small time-steps, the last (second-order) term in Equation (11) will be small and neglected in future calculations. The width of the avalanche does not change. We define a parameter \( \gamma \) such that

\[
\gamma \Delta V = w \Delta h \quad \text{and} \quad (1 - \gamma) \Delta V = w \Delta l.
\]  

(12)

Since the trees are incompressible, the change in volume of the avalanche over the time interval \( \Delta t \) is

\[
\Delta V = n_t V_1 \Delta t,
\]  

(13)

where \( V_1 \) is the tree volume. We express the tree volume as

\[
V_1 = \theta_1 V,
\]  

(14)

where \( \theta_1 \) is the volumetric tree content defined over the volume

\[
V = d_e d_b h_e.
\]  

(15)

Thus, the change in height and length of the avalanche can be calculated according to

\[
\Delta h = \frac{\gamma}{l} w \theta_1 h_1 \Delta t
\]  

(16)

and

\[
\Delta l = \frac{1 - \gamma}{h} w \theta_1 h_1 \Delta t.
\]  

(17)

The dimensionless parameter \( \gamma \) allows for different rates of avalanche growth in the length and height directions. For
γ = 0, the entrained tree mass increases exclusively the length of the avalanche. For γ = 1 the entrained tree mass increases the avalanche flow height.

The energy-balance Equation (5) can now be written

\[ m_0 g Z_0 + m_0 \frac{u_0^2}{2} + \Delta m_e g Z_e = \left( m_0 + \Delta m_e \right) \left( g Z_1 + \frac{u_1^2}{2} \right), \]

(18)

where the position of the center of mass \( Z_e \) (entrained tree mass) is defined according to Figure 5 and given by

\[ Z_e = Z_0 - \frac{1}{2} \left( l_0 + u_0 \Delta t_1 \right) \sin \psi - \frac{1}{2} h_0 \cos \psi + Z_i. \]

(19)

Note that the potential energy of the trees is considered in the term \( \Delta m_e g Z_e \). For the moment, we will assume that \( E \) is zero in order to study the deceleration of the avalanche caused by tree entrainment alone.

The deceleration of an avalanche caused by tree entrainment can be found by substituting the equations for \( u_1 \) (Equation (4)), \( Z_1 \) (Equation (6)), \( \Delta m_e \) (Equation (8)) and \( Z_e \) (Equation (19)) into Equation (18):

\[ a_{et} = -k \frac{v_0^2}{2} - \frac{g \theta_1 h_0}{2} \left( \frac{\gamma}{l_0} \cos \psi + 1 - \frac{\gamma}{h_0} \sin \psi \right) - k g Z_1, \]

(20)

where

\[ k = \frac{m_t}{\rho_t l_0 h_0 d_w d_l}. \]

The derivation of Equation (20) again neglects all second-order terms.

The equation for \( a_{et} \) contains the term, \( k (v_0^2/2) \), indicating that mass entrainment introduces a velocity-dependent deceleration. The term \( k g Z_1 \) represents the avalanche acceleration (note sign) caused by the falling trees, i.e., it represents potential energy of the trees that is added to the flow energy of the avalanche. The remaining terms in the equation arise because the center of mass of the avalanche moves as the avalanche grows in length and height.

### 5. TREE FRACTURE AND BRANCH LOPPING

The decelerations caused by tree-trunk and branch fracture are given by

\[ a_{t} = - \frac{u_1 \pi r_t^2}{\rho_t d_t d_l h_0 l_0}, \]

(22)

and

\[ a_{b} = - \frac{u_1 \pi r_b^2}{\rho_b d_b d_l h_0 l_0}, \]

(23)

respectively. These expressions are found by again applying the conservation-of-energy Equation (5), with the energy consumption rate, \( \dot{E}_t \), which is the total fracture energy per unit time for either the tree trunks or branches,

\[ \dot{E}_t = n_t u_1 \pi r_t^2 = \frac{w}{d_t} \frac{u_0}{d_t} u_1 \pi r_t^2 \]

(24)

\[ \dot{E}_b = n_b u_1 \pi r_b^2 = \frac{h_0}{d_b} \frac{w}{d_b} \frac{u_0}{d_b} u_1 \pi r_b^2. \]

(25)

We have considered the case of branch fracture separately because often powder-snow avalanches will effectively lop the branches of trees, leaving the trunks standing. Note the appearance of the parameter \( d_w \), the mean branch spacing in the equation for \( \dot{E}_b \). Typical values for \( u_t \) are given in Table 1.

<table>
<thead>
<tr>
<th>Tree</th>
<th>Fracture energy (J cm⁻²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pine</td>
<td>6.0 - 70</td>
</tr>
<tr>
<td>Fir</td>
<td>3.5 - 6.5</td>
</tr>
<tr>
<td>Beech</td>
<td>8.0 - 12.0</td>
</tr>
<tr>
<td>Larch</td>
<td>5.0 - 7.5</td>
</tr>
<tr>
<td>Spruce</td>
<td>4.0 - 5.0</td>
</tr>
</tbody>
</table>

Note: The data are taken from Sell (1987). The values reported are for dry, dead wood.

### 6. TREE OVERTURNING

When trees overturn, a lump of soil is uprooted containing the root cluster and surrounding soil. Matteck identified two primary lump shapes: a half-cylinder and a half-sphere (Matteck and Breier, 1993). In the following we will consider the case of a half-cylinder with failure radius \( r_f \) and length \( 2r_f \). We assume that the failure surface of the lump lies outside the extent of the root cluster and that the overturning is governed by the strength of the soil and by \( r_f \). Trees with shallow root systems will have smaller \( r_f \) values and subsequently smaller overturning energies. The fracture energy of the roots is not considered in the analysis.

The mass of the lump is

\[ m_o = \rho_o \pi r_f^3, \]

(26)

where \( \rho_o \) is the density of the soil. When the trees overturn they are pressed flat by the avalanche on to the ground surface. This means that the centroid of the half-cylinder is raised the vertical distance (see Fig. 3),

\[ \Delta h = \frac{4r_f}{3\pi} (\cos \psi + \sin \psi). \]

(27)

The energy required to raise the weight of the root-cluster mass, \( e_w \), is

\[ e_w = \frac{4 \rho_o \pi r_f^3}{3} (\cos \psi + \sin \psi). \]

(28)

Although the cylinder rotates a total distance,

\[ S_d = \left( \frac{\pi}{2} + \psi \right) r_f, \]

(29)

we will assume, however, for the energy analysis that the slip length, \( S_a \), is given by

\[ S_a = 2 \delta r_f, \]

(30)

where \( \delta \) is the angle of internal friction (see Fig. 6). The length of the slip surface is the length of the failure arc where the self-weight of the tree acts. After displacing this distance
The overburden stress, $\sigma_o$, acting on the slip surface is composed of two parts. The first, $\sigma_{o}$, arises from the tree weight,

$$
\sigma_o = \frac{4r_f}{3\pi} \rho_o g \cos \psi.
$$

The total overturning work for a single tree, found from Equation (31), is

$$
e_o = 8r_f^3 \delta^2 \left[ c + \left( \frac{m_t g}{4r_f^2} + \frac{4r_f}{3\pi} \rho_o g \cos \psi \right) \tan \delta \right]
+ \frac{4\rho_o g r_f^2 \pi}{3} (\cos \psi + \sin \psi).
$$

The factor $8r_f^3 \delta^2$ arises from the multiplication of the slip length $S_o$ with the mean force $f_o$. Again, $\delta$ is expressed in radians. The total energy rate, $\dot{E}_o$, of tree overturning is a function of the number of trees the avalanche overturns per unit time,

$$
\dot{E}_o = n_e e_o.
$$

When this value is substituted into the conservation-of-energy equation (Equation (5)), we find the deceleration of the avalanche caused by tree overturning is

$$
a_o = \frac{8r_f^3 \delta^2}{\rho_o d_l h_o d_w d_l} \left[ c + \frac{m_t g}{4r_f^2} + \frac{4r_f}{3\pi} \rho_o g \cos \psi \right] \tan \delta
+ \frac{4\rho_o g r_f^2 \pi}{3} (\cos \psi + \sin \psi).
$$

The first term in the above equation arises from the Mohr–Coulomb failure criterion; the second term arises from raising the lump centroid. Note that the second term is a function of $r_f^2$. This implies that large amounts of energy can be consumed when raising the lump masses; however, this will probably not occur: the trees will fracture before trees with expansive root systems are overturned.

Considering an Alpine soil with $\delta = 30^\circ$, $c = 5\text{kPa}$, $\rho_o = 2000\text{ kg m}^{-3}$ and trees weighing $m_t = 1000\text{ kg}$ with $r_f = 2\text{m}$, we find that the deceleration caused by raising the root cluster is greater than the work required to overcome the shear failure stress.

7. RUNOUT CALCULATIONS

The Swiss Guidelines on avalanche-runout calculation employ the Voellmy–Salm model to predict runout distances (Voellmy, 1955; Salm and others, 1990). Avalanche deceleration, $a_{vs}$, is governed by a dry-Coulomb-like friction and a velocity-dependent friction,

$$
a_{vs} = -(bg \cos \psi + su^2).$$

Suggested values for the parameters $b$ and $s$ are provided in the guidelines. These values have been determined by back-calculating observed avalanche events (Buser and Frutiger, 1980).

For flow in forests, the parameter $s$ is approximately doubled; the dry-friction parameter remains unchanged.

The energy analysis allows us to determine how the friction parameters $b$ and $s$ should be modified to take into account flow through forests. Let $\Delta b$ and $\Delta s$ represent the increase in flow friction caused by tree entrainment and fracture. A comparison to Equation (20) (entrainment) and Equation (22) (trunk fracture) shows that

$$
\Delta s = \frac{m_t}{2 \rho_o d_l h_o d_w d_l}
$$

and

$$
\Delta b = \frac{u_t \pi r_f^2}{\rho_o d_w d_l h_o d_l} \frac{1}{g \cos \psi}.
$$

In order to double the velocity-dependent friction $s$ (as specified by the Swiss Guidelines), requires a biomass loading (tree mass per square meter of forest) of the order

$$
350\text{ kg m}^{-2} \leq \frac{m_t}{d_w d_l} \leq 500\text{ kg m}^{-2}.
$$

Table 2 presents some typical biomass loadings as a function of tree size, spacing and branch weights. Two conclusions can be drawn from Table 2. Firstly, the change in dry friction is
small, thus confirming the guiding principle of increasing only the velocity-dependent friction, and, secondly, the biomass loadings of typical forests are smaller than assumed by the Swiss Guidelines (Equation (43)). The mass entrained by the avalanche, however, will certainly be increased if the avalanche additionally erores the snowpack and part of the soil cover. Field observations would support this supposition. Therefore, the entrained mass values required to double the velocity-dependent friction as specified by the Swiss Guidelines (Equation (43)) are easily attainable. For example, if an avalanche entrained a forest with $m_t/d_w d_l = 150$ kg m$^{-2}$ (see Table 2), a 0.5 m high snowpack with a density of 300 kg m$^{-3}$ and additionally 10 cm of soil with density $\rho_s = 2000$ kg m$^{-3}$ then the total mass per square meter entrained by the avalanche is 500 kg m$^{-2}$.

### 8. EXAMPLE CALCULATIONS

A simple explicit time-integration procedure was written to track the motion of an avalanche given an initial size and velocity. The total acceleration of the avalanche is determined according to one of five cases:

1. **No forest**
   
   $$a = a_k + a_v.$$  

2. **Tree fracture and branch lopping**
   
   $$a = a_k + a_v + a_a + a_o.$$  

3. **Tree fracture and entrainment**
   
   $$a = a_k + a_v + a_a + a_e.$$  

4. **Overturning**
   
   $$a = a_k + a_v + a_o.$$  

5. **Overturning and entrainment**
   
   $$a = a_k + a_v + a_a + a_e.$$  

Consider the following case: A flowing avalanche with dimensions $h_0 = 3$ m and $l_0 = 100$ m is flowing with a velocity of 20 m s$^{-1}$ down a 30° slope and impacts a 150 year old spruce forest. The average spacing of the trees is $d_w = d_l = 4$ m. The trees have an average height of 20 m and girth of 40 cm ($r_t = 20$ cm). The center of mass of the trees is located at $Z_t = 70$ m. The tree branches are on average 3 m long with 5 cm radius. For 15 m of the tree's length, five branches are located at 20 cm intervals. Since only half of the branches are fractured we find $d_o = 10$ cm. The properties of the mountain soil are $c = 5000$ Pa, $\delta = 30°$ and $\rho_s = 2000$ kg m$^{-3}$. We assume that $r_t = 1$ m.

Figures 7 and 8 compare the velocity of the avalanche over the flow distance for several cases. The results are always compared to the case of no forest to clearly show the influence of the forest. Note that the avalanche is moving down a steep slope and thus continues to accelerate over the distance of 750 m.

The calculations clearly show that the avalanches are not decelerated by fracturing or overturning trees, but rather by entraining them into the flow. There is no significant difference between the no-forest case and the cases of tree fracture and tree overturning. Although entraining fractured tree debris slows the avalanche down, the deceleration may not be significant. Instead of reaching a velocity of 45 m s$^{-1}$, the avalanche reaches a velocity of 42 m s$^{-1}$. The reason why tree overturning with entrainment decelerates the avalanche more noticeably (the avalanche reaches a velocity of only 27 m s$^{-1}$) is that the heavy root cluster is entrained in the flow.

The avalanche had a relatively small initial volume of 30 000 m$^3$. Larger avalanches would be slowed down even less.

### Table 2. Biomass loading and change in dry-friction parameter $b$ as a function of tree height $h_t$, trunk radius $r_t$, branch spacing $d_w$, foliage height $h_f$, branch weight $m_b$, and spacing $d_w d_l$

<table>
<thead>
<tr>
<th>Tree height (m)</th>
<th>Trunk radius (m)</th>
<th>Branch spacing (m)</th>
<th>Branch mass (kg)</th>
<th>Foliage height (m)</th>
<th>Tree spacing (m)</th>
<th>Biomass loading ($\Delta b$) (kg m$^{-2}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>5.0</td>
<td>0.075</td>
<td>0.20</td>
<td>2.0</td>
<td>5.0</td>
<td>1.0</td>
<td>225</td>
</tr>
<tr>
<td>10.0</td>
<td>0.075</td>
<td>0.50</td>
<td>2.0</td>
<td>7.0</td>
<td>4.0</td>
<td>50</td>
</tr>
<tr>
<td>15.0</td>
<td>0.100</td>
<td>0.50</td>
<td>3.0</td>
<td>12.0</td>
<td>10.0</td>
<td>85</td>
</tr>
<tr>
<td>20.0</td>
<td>0.100</td>
<td>0.50</td>
<td>3.0</td>
<td>15.0</td>
<td>10.0</td>
<td>98</td>
</tr>
<tr>
<td>20.0</td>
<td>0.150</td>
<td>0.50</td>
<td>4.0</td>
<td>10.0</td>
<td>10.0</td>
<td>144</td>
</tr>
<tr>
<td>30.0</td>
<td>0.200</td>
<td>0.50</td>
<td>5.0</td>
<td>20.0</td>
<td>25.0</td>
<td>152</td>
</tr>
<tr>
<td>30.0</td>
<td>0.150</td>
<td>0.50</td>
<td>5.0</td>
<td>20.0</td>
<td>36.0</td>
<td>70</td>
</tr>
</tbody>
</table>

Note: The density of wood is taken to be $\rho_w = 850$ kg m$^{-3}$. The calculation of $\Delta b$ is based on fracture energies of $u_k = 5.1$ J cm$^{-2}$.
Fig. 8. Tree overturning. (a) Comparison of the velocity of the avalanche over open terrain and over forested terrain when 150 year old spruce trees are overturned. (b) The overturned trees are entrained in the flow. Avalanches can be decelerated if they entrain the heavy root cluster.

Fig. 9. The difference between tree fracture with entrainment and tree overturning. An avalanche of 30 000 m$^3$ impacts a 30 year old forest. The overturning failure radius of the $h_t = 5$ m trees is $r_1 = 100$ cm. (a) Avalanche deceleration when the trees fracture and are entrained in flow. (b) Avalanche deceleration when the trees overturn.

properties of the soil ($\delta$ and $c$) and wood remain unchanged. We compare two cases: tree fracture with entrainment and tree overturning without entrainment. We assume that the failure radius of the root system is $r_1 = 100$ cm. The results are displayed in Figure 9. In this example, tree overturning decelerates the avalanche more than trunk fracture with entrainment.

9. CONCLUSIONS

In this paper we presented a simple center-of-mass avalanche model that accounts for avalanche flow in forests and distinguishes between two different modes of tree failure: fracture and overturning (with or without debris entrainment). We showed that large avalanches can destroy forests without significant deceleration. This fact explains the observations of the 1951 and 1999 winters where avalanches flowed long distances while destroying large tracts of forests.

The analysis procedure relates forest properties directly to avalanche-flow friction parameters. The energy analysis avoids the problem of determining how the destructive force of avalanches is applied to fracture or overturn trees. However, it cannot predict for what avalanche size or flow velocity the trees will be destroyed, since this requires knowing how the force is applied to the trees. The energy analysis assumes that the avalanches are sufficiently large to destroy the forests.

We expressed avalanche deceleration in terms of Swiss Guideline friction parameters. We showed that the velocity-dependent friction accounts for tree, snow and soil-cover entrainment. The dry-Coulomb friction parameter can be modified to include tree fracture and overturning.

Our calculations revealed that debris entrainment slows down an avalanche more than tree fracture. If a storm damages a protective forest it would therefore be advantageous to keep the tree debris in place. We also showed that an older forest can decelerate smaller avalanches (say, <30 000 m$^3$) significantly when the trees overturn and the avalanche entrains the heavy root cluster. In all cases, when the trees fracture they consume very little of the avalanche's flow energy.

In conclusion, we believe that the most important contribution of this paper is that it relates parameters such as tree spacing, girth and height to the deceleration of avalanches. In future, this will help practitioners to classify forest damage (fracture and overturning), understand avalanche events better (why an avalanche stopped or flowed a long distance), provide a scientific method to investigate the mechanical properties of forests and trees, and finally to care for mountain forests so that they always, irrespective of age, provide the maximum protective capacity against snow avalanches.

REFERENCES


